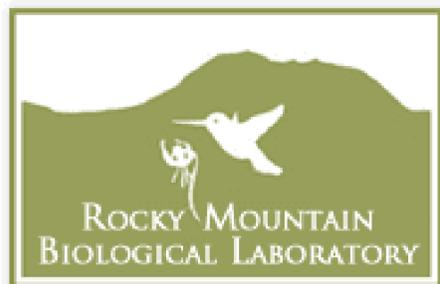


Physics - Informed Neural Networks (PINNs) to improve biological reality of machine -learning -based models of the soil CO₂ flux in subalpine forests

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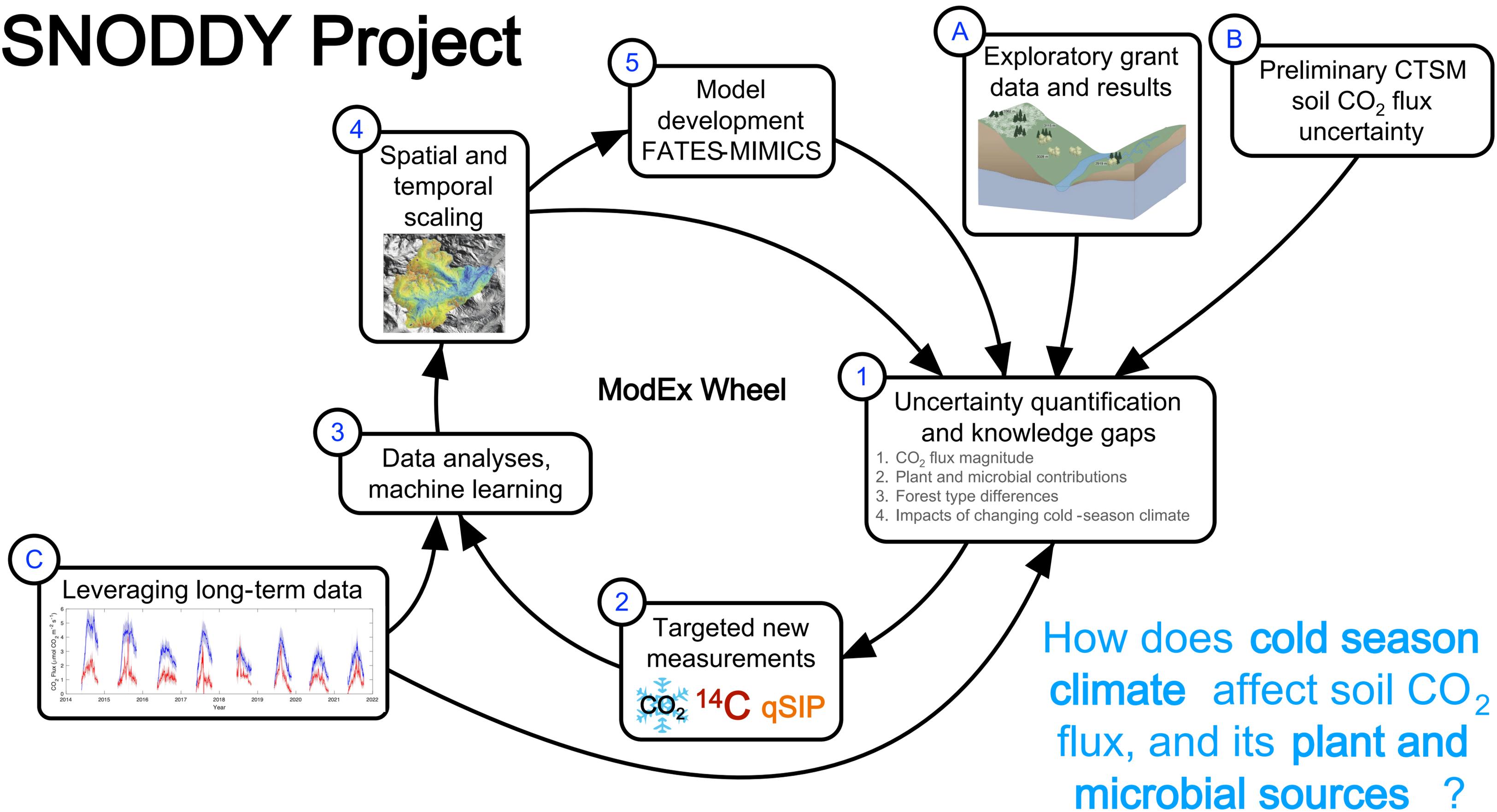
ESS
Environmental
System Science



U.S. DEPARTMENT OF
ENERGY

Office of
Science

SNODDY Project



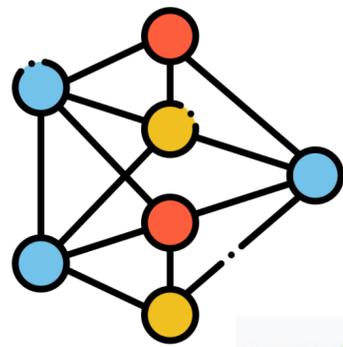
SNODDY Project

DOE ESS Grant

- PI - Mariah Carbone
- Co-PIs: Andrew Richardson, Ben Lucas, Will Wieder, Adrianna Foster
- Collaborators: Austin Simonpietri, Bruce Hungate, Egbert Schwartz, Gena Blumencweijg, Kenneth Williams (LBNL)

