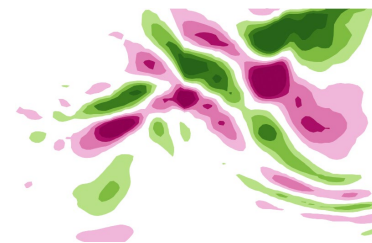
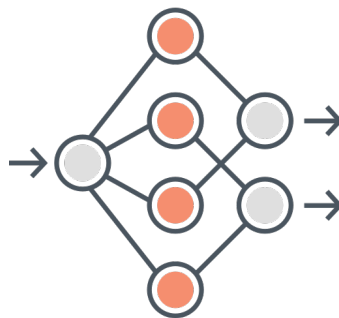
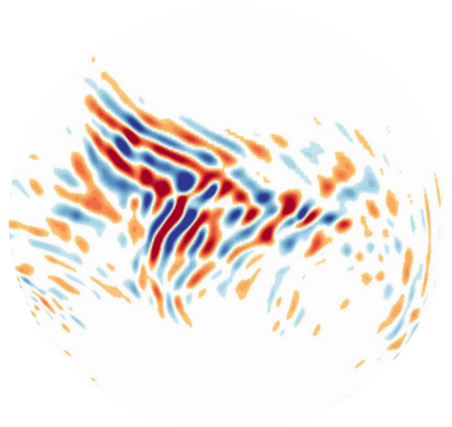


Nonlocal Deep Learning Parameterization for Process Representation in Climate Models

Aman Gupta, Aditi Sheshadri, Tom Meltzer, Sujit Roy, Valentine Anantharaj

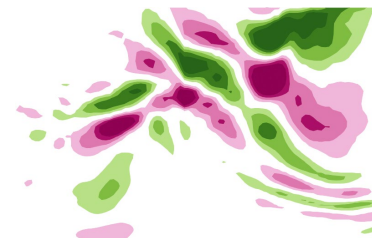
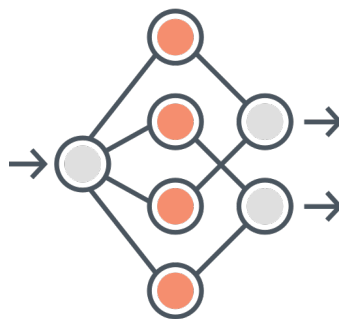
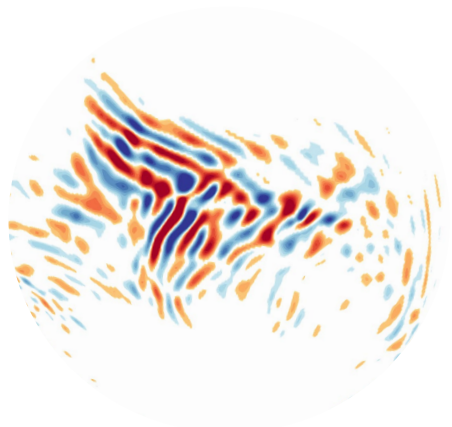
30th CESM Workshop, Boulder, CO
11th June 2025



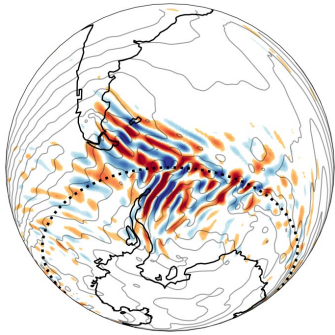
Nonlocal Deep Learning Parameterization for **Atmospheric Gravity Waves** Representation in Climate Models

