

# Fracture of sea ice by ocean surface waves in CESM3

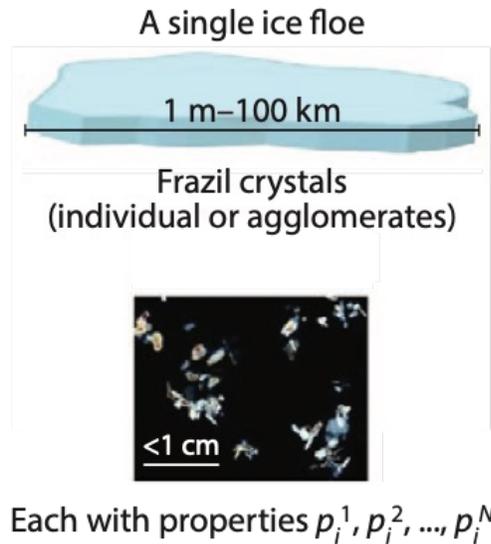
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Lettie Roach  
*Alfred Wegener Institute*

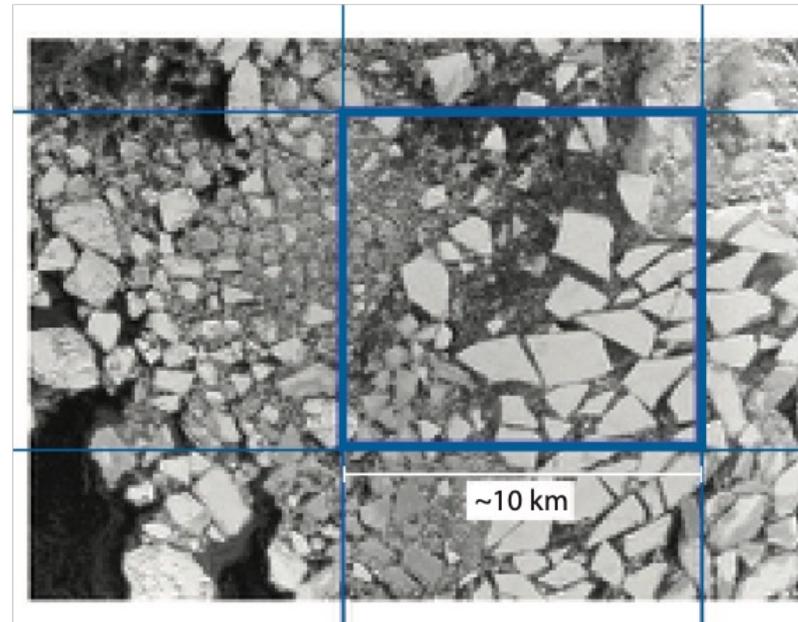
Wave-ice group: David Bailey, Cecilia Bitz, Alice DuVivier Marika Holland,  
Erin Thomas, Bruno Tremblay, Geraint Webb, Diajeng Wulandari Atmojo