qSIP

¹⁴C



CLM

PhenoCam

Will Wieder
NCAR

Bruce Hungate
NAU

Gena Blumencweijg
PhD Student NAU

Austin Simonpietri
PhD Student NAU

Me



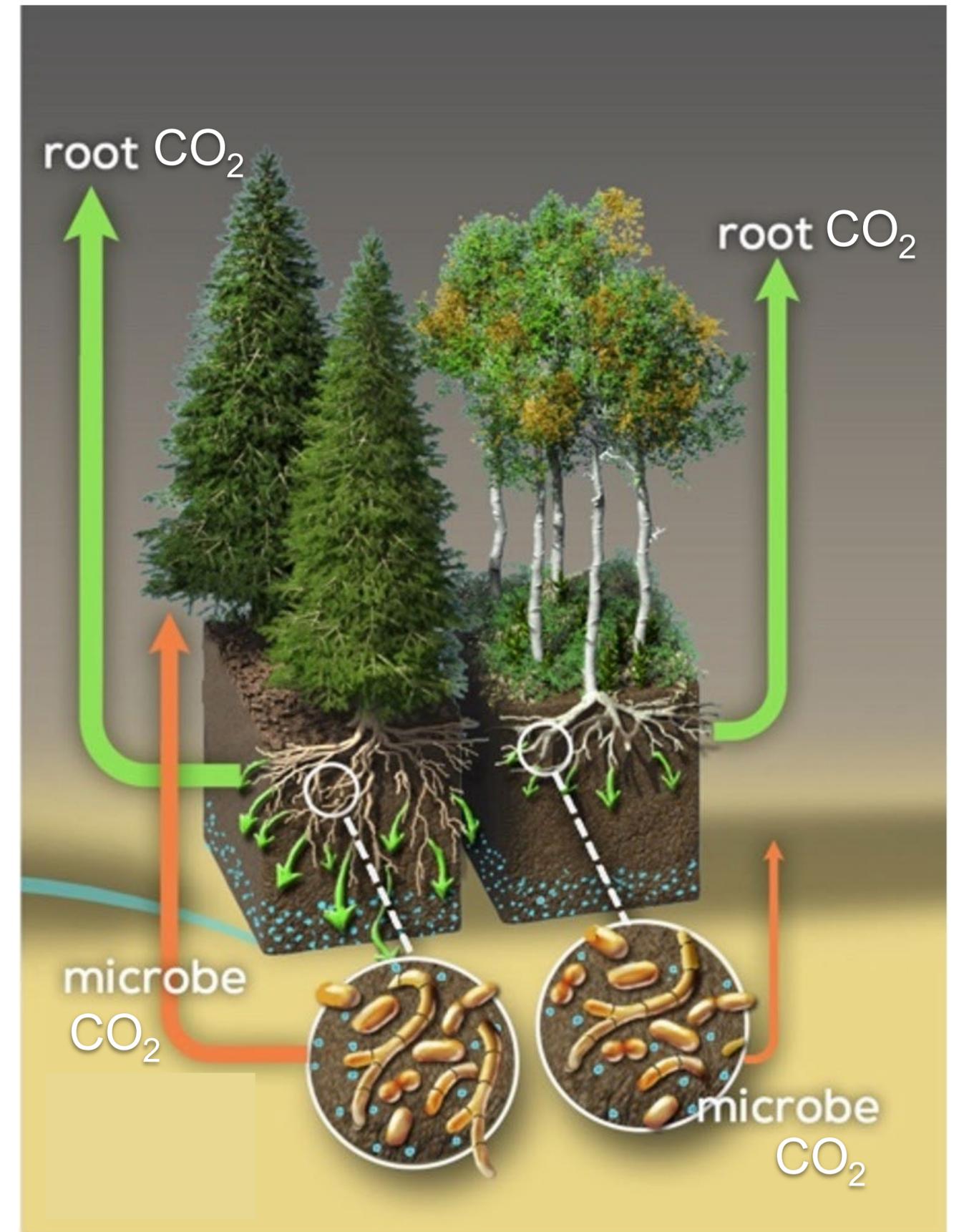
Mariah Carbone
NAU

Adrianna Foster
NCAR

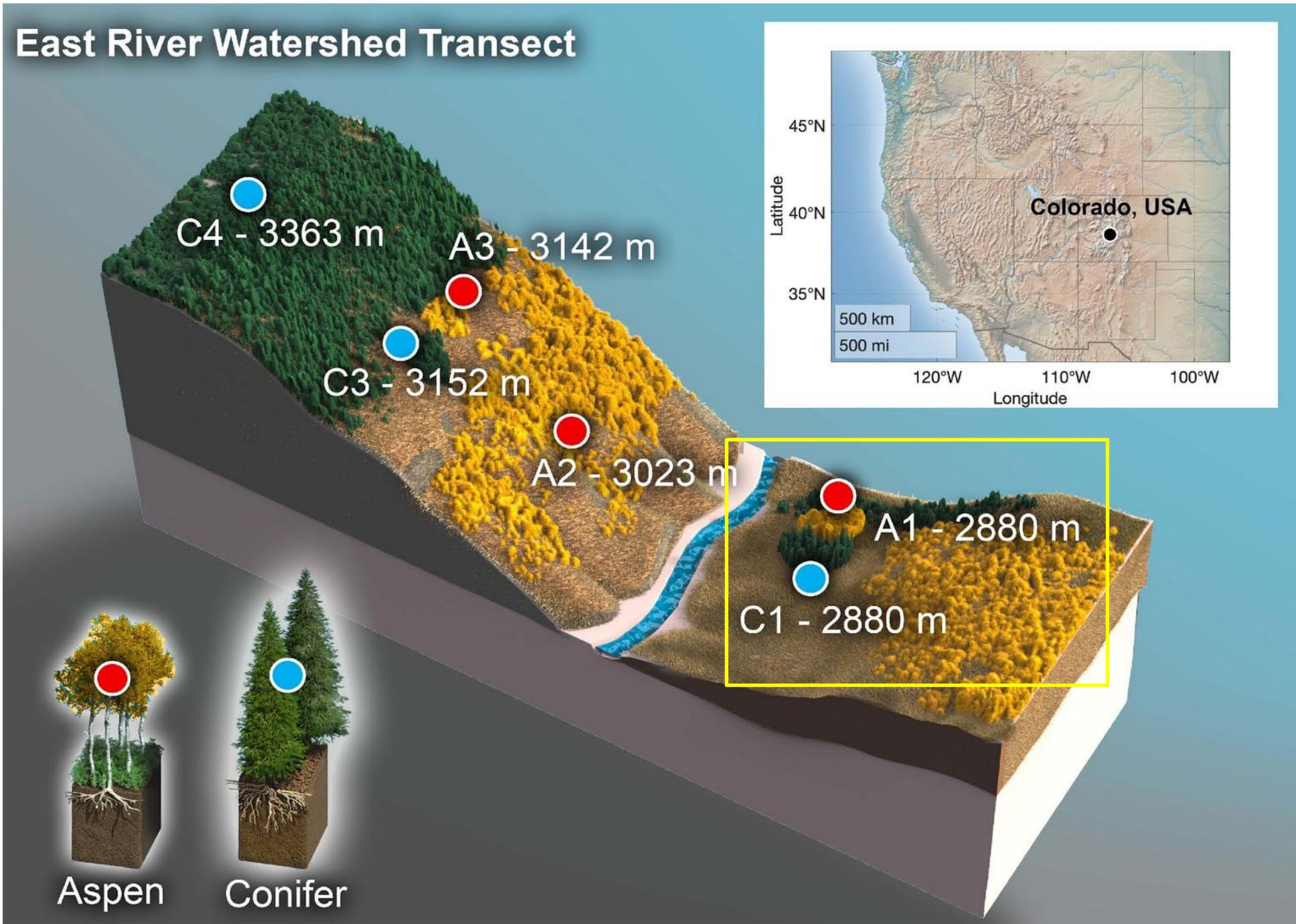
Not Pictured
Andrew Richardson
Ben Lucas, NAU

Why the soil CO₂ flux?

- 2nd largest flux
- Two biological sources:
- Microbial decomposition
- Root respiration
- Difficult to tease apart



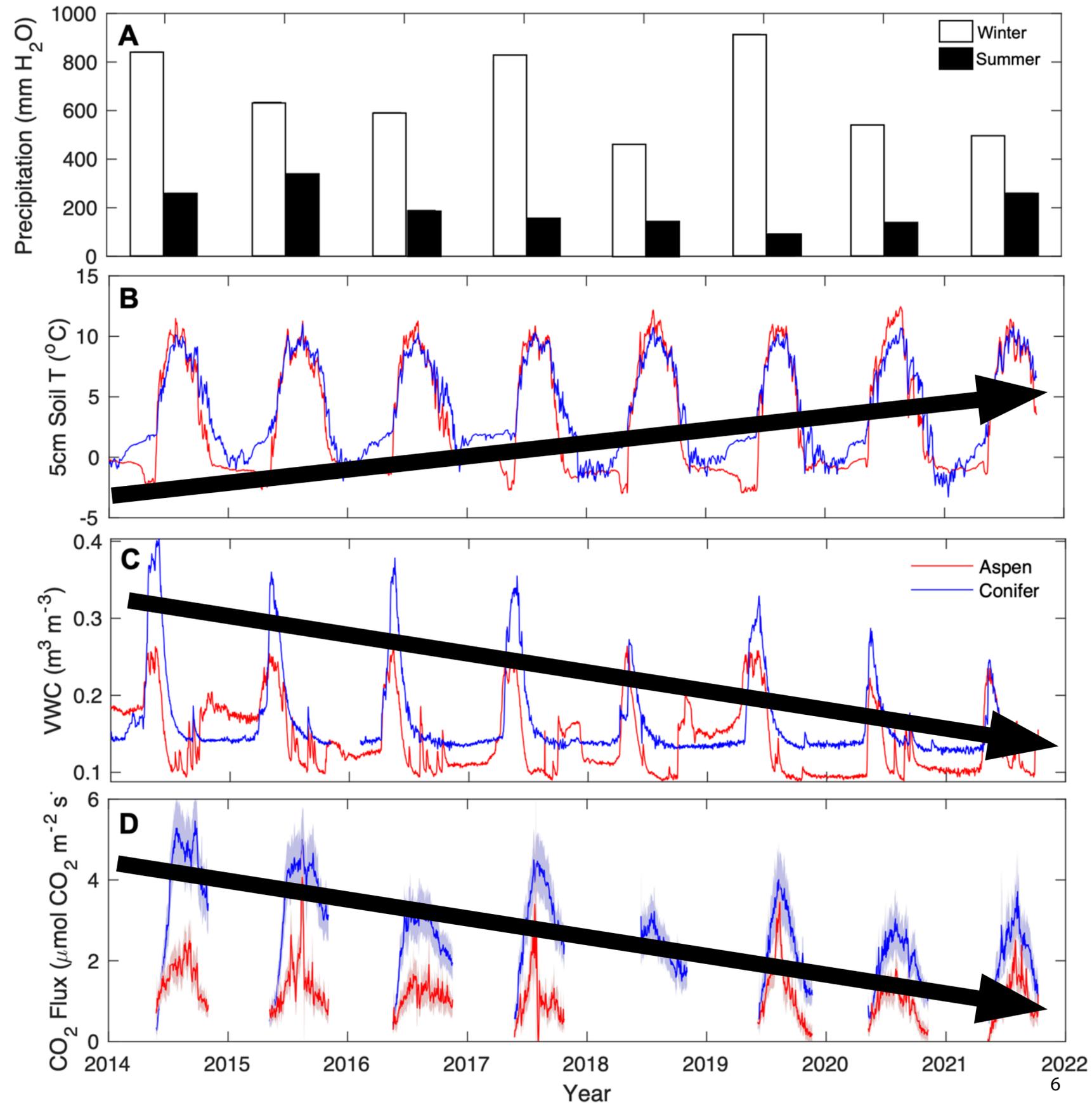
Field sites



- Snodgrass mountain, in the East River watershed, CO
- 2880 m elevation

Dominant forest types:

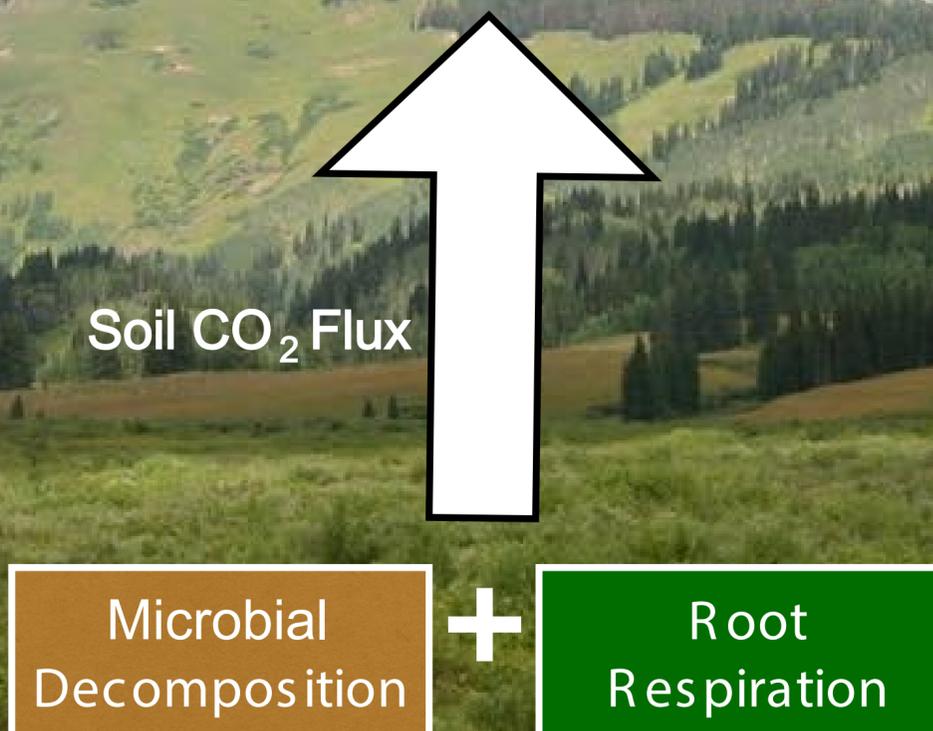
- Aspen and mixed conifer spruce/fir stands



- Variable snow/rain inputs
- Increasing soil and air temperature
- Decreasing soil moisture
- Decreasing soil CO₂ flux
- Surface soils responsible for declining trend

Motivation

Toward more accurate and ecologically realistic modeling of soil CO_2 flux and its microbial and root contributions