Aman Gupta, Aditi Sheshadri, Tom Meltzer, Sujit Roy, Valentine Anantharaj

30th CESM Workshop, Boulder, CO
11th June 2025



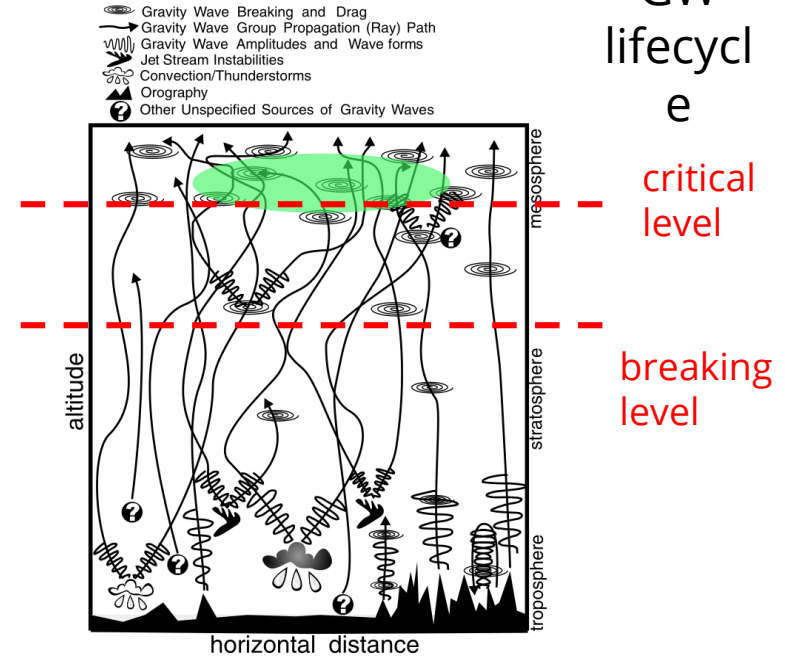
Atmospheric Gravity Waves (GWs)



- ✦ Sources: jets, convection, mountains etc.
- ✦ Multiple scales: 100 m to 1000s km

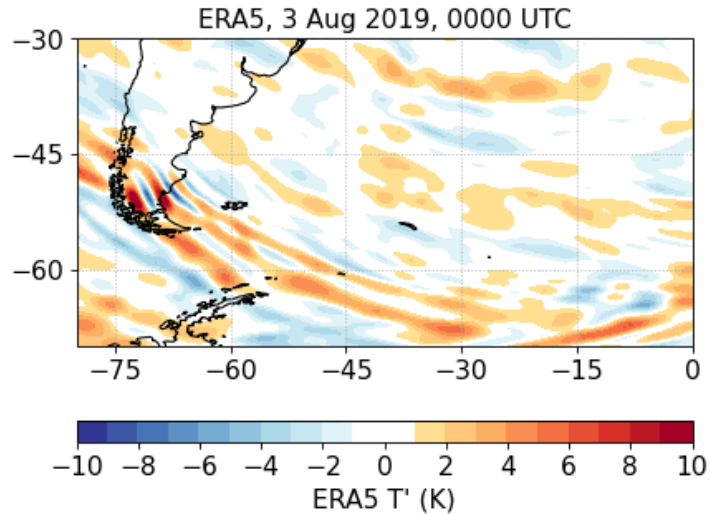
$$c_z \sim 0-15 \text{ m/s}$$

$$c_H \sim 0-150 \text{ m/s}$$



- ✦ Vertical coupling: carry near surface momentum to upper atmosphere within hours. 10x faster propagation in the horizontal.

Current GW Parameterizations have Notable Biases

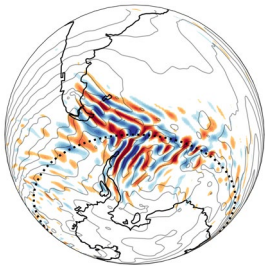


Key properties:

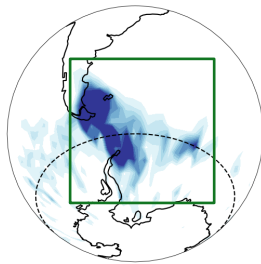
- 1) **Lateral propagation:** of wave fluxes away from source
- 2) **Refraction:** changes in wavenumber as they propagate
- 3) **Transience:** temporal coherence of wave packets

Biases in:

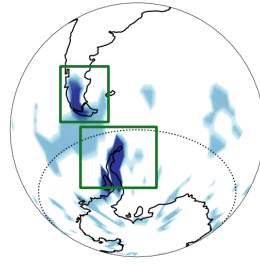
- a) QBO representation
- b) "cold-pole" bias in Austral summer stratosphere
- c) Midlatitude jet strength and mesospheric overturning circulation



phase structure



resolved flux



parameterized flux

ML to Learn Subgrid-scale Gravity Wave Fluxes

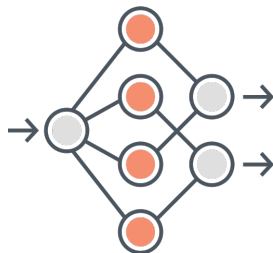
Learn momentum fluxes
from high-resolution, GW-
resolving data