# Representing sea ice in climate models

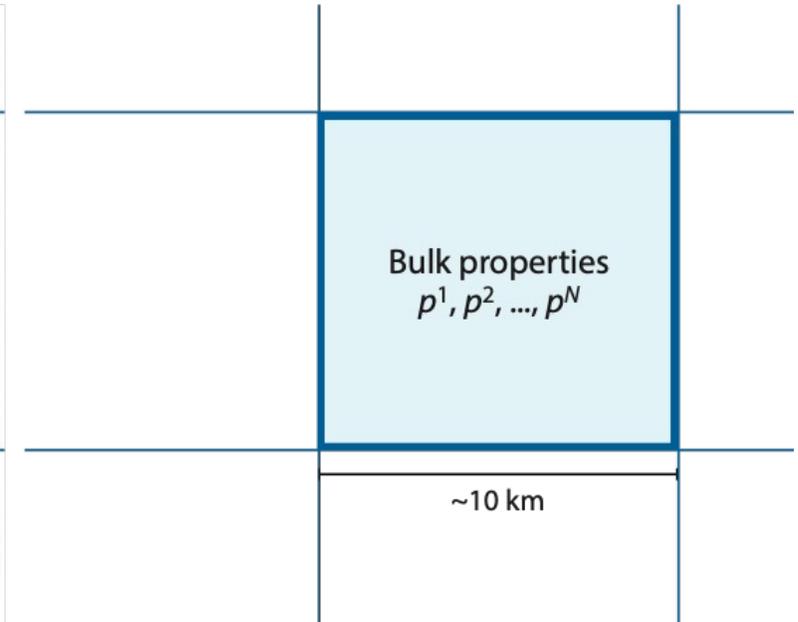
## a Individual components



## b A composite material

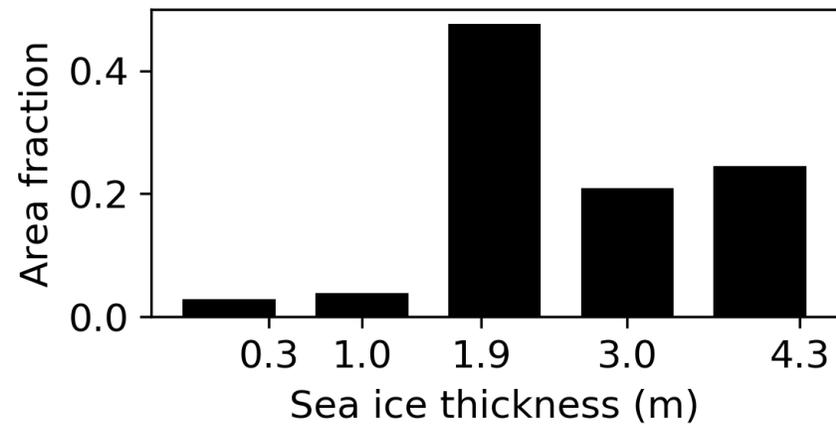


## c A representative continuum



# The sea ice thickness distribution, $g(h)$

- Rothrock & Thorndike (1975)



$$\frac{\partial g}{\partial t} = -\nabla \cdot (g\vec{v}) - \frac{\partial}{\partial h}(fg) + \psi$$

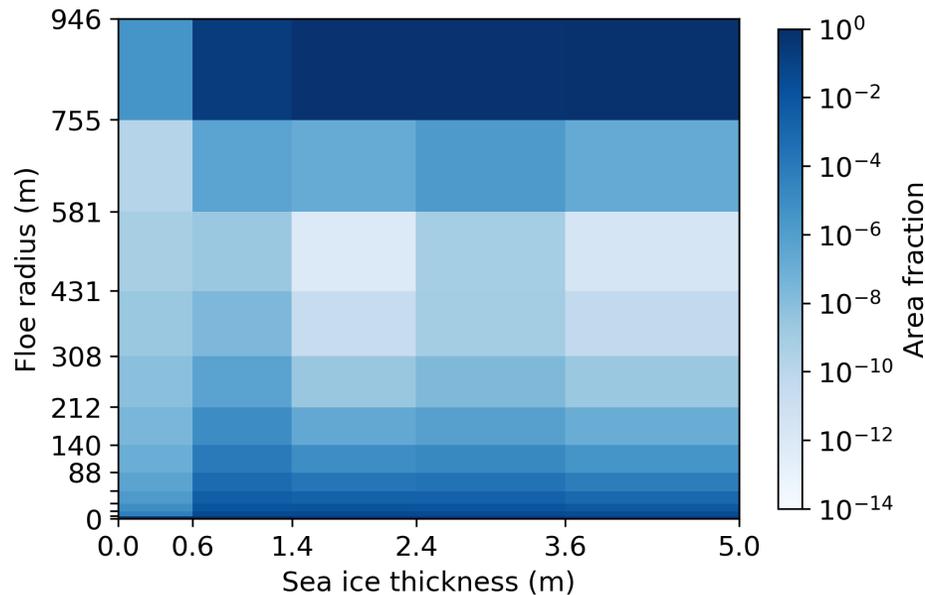
Advection

Ridging/rafting

Thermodynamics

# The sea ice floe size and thickness distribution, $f(r,h)$

- $f(r,h)$  is the fraction of grid surface area covered by ice with thickness between  $h$  and  $h+dh$  and lateral floe size between  $r$  and  $r+dr$  (Horvat & Tziperman, 2015)



$$\frac{\partial f(r, h)}{\partial t} = -\nabla \cdot (f(r, h)\mathbf{v}) + \mathcal{L}_T + \mathcal{L}_M + \mathcal{L}_W$$

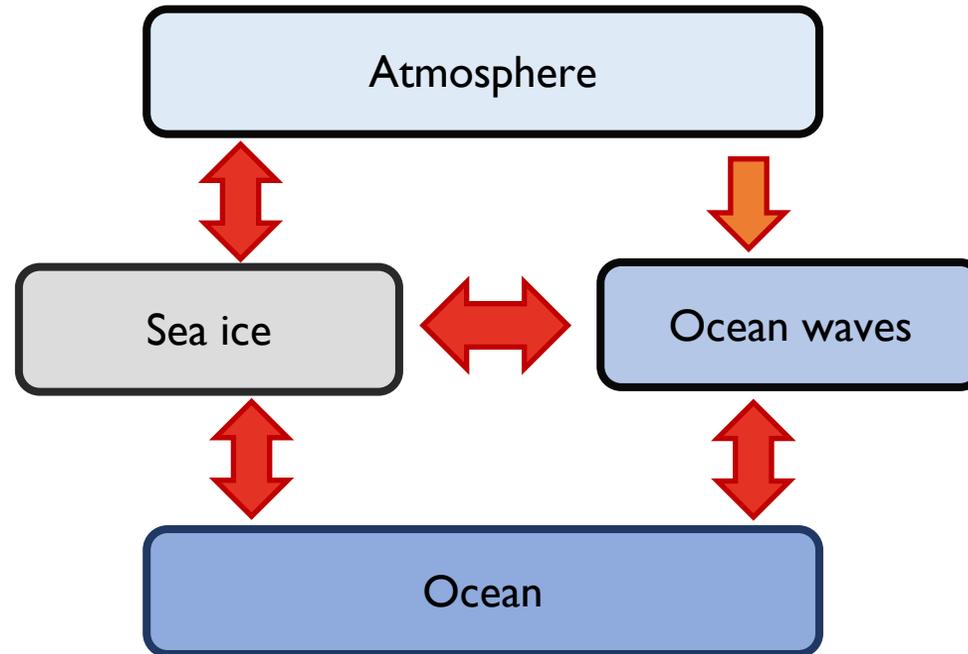
Advection
Thermodynamics
Mechanical interactions
Wave fracture