Soil CO_2 Flux

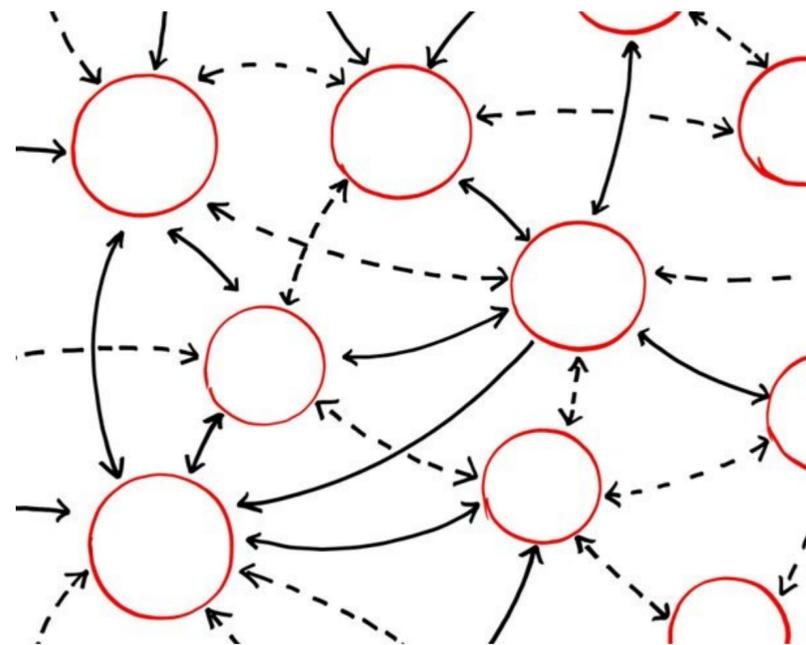
Microbial
Decomposition

+

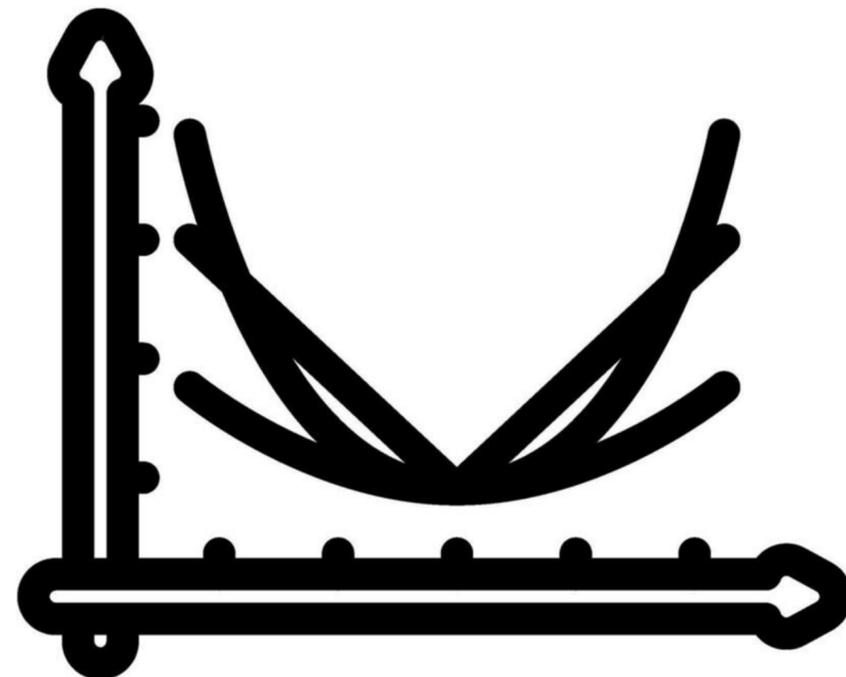
Root
Respiration

Machine learning goal

- Goal of classic NN: minimize loss
- Loss function: Mean squared error (observed – predicted)
- Limitation: overfit data, leading to biological implausibility.
- Temperature, moisture, carbon supply

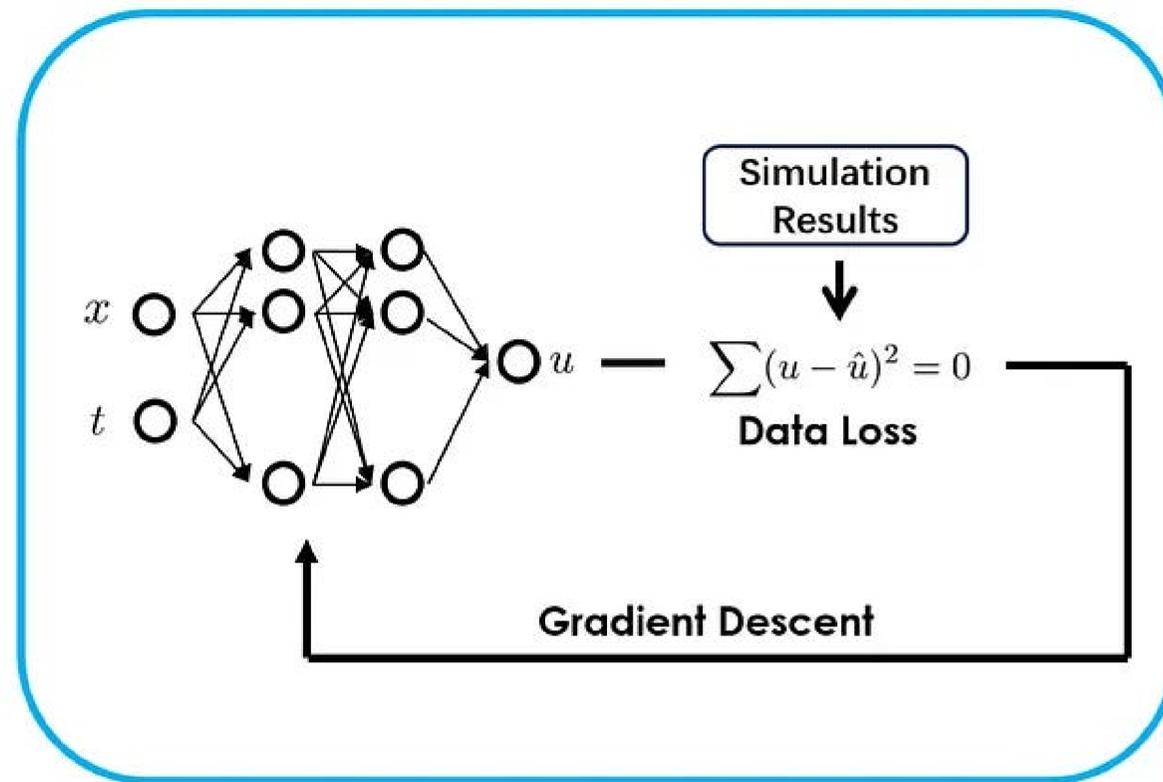


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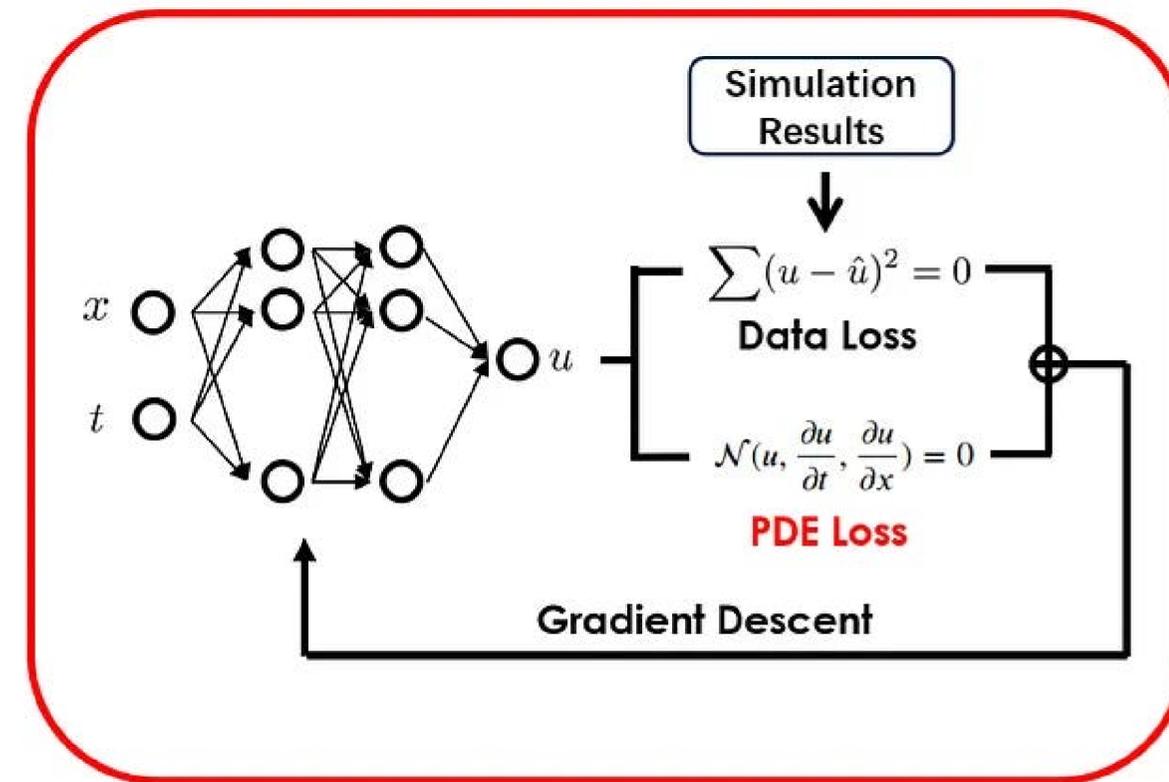


Physics -Informed Neural Network (PINNs)