Couple the ML flux predictor to a
coarse-resolution climate model

Background atmospheric
conditions
(*resolved by climate models*)

$$\begin{bmatrix} u \\ v \\ \theta \\ \omega \end{bmatrix}$$

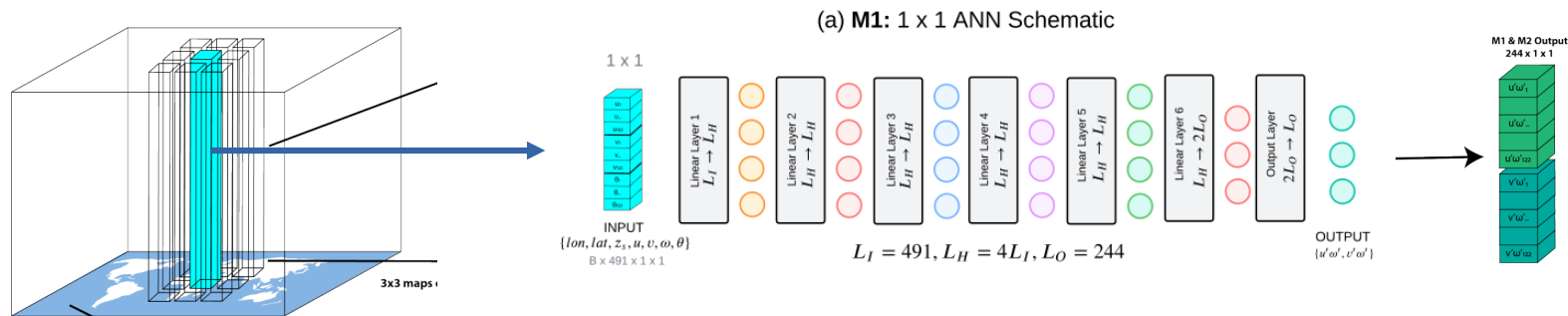


$$\begin{bmatrix} u'\omega' \\ v'\omega' \end{bmatrix}$$

Gravity wave
momentum fluxes from high-
resolution reanalysis/obs
(*unresolved by climate models*)

We train three ML models with varying degrees of nonlocality

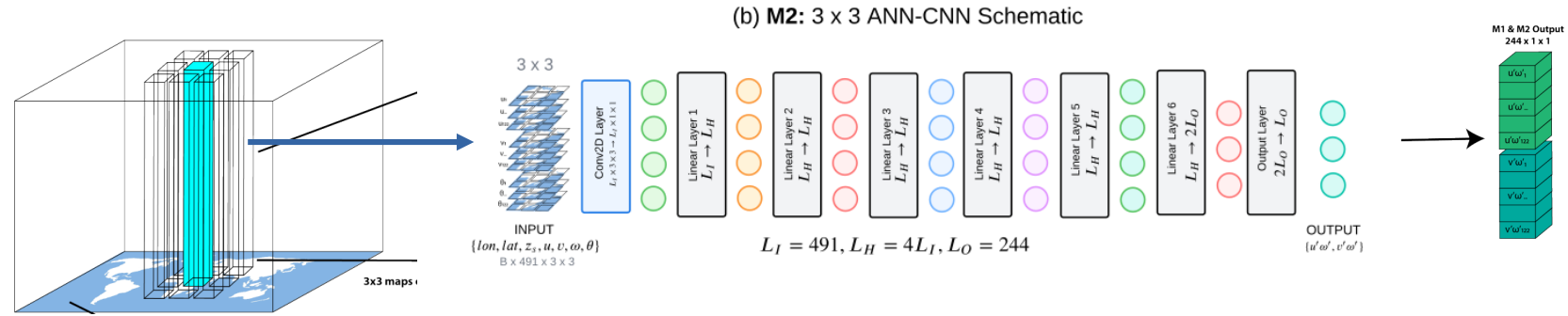
M1: Single Column



Model M1: inspired from traditional parameterizations
Dynamical variables in a column used to predict flux in the column