Implemented by Roach et al. (2018a, 2019) in CICE6/Icepack  
 - no feedback between FSD and dynamics or mechanical interactions  
 + new wave fracture

Variants also by Boutin et al. (2020, 2022), Bateson et al. (2020), and others

# Coupled CESM3 development simulation

- b.e30\_alpha07g.BHISTC\_LTso.ne30\_t232\_wgx3.271



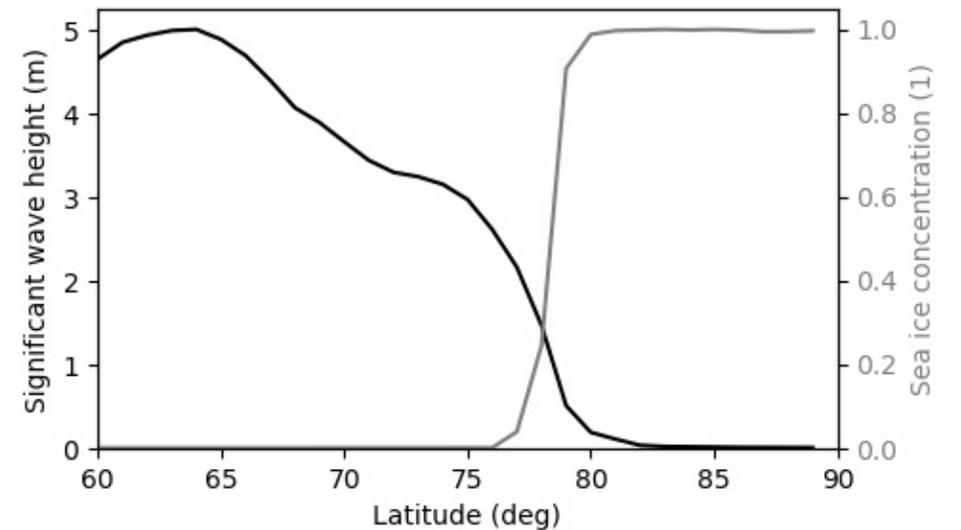
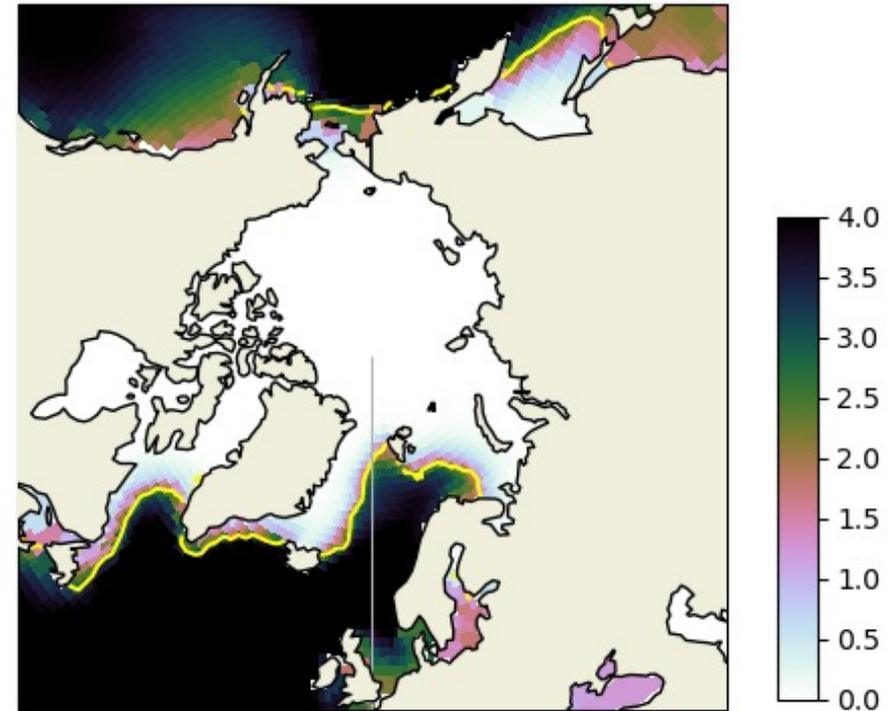
# Wave attenuation in sea ice