Modify the loss



Traditional NN



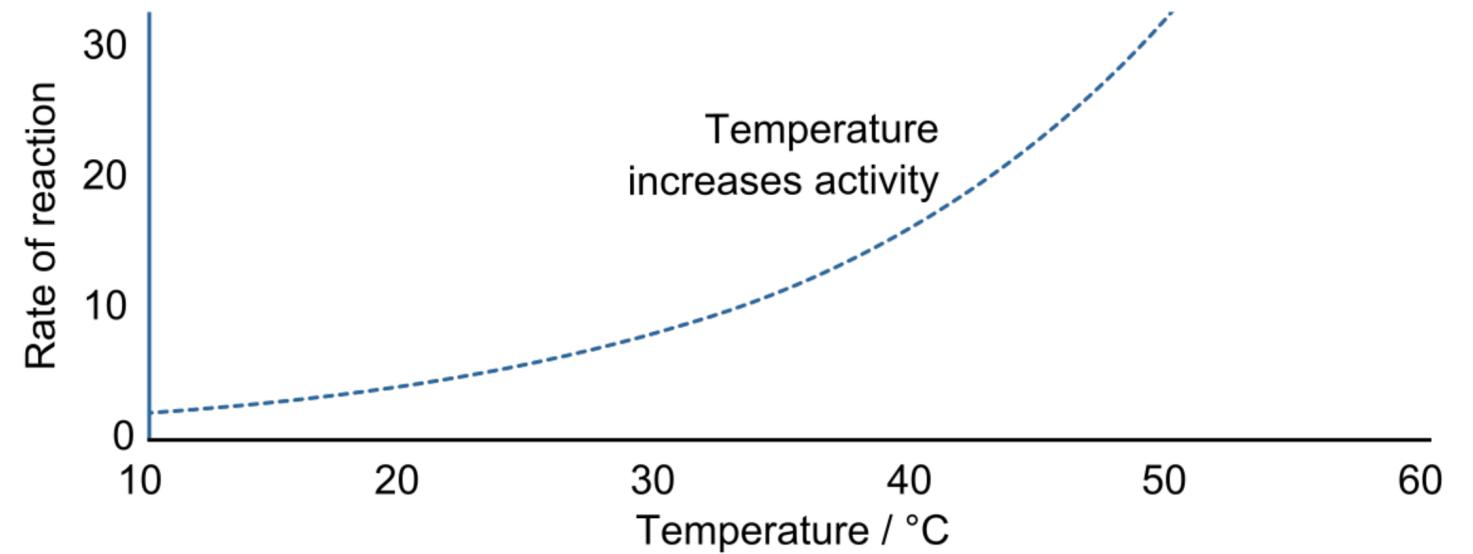
Physics-informed NN

- Idea: Modify data loss with process penalty

Process penalty: Q10

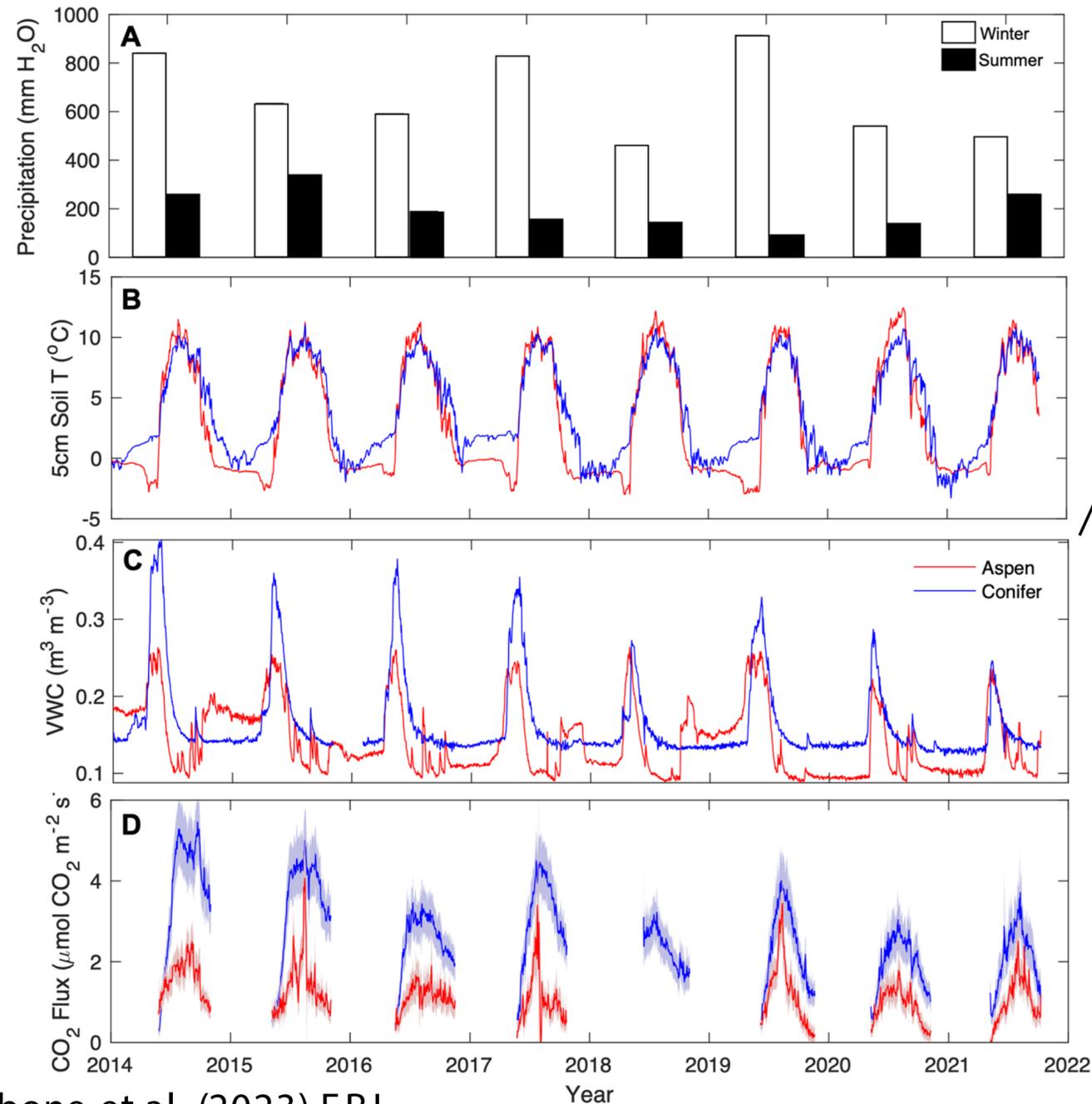
A few notes

- Q10 quantifies how biological reaction rates change with a 10 °C increase in temperature;
- Q10 of 2 is often used in process-based models to represent the temperature response of a plant or ecosystem;



Methods

Classic NN vs Q10 constrained NN



Load data

Daily soil CO₂ efflux (R), T_{soil}, VWC, snow/precipitation, stand

Neutral Network architecture

- MLP with tanh activation & dropout
- Target variable: $\log(R)$
- Adam optimizer

Loss function

Classic NN (data fit):