We train three ML models with varying degrees of nonlocality

M2: Multiple Columns

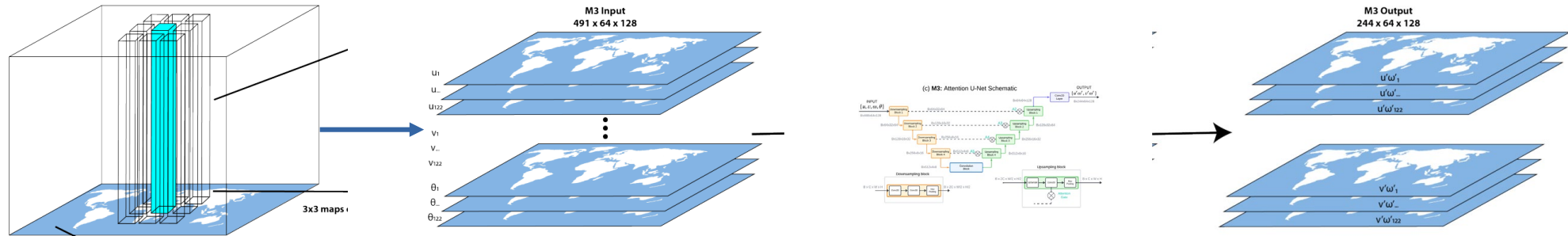


Model M2: Introducing slight nonlocality in space

Dynamical variables in 1 + 8 neighboring columns to predict fluxes in the central column

We train three ML models with varying degrees of nonlocality

M3: Global Attention U-Net



Model M3: Globally nonlocal Attention UNet (Oktay et al. 2018)
Global input of dynamical variables to predict fluxes globally.

ML to Learn Subgrid-scale Gravity Wave Fluxes

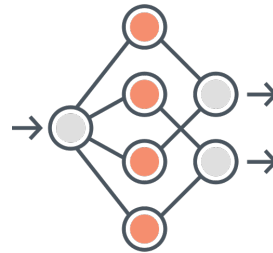
Learn momentum fluxes
from high-resolution, GW-
resolving data



Couple the ML flux predictor to a
coarse-resolution climate model

Background atmospheric
conditions
(resolved by climate models)

$$\begin{bmatrix} u \\ v \\ \theta \\ \omega \end{bmatrix}$$

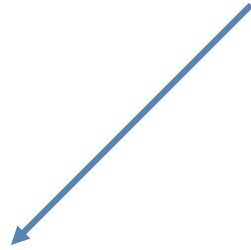


$$\begin{bmatrix} u' \omega' \\ v' \omega' \end{bmatrix}$$

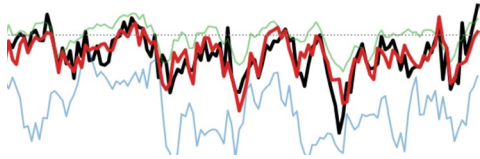
Gravity wave
momentum fluxes retrieved
from high-resolution reanalysis
(unresolved by climate models)

Trained on 4 years of ERA5 and 4 months (NDJF) of 1.4 km ECMWF-IFS

Evaluate performance beyond RMSE



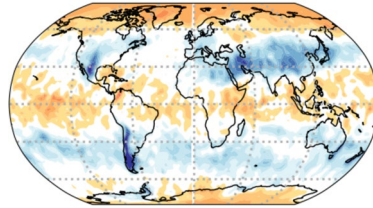
Test 1. Temporal Evolution



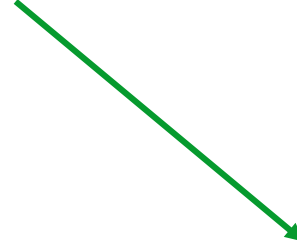
Does the model correctly learn the temporal wave evolution



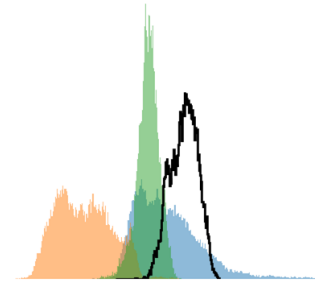
Test 2. Seasonal Averages



Does the model generate accurate global flux distribution?