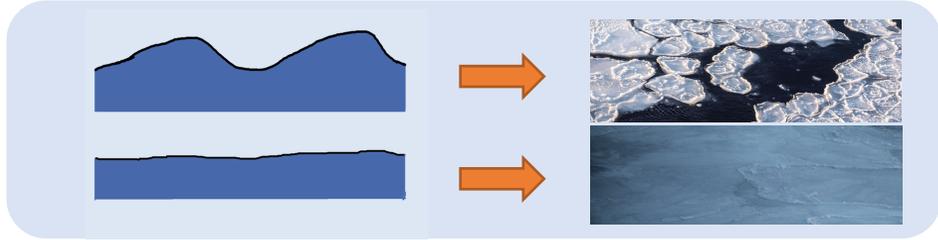
Photo: Lettie Roach, CODA cruise, Beaufort Sea, 2019

- Considerable uncertainty in wave attenuation (e.g. Cooper et al. 2022)
- We use Meylan et al. (2021) floe-size-dependent attenuation

2010-03 Significant wave height (m)



# Wave-dependent new ice growth

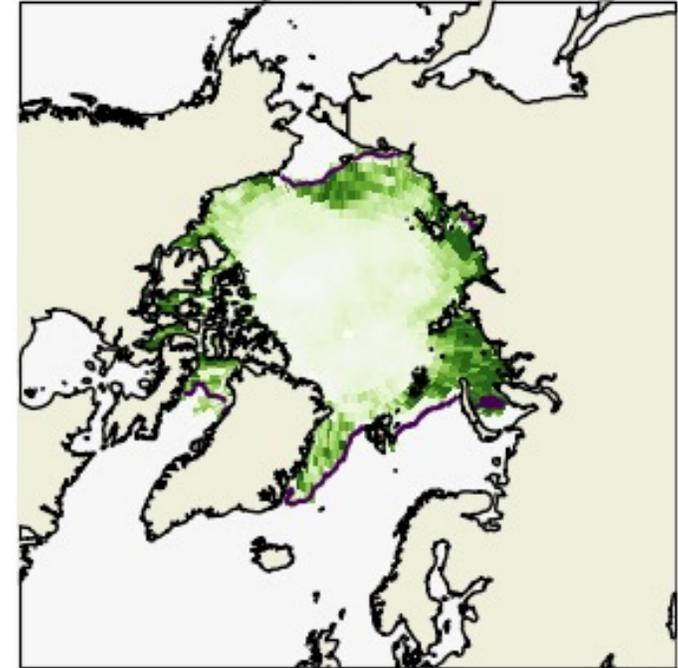


- Tensile failure limit on floe size in a wave field (Shen et al. 2001)

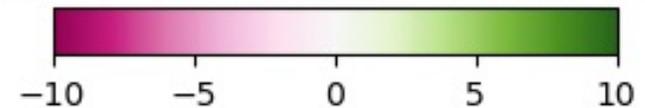
- $$D_{\max} \approx \sqrt{\frac{2C_2\lambda^2}{\pi^3 W_A g \rho_i}}$$

- Calibrated with in situ observations (Roach et al. 2018b)

2013-10

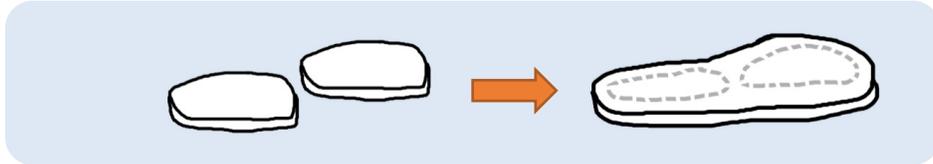


Perimeter tendency per unit area ( $\text{km}^{-1} \text{day}^{-1}$ )



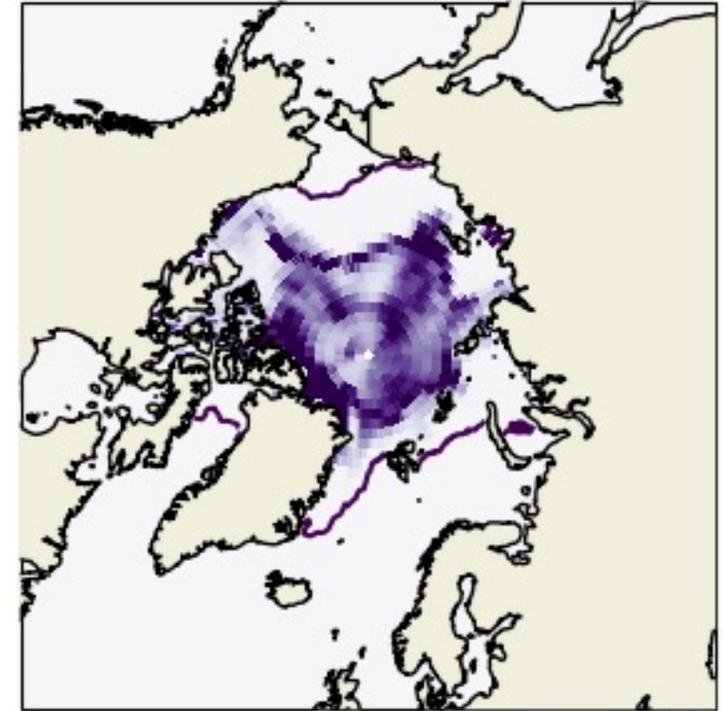
- Very effective in increasing perimeter