$$L = \text{MSE}(\exp(\log R_{\text{pred}}), R_{\text{obs}})$$

Q10-constrained PINN

$$L = \text{MSE} + \lambda \cdot L_{\text{Q10}}$$

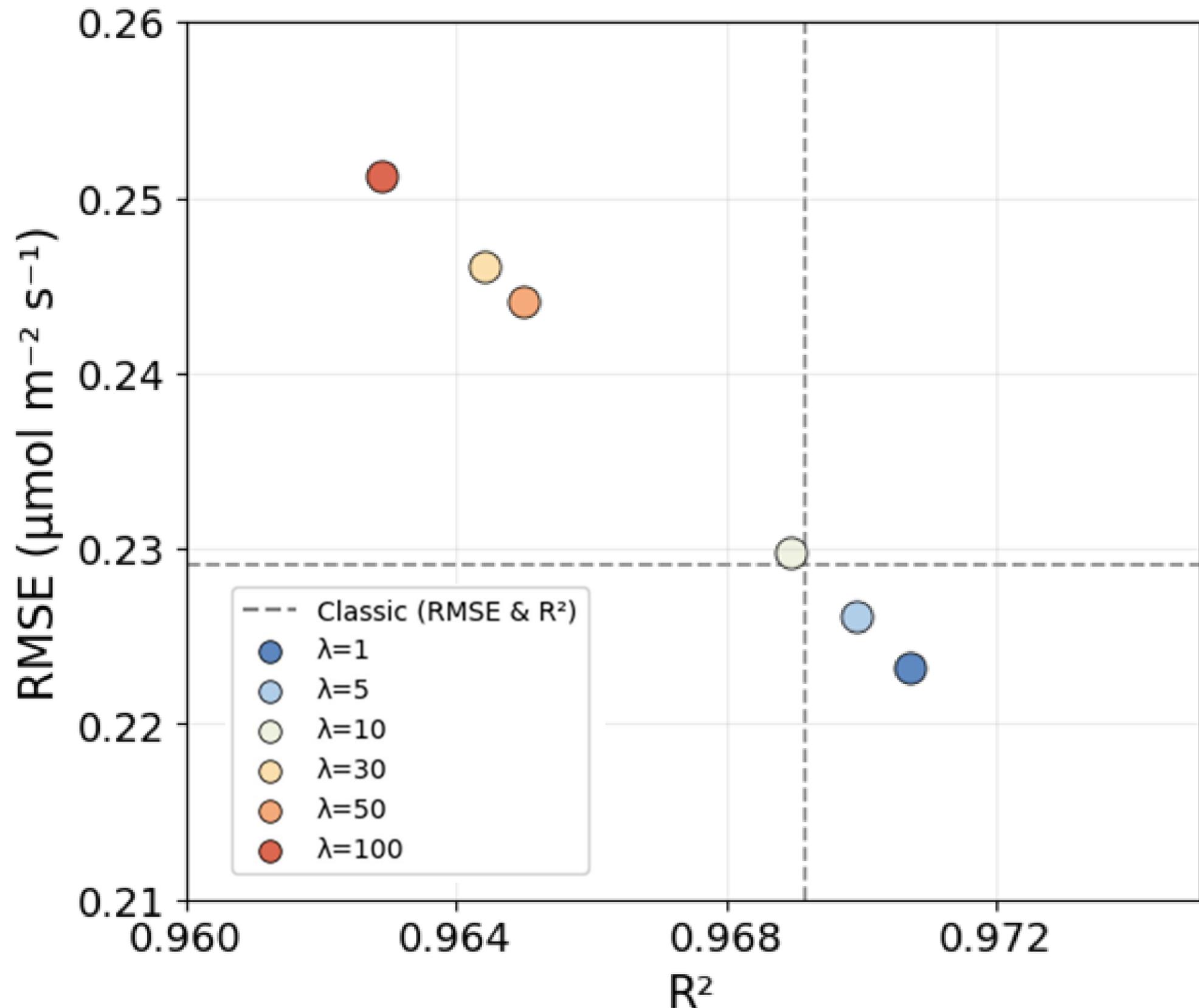
Test for different values λ

Compute local Q10

Results

Predictive skill

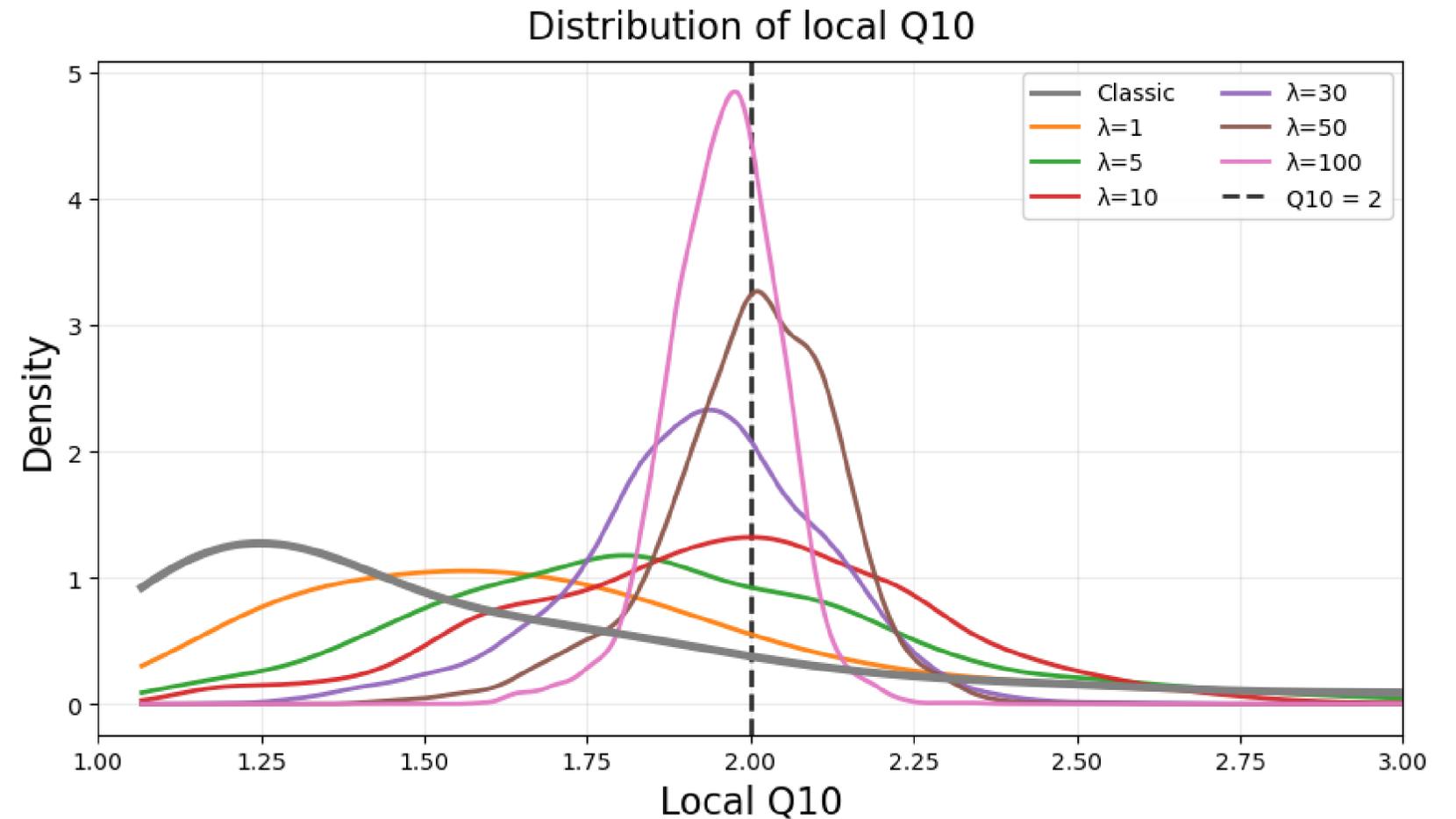
- Grey dash lines: classic NN
- Each point: a Q10 constrained PINN with different λ
- Small λ values (1,5): Q10 constrained PINN outperforms classic NN;
- Q10 constraints are keeping the model from over fitting data;



Results

Q10 distribution

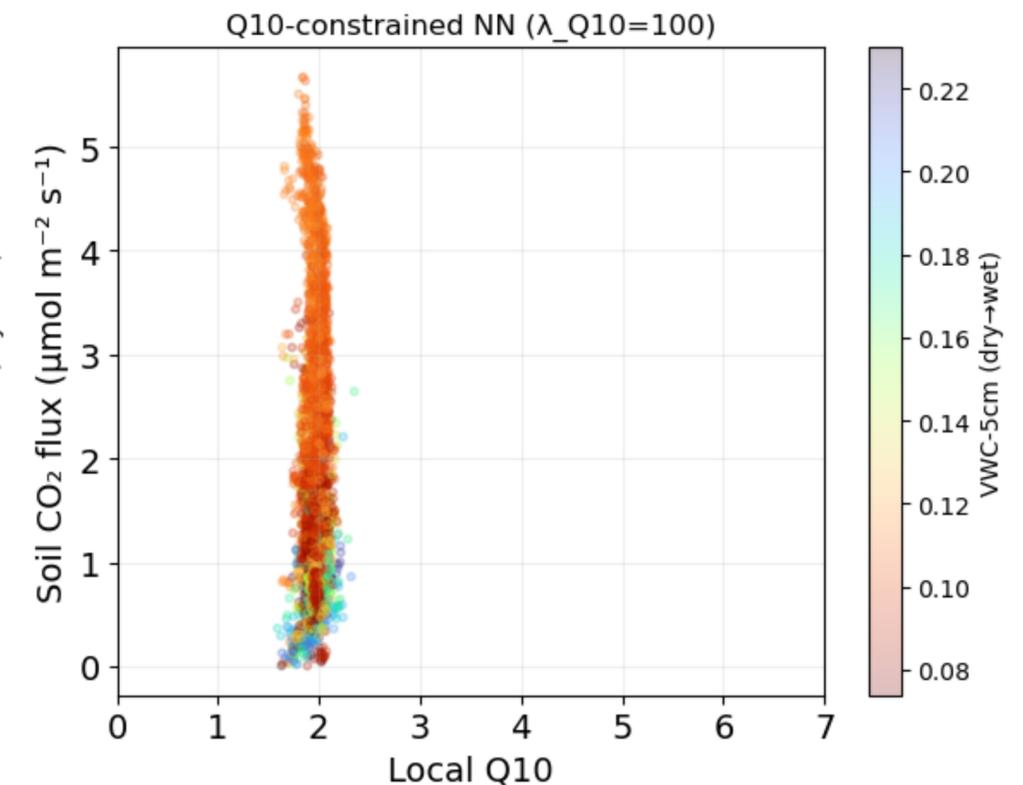
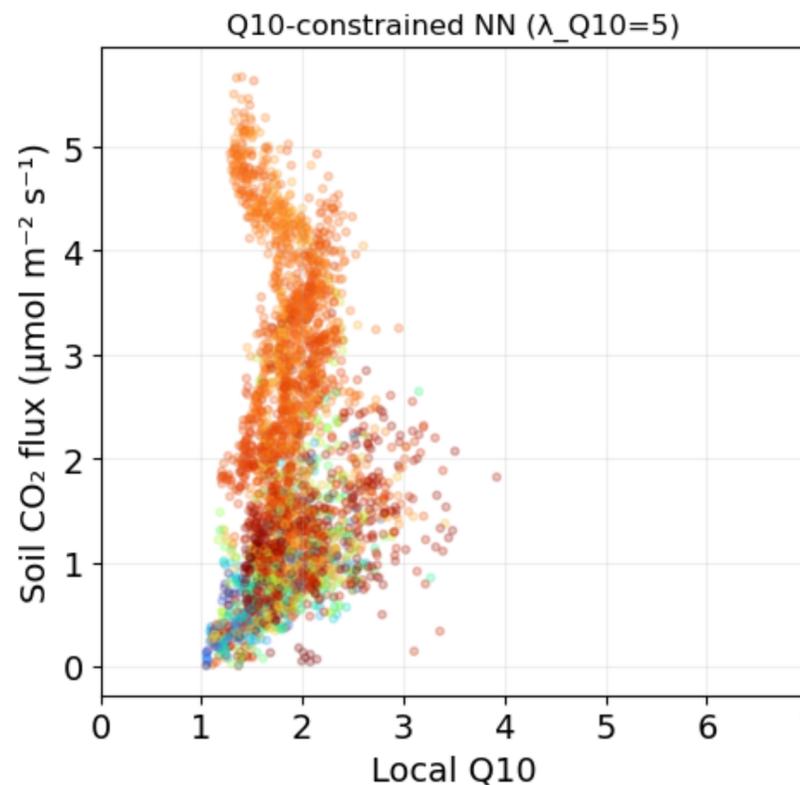
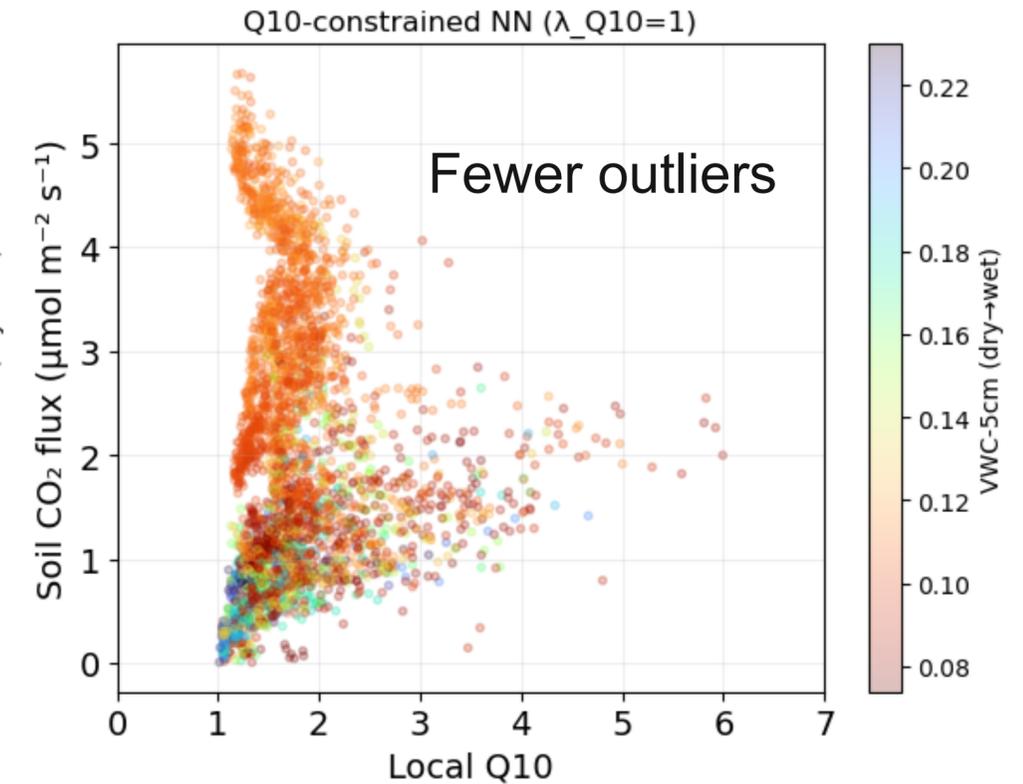
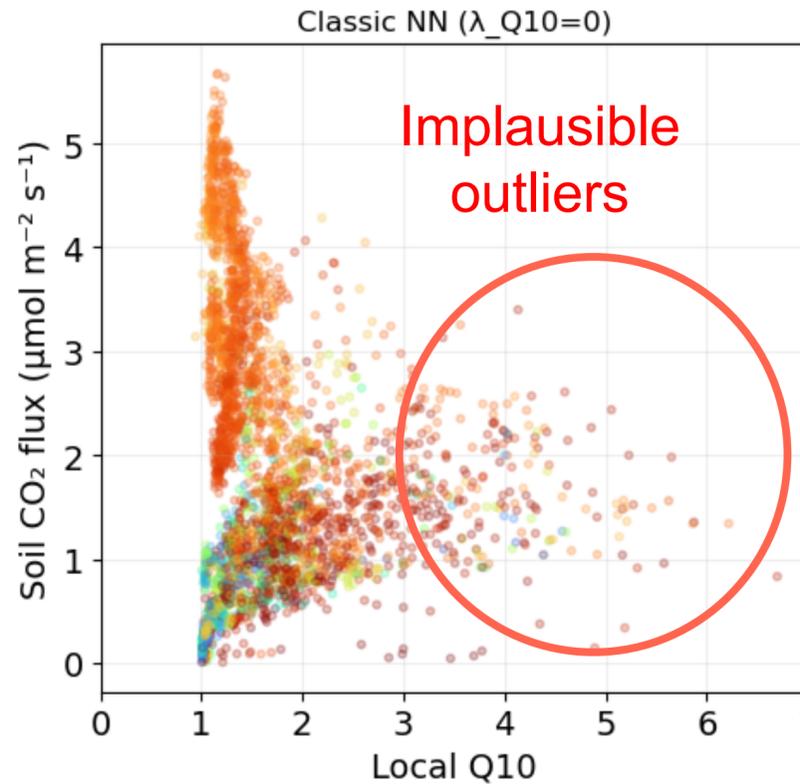
- Grey line: classic NN;
- Classic NN: highly scattered Q10 with high variability;
- PINN narrows Q10 estimates to a biologically plausible band.
- As λ increases, the Q_{10} values become narrower and are pulled closer to the target value of 2.