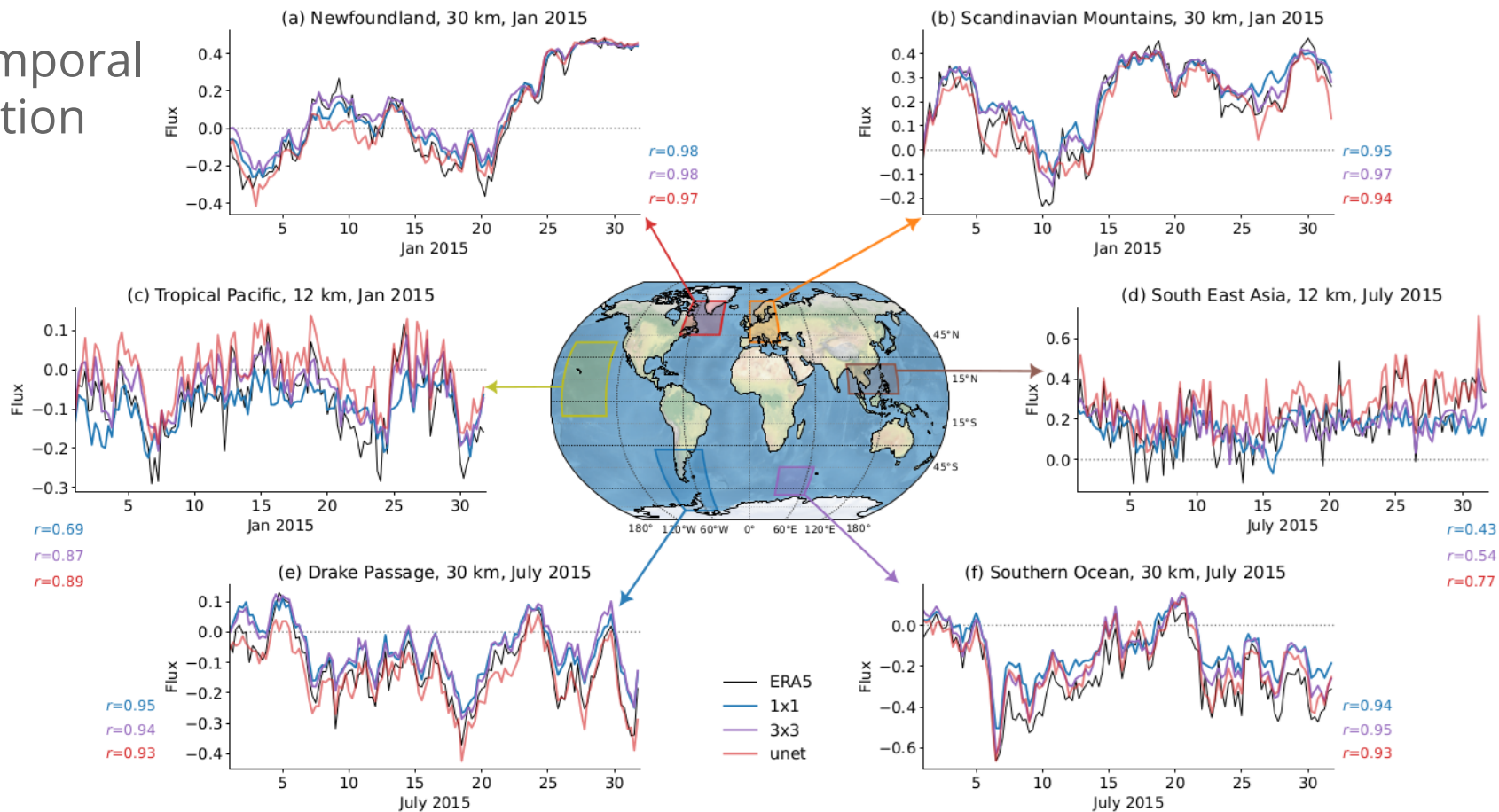


Test 3. Flux distribution



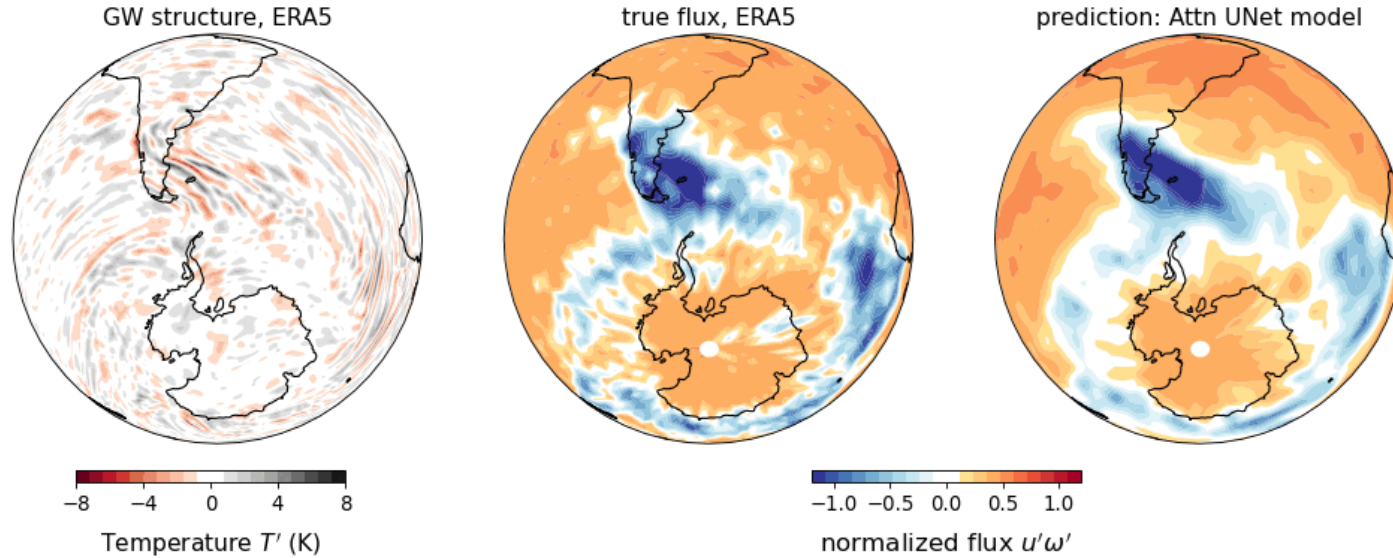
Does the model generate desired statistics?