# Floe welding

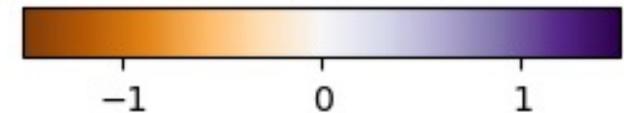


- In freezing conditions, floes freeze together according to geometric probability of overlap - coagulation equation (Roach et al. 2018a)
- Calibrated with in situ observations (Roach et al. 2018b)

2013-10

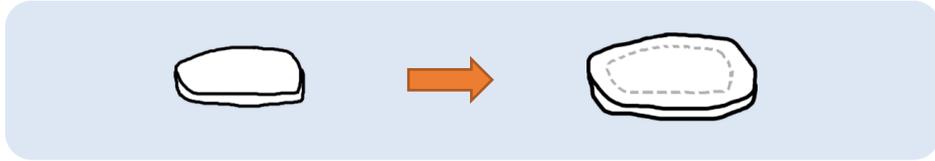


Representative radius tendency ( $\text{m day}^{-1}$ )



- Effective in increasing representative radius

# Lateral growth



$$\mathcal{L}_T(r, h) = -\nabla_{(r, h)} \cdot (f(r, h) \mathbf{G}) + \frac{2}{r} f(r, h) G_r$$

- Lateral growth rate is the volume of new ice growth in the 'lead region' per time

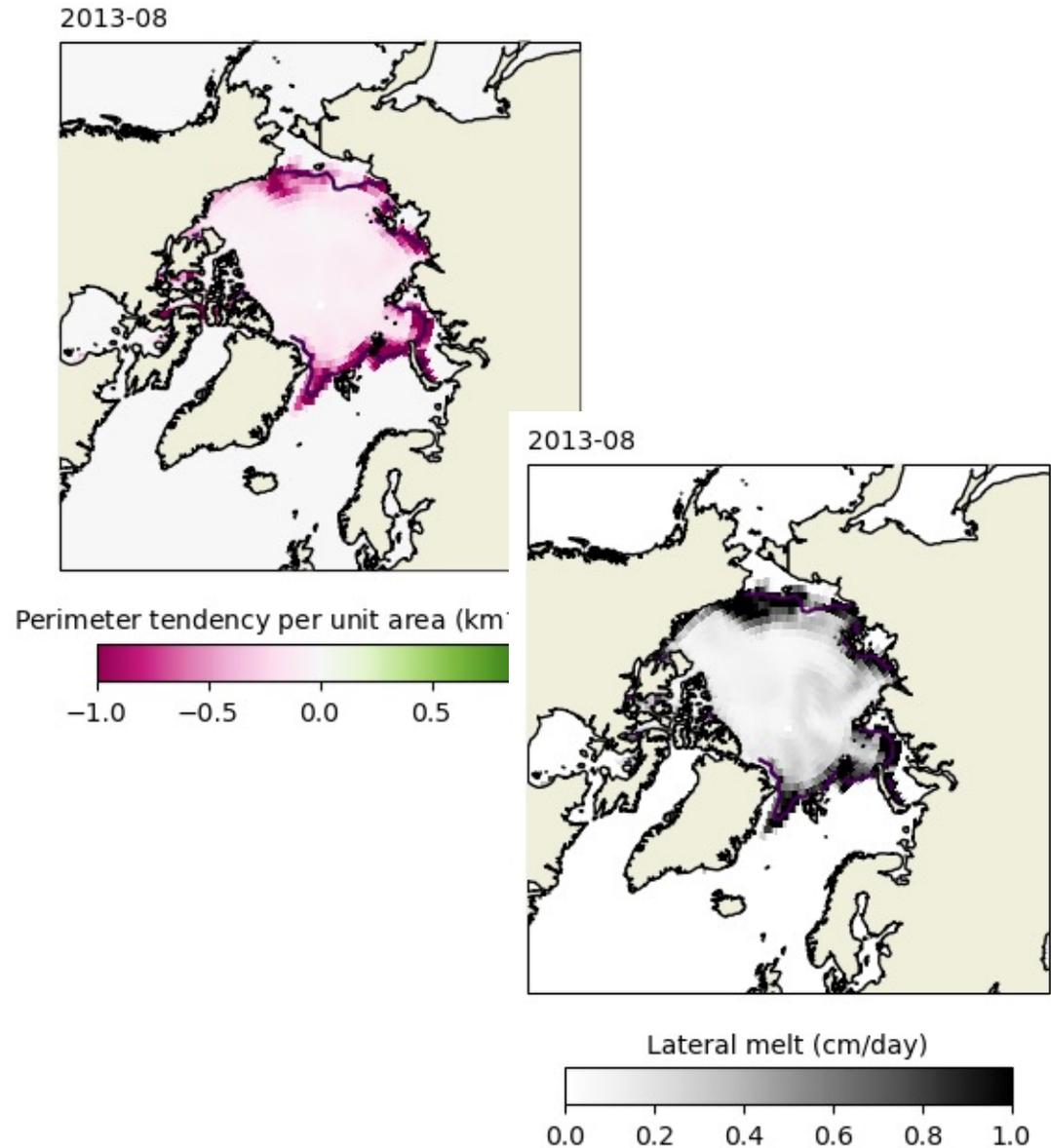
Minimal impact to  
perimeter,  
representative radius,  
concentration