Results

Q10 vs Flux

- Classic NN generates implausible outliers;
- Q10 constrained PINN stabilized the behavior;
- $\lambda = 5$, good trade-off between stability and allowing natural variability;



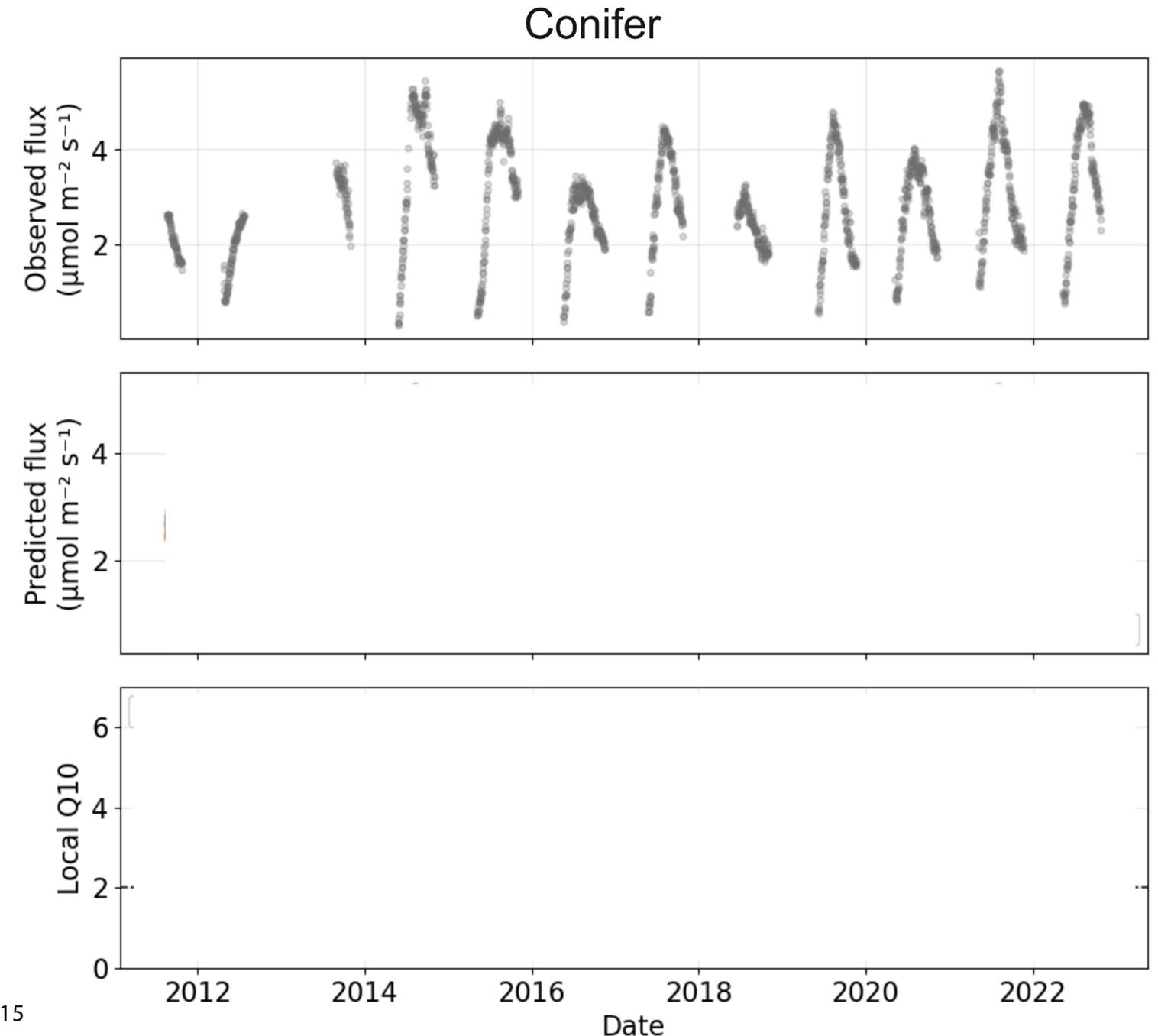
Results

Time series

Q10 constrained PINN ($\lambda = 5$)

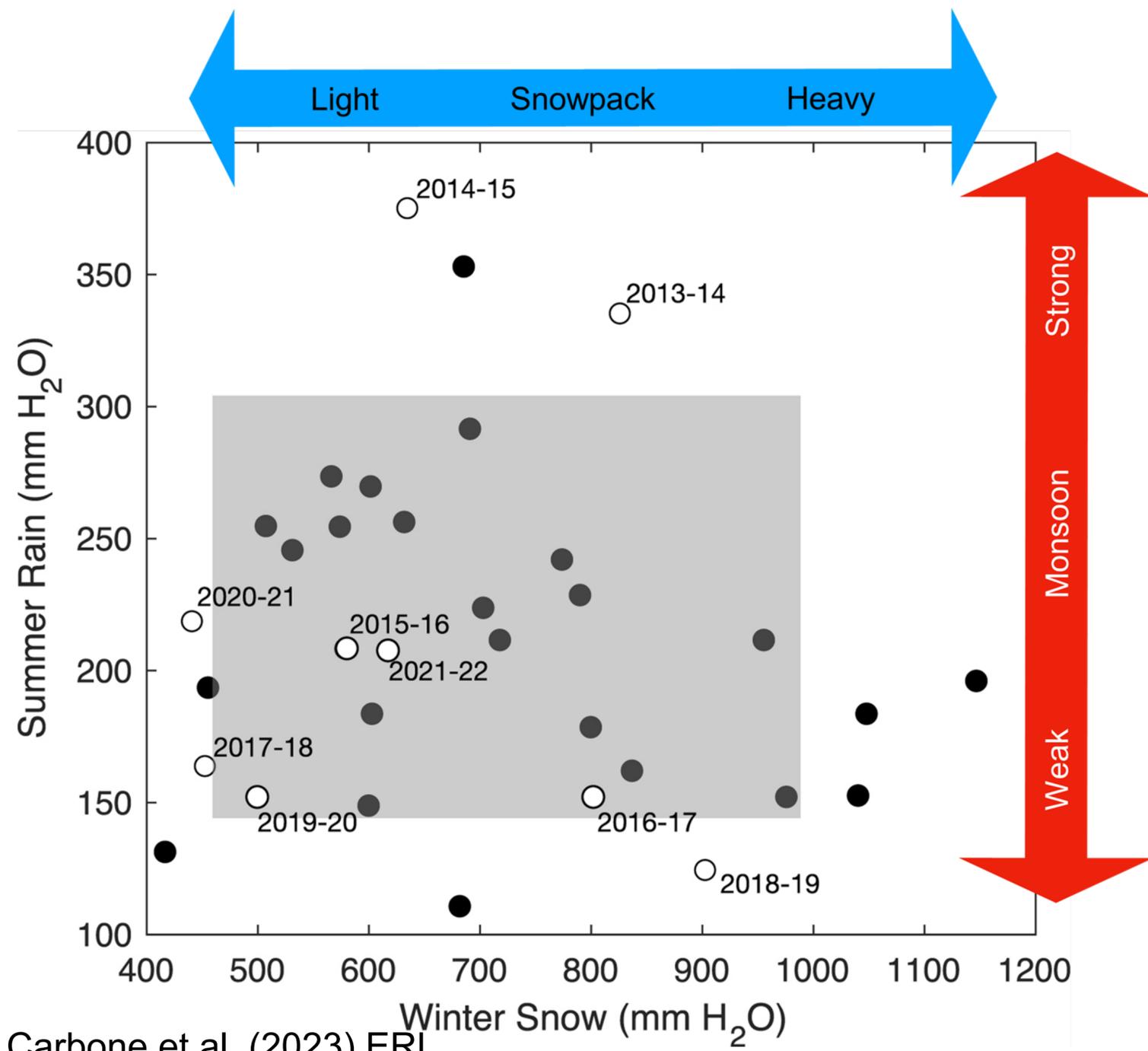
- has slightly higher RMSE and R^2 than the classic NN;
- reproduces the seasonal patterns almost identically to the classic NN;
- smooths out some abrupt jumps that are visible in measurements, but that may NOT be realistic;
- has more realistic seasonal variations in Q10

— Classic NN
— Q10 constrained NN

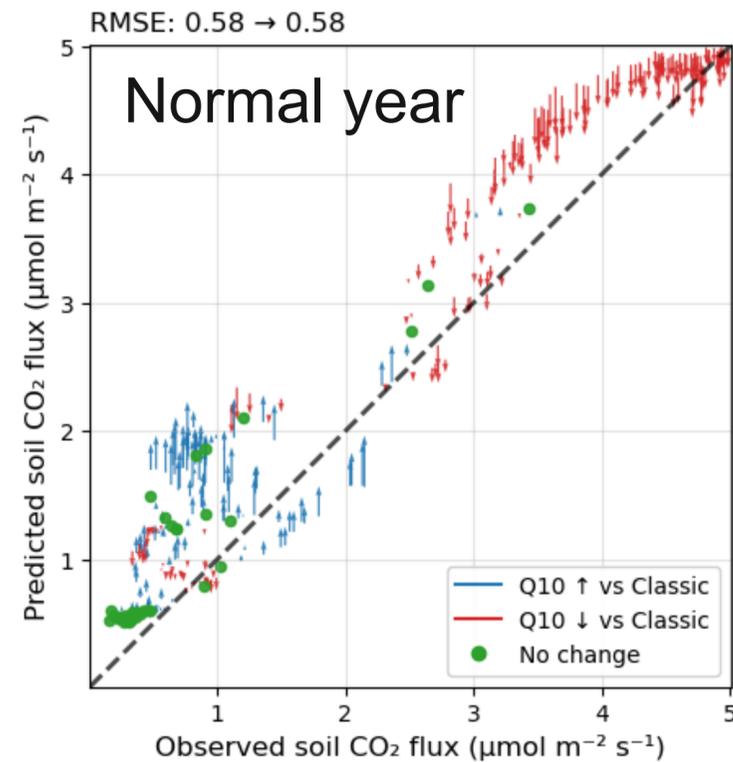


Results

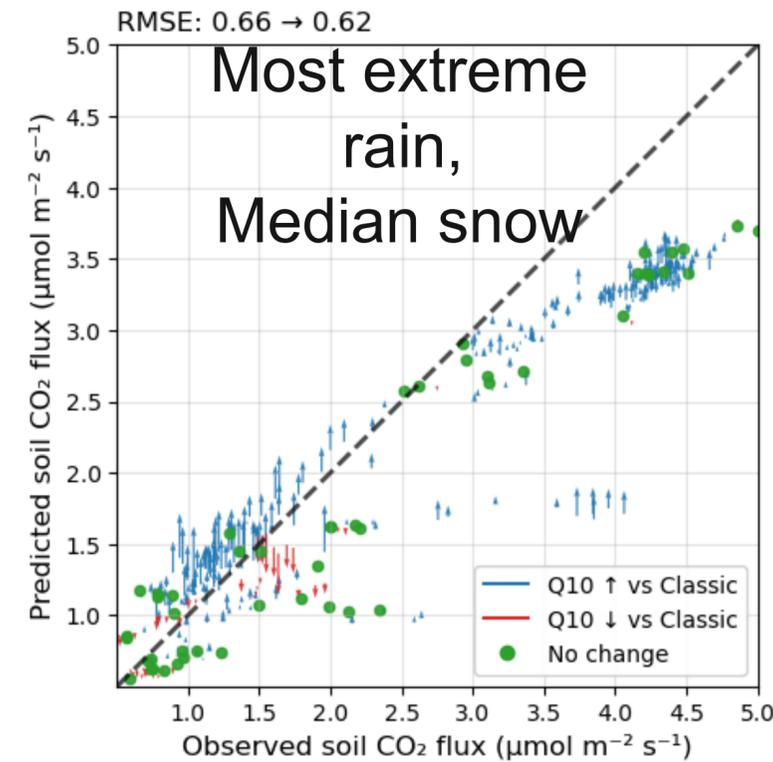
Leave one year out



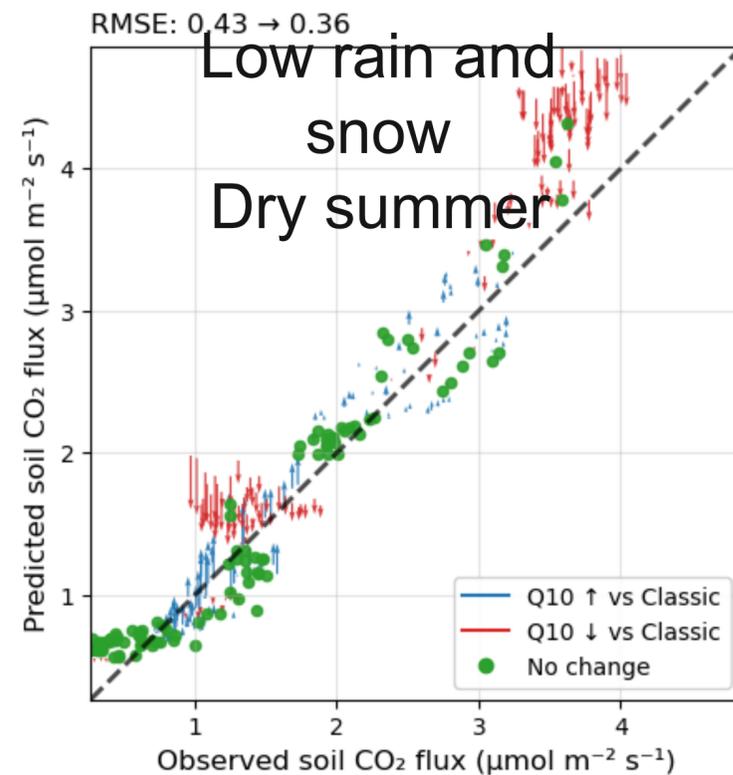
(Year 2022) Classic → Q10 ($\lambda=5$)



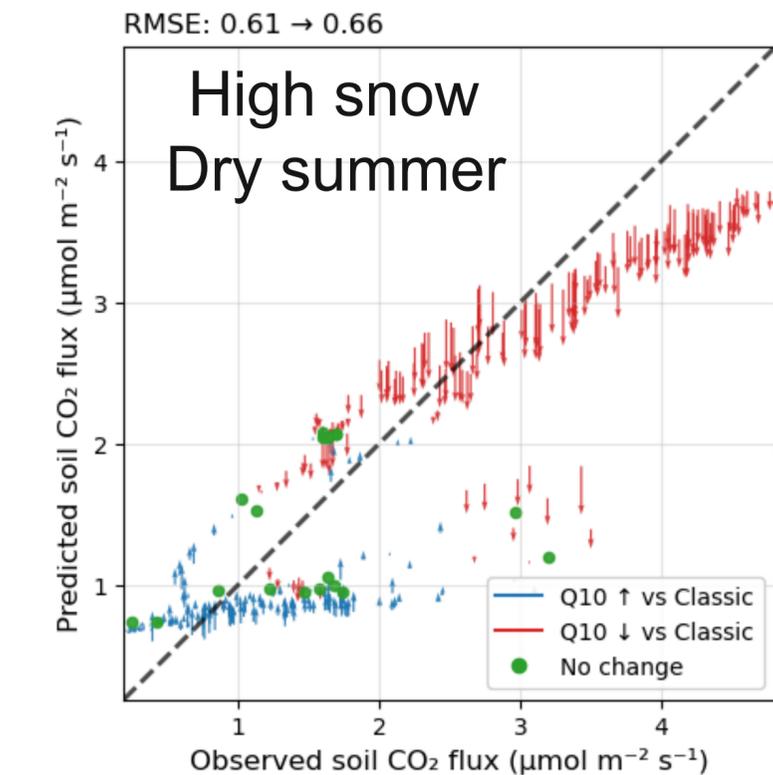
(Year 2015) Classic → Q10 ($\lambda=5$)



(Year 2020) Classic → Q10 ($\lambda=5$)



(Year 2019) Classic → Q10 ($\lambda=5$)

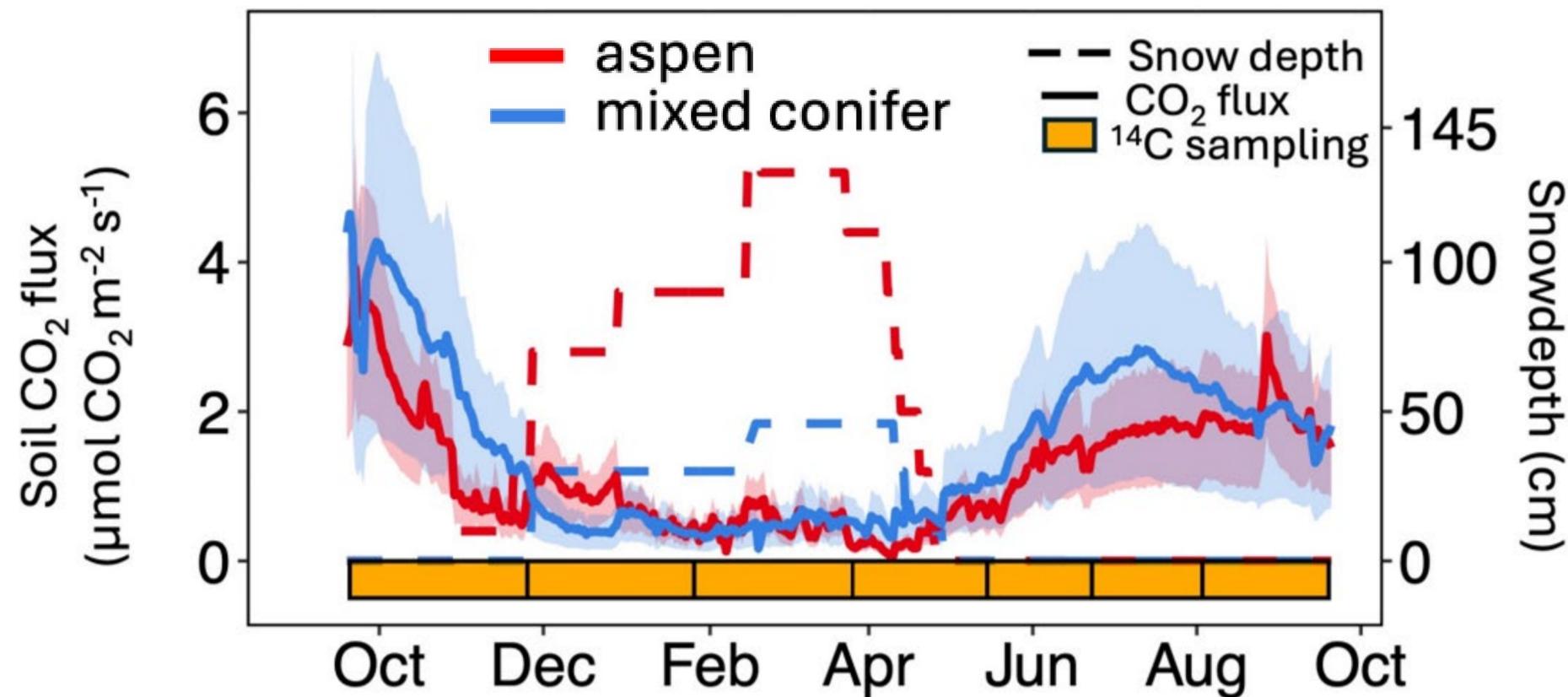


Future direction

Fractional contribution of two sources

Mass balance: $\Delta^{14}\text{C}_{\text{Soil CO}_2} = F \times \Delta^{14}\text{C}_{\text{root}} + (1-F) \times \Delta^{14}\text{C}_{\text{decomp}}$