# Floe-size-dependent lateral melt

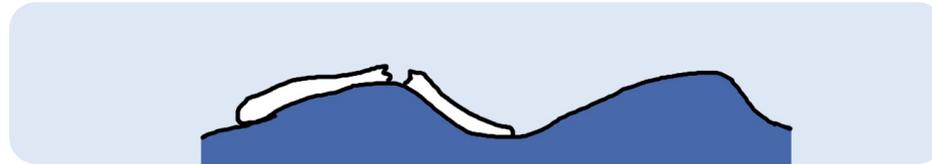


$$\mathcal{L}_T(r, h) = -\nabla_{(r, h)} \cdot (f(r, h) \mathbf{G}) + \frac{2}{r} f(r, h) G_r$$

- Lateral melt rate as standard model
- Impacts ice concentration, thickness distribution



# Fracture of sea ice by ocean surface waves



Sea ice is completely rigid

OR

Sea ice is completely flexible

Dumont et al. (2011)

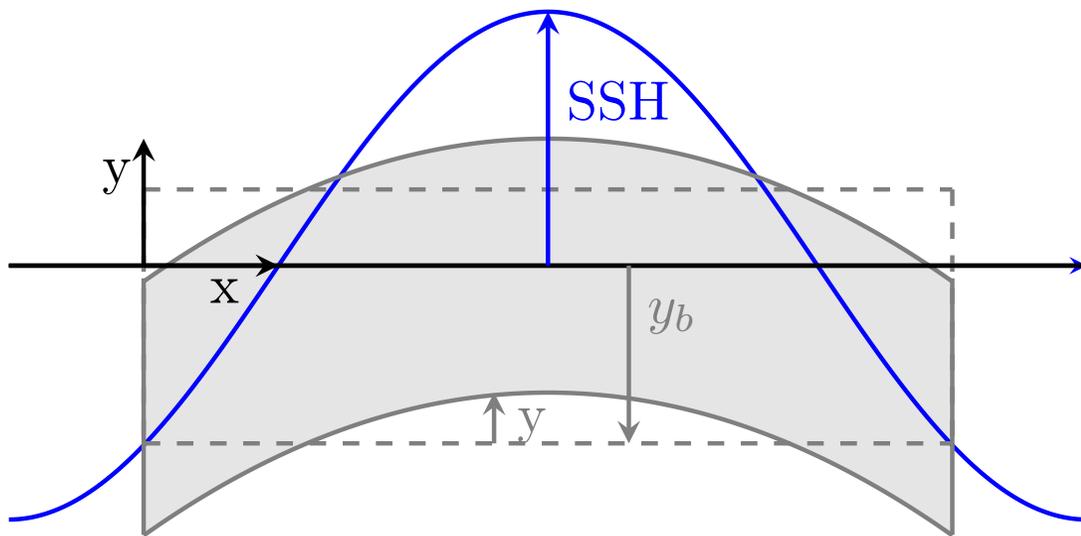
Williams et al. (2013)  
Horvat & Tziperman (2015)  
Roach et al. (2018a, 2019)