$\Delta^{14}\text{C}_{\text{Soil CO}_2}$: Collect in field
 F : Fraction of respiration from roots
 $\Delta^{14}\text{C}_{\text{root}}$: Root incubation
 $(1-F)$: Fraction of respiration from microbes
 $\Delta^{14}\text{C}_{\text{decomp}}$: Soil incubation

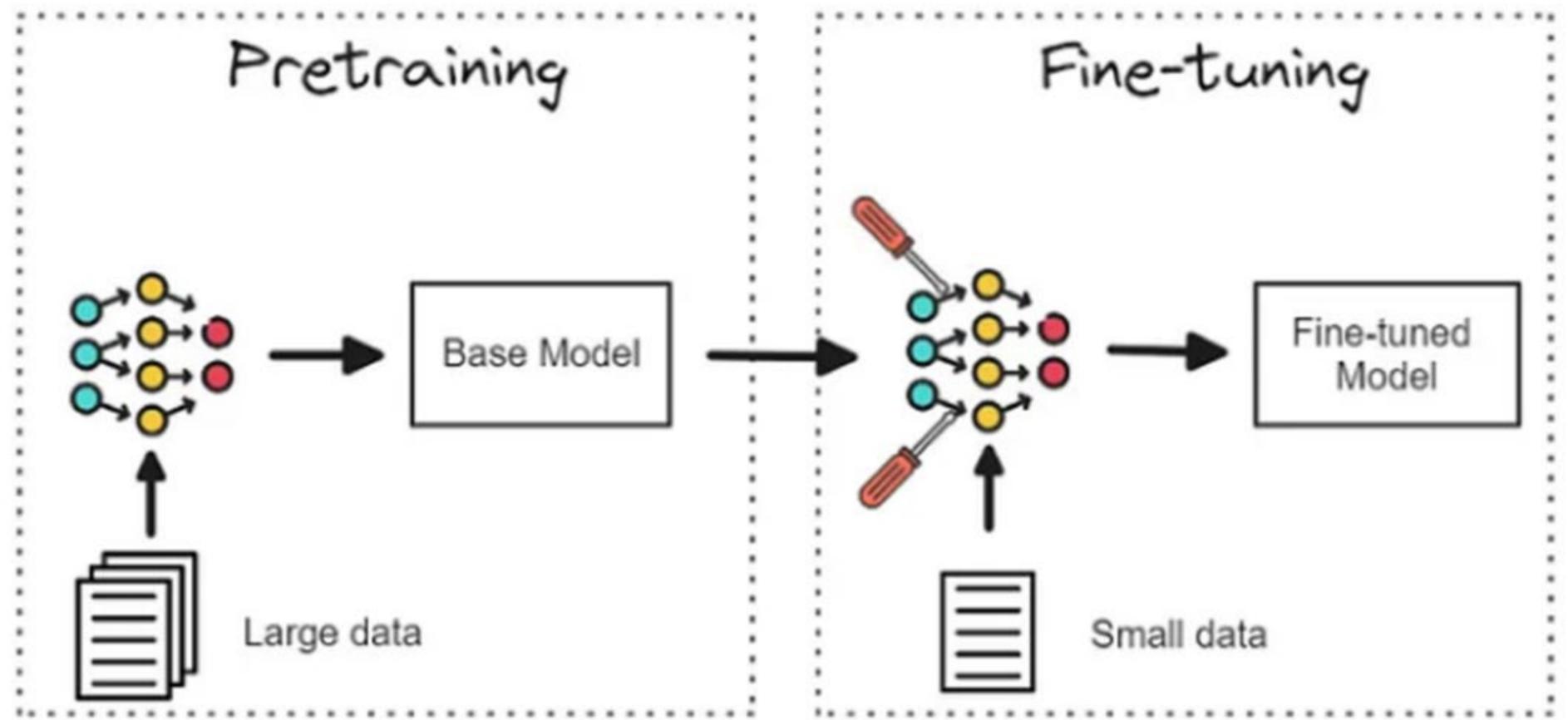


- Target: microbial decomposition and root respiration;
- Measurement: ¹⁴C partitioning;
- Valuable but sparse dataset;



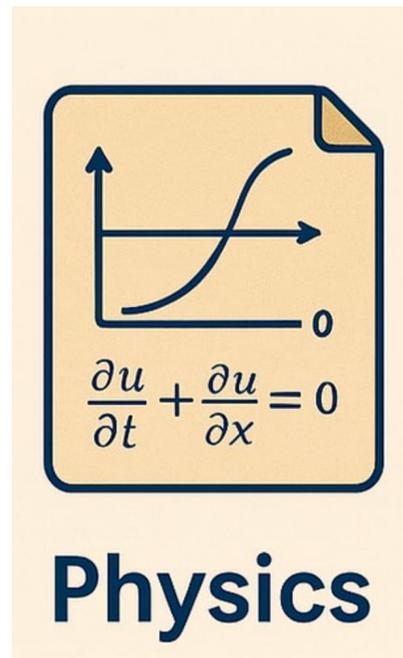
Future direction

Datasets



Using CLM and MIMICS simulations under different scenarios

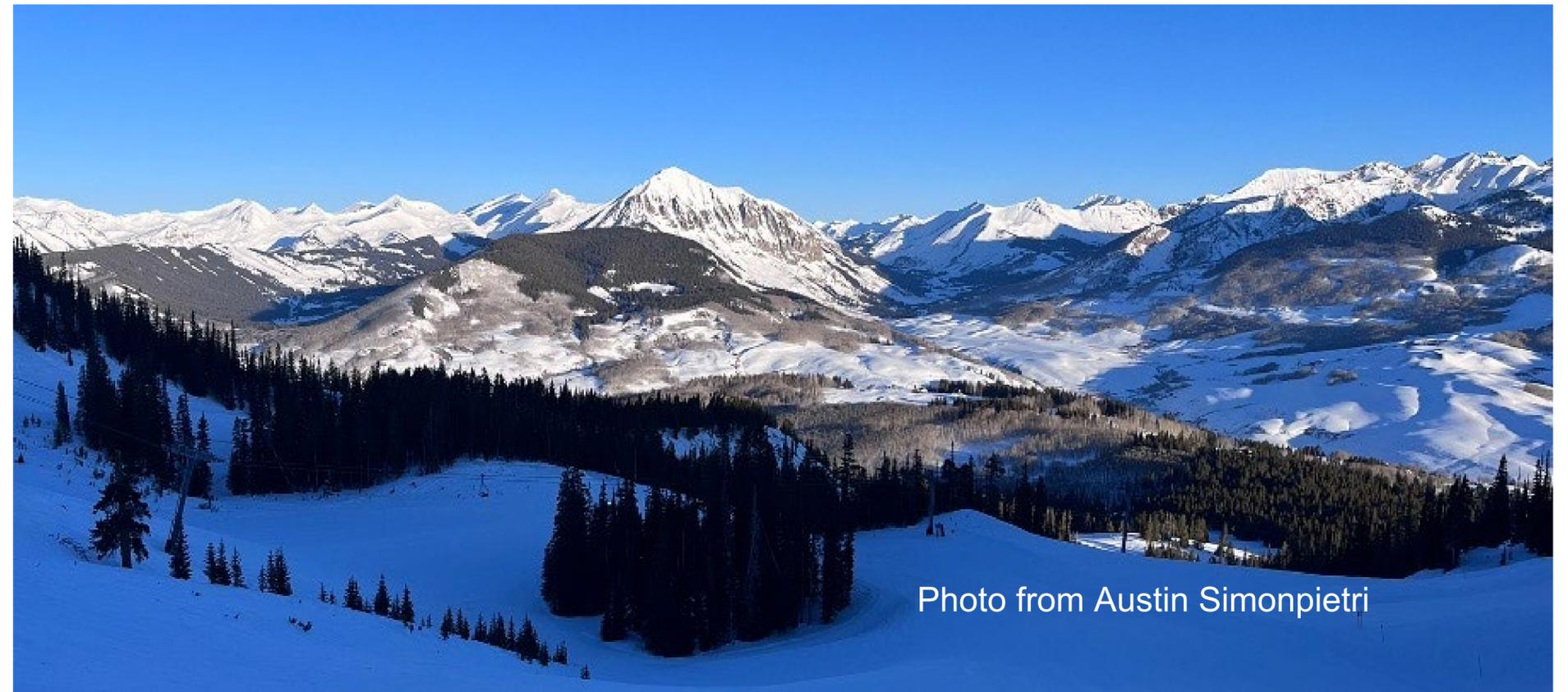
Isotope-partitioned measurements



- Mass balance
- Different temperature sensitivities
- Substrate supply ...

Take home message

- Classic NN: purely data-driven, but may misattribute effects from different drivers.
- PINN: guides temperature sensitivity toward biologically realistic values without sacrificing accuracy.



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Flux gradient approach

- Flux-gradient approach we are using is very sensitive to the estimated **soil diffusivity** , which is estimated from bulk density and volumetric water content at three depths. So, if heavy rain saturates the upper 1 cm of soil, CO₂ may build up at all three depths, the CO₂ gradient in the soil would be incorrectly converted to a flux estimate because we aren't accounting for that saturated layer.