# Wave fracture: new approach from thin elastic plate theory

SSH: Sea Surface Height

$y$ : Beam deflection

$y_b$ : Ice draft



Assume hydrostatic equilibrium

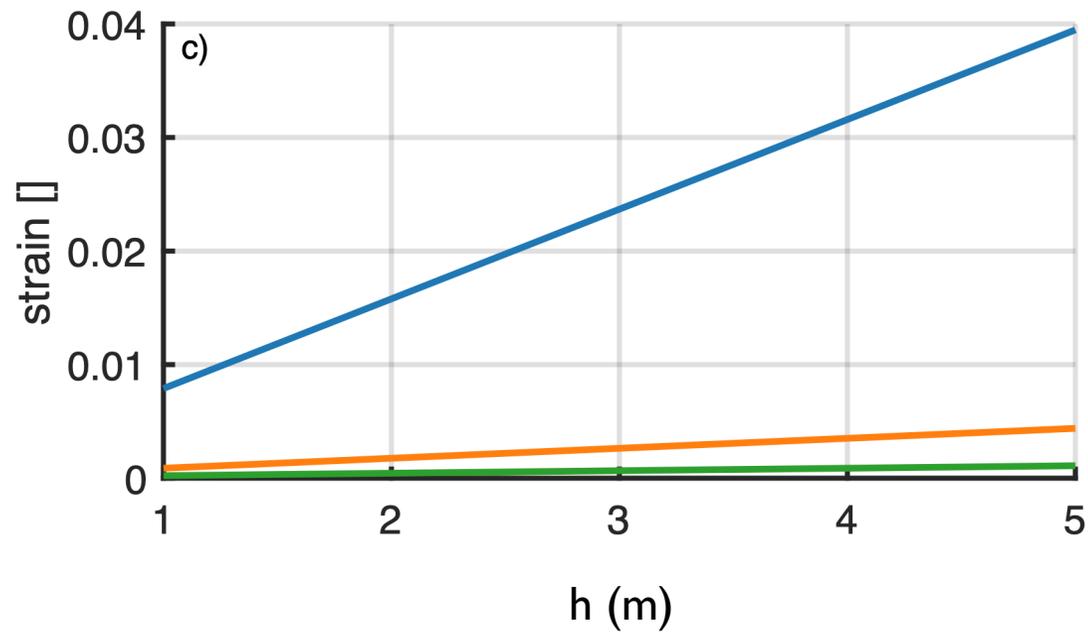
$$\frac{d^4 y}{dx^4} + \frac{1}{\Lambda^4} y = \frac{1}{\Lambda^4} \sum_{i=1}^N A_i \cos(2\pi x / \lambda_i - \phi_i)$$

- Fourth-order inhomogeneous ODE that can be solved analytically
- $\Lambda$  is a characteristic length scale
- Strain  $\epsilon = \frac{h}{2} y''(x)$

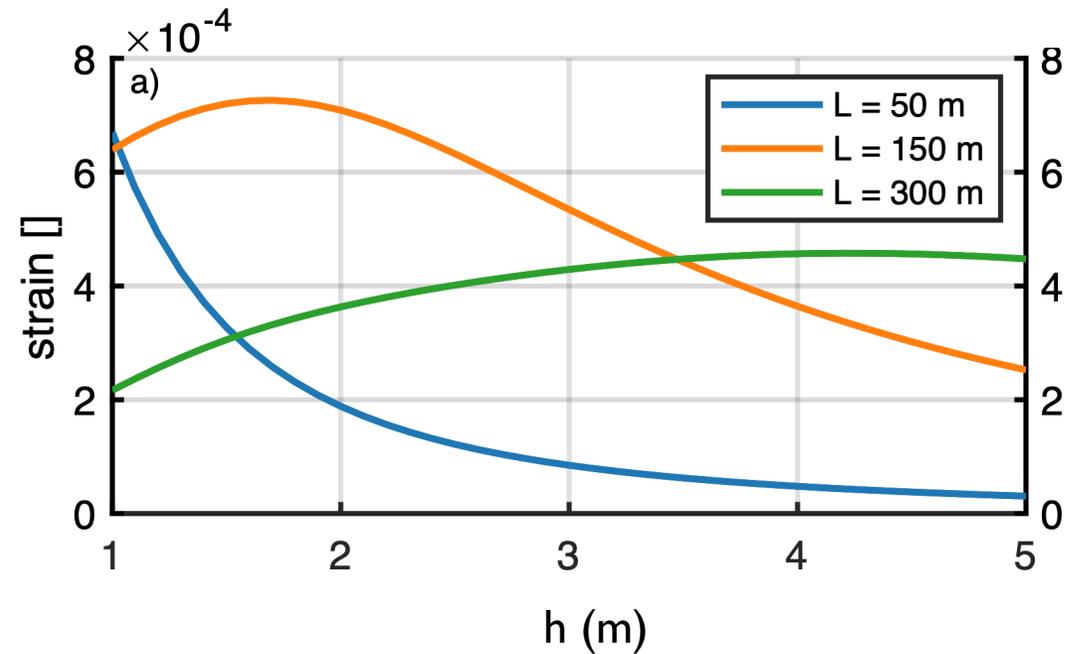
# Strain as a function of ice thickness

- Observations suggest a critical strain around  $3 \times 10^{-5}$  (Langhorne et al. 1998)
- Force floe with Bretschneider spectrum, 1 m amplitude

Fully-flexible

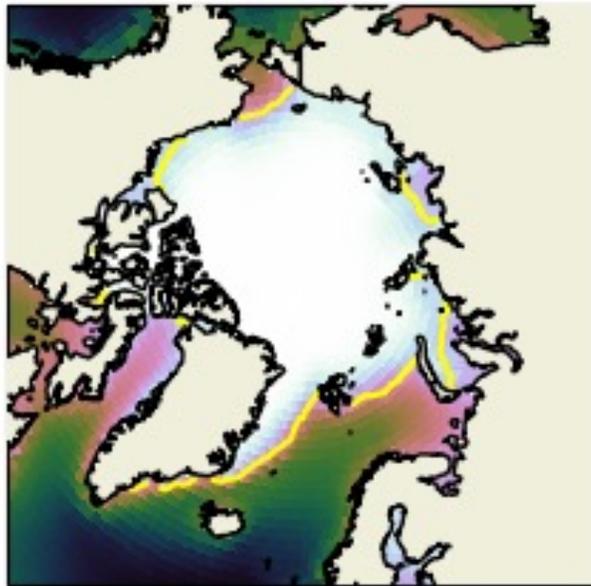


Thin elastic plate

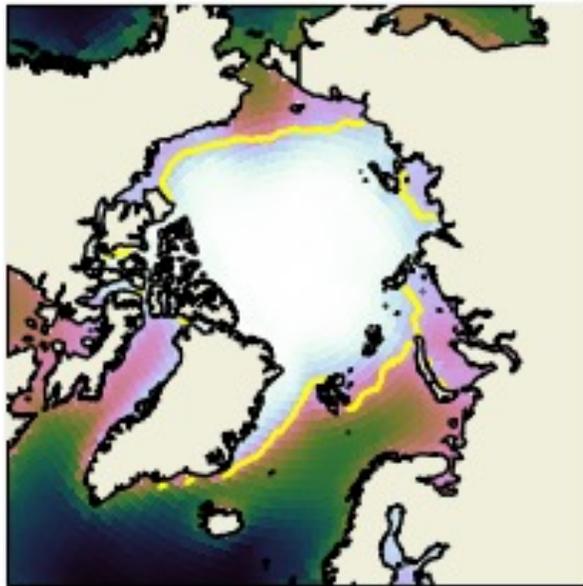


# Increasing wave heights in the 'new' Arctic

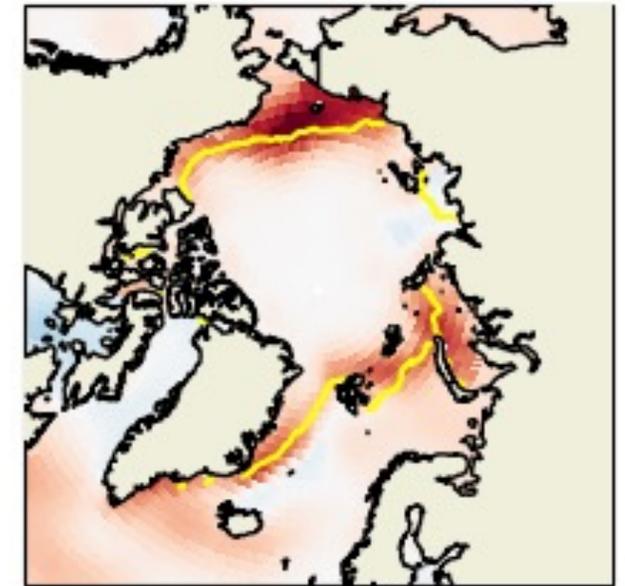
1984-1993 September



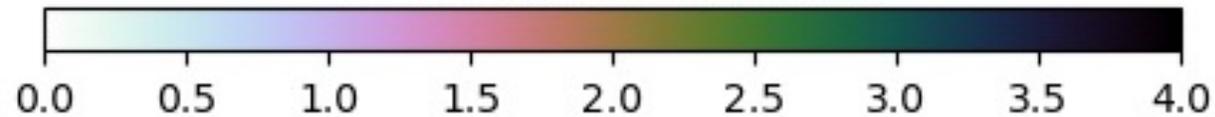
2004-2013 September



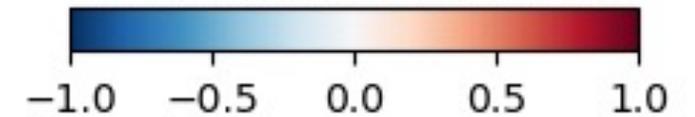
Difference, September



Significant wave height (m)



Significant wave height (m)



# Open questions

- How do waves and related sea ice processes change in the emerging Arctic and Antarctic?
- How significant are sea ice—wave feedbacks in the coupled model?
- How can we improve process representation?
- How can we compare with limited observations?

# Simulation needs

- Some baseline to compare against – no FSD, no wave-ice interactions?
- Constrained simulation to compare with observations – data-atmosphere?
- Wave output / output for CMIP7?

# Questions?

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<https://lettie-roach.github.io/>

Photo: Ben Adkison  
PIPERS cruise, Ross Sea, 2017