1. Temporal Evolution



ML models skillfully learn the intermittent and coherent evolution of GW fluxes in the atmosphere over both orographic and nonorographic hotspots. **Nonlocal models perform better.**

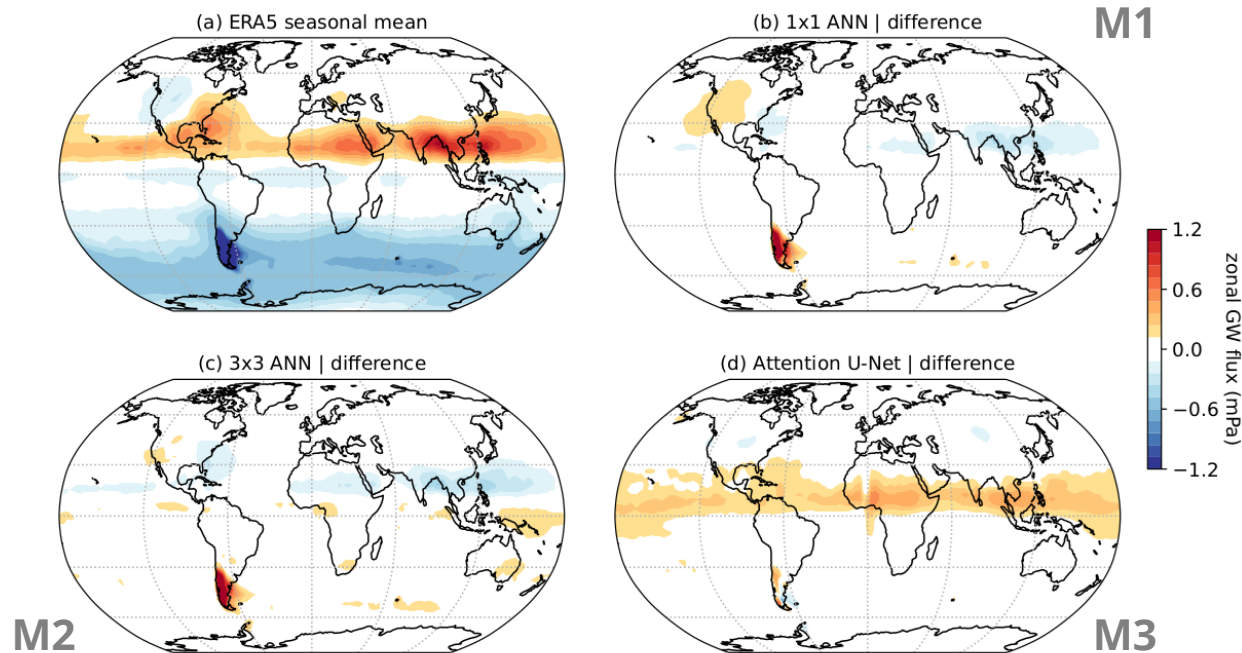
GWs in the Southern Hemisphere, 30 km (10 hPa), 16-07-2015 01 UTC



Attention UNet correctly identifies wave excitation and lateral propagation over multiple hotspots over the Southern Ocean (Andes, small islands, storm tracks, Antarctic Peninsula, etc.)

Successful simulation of belts of midlatitude GW activity in both hemispheres without special provisions for recurrence.

JJA mean zonal flux comparison, 10-30 hPa average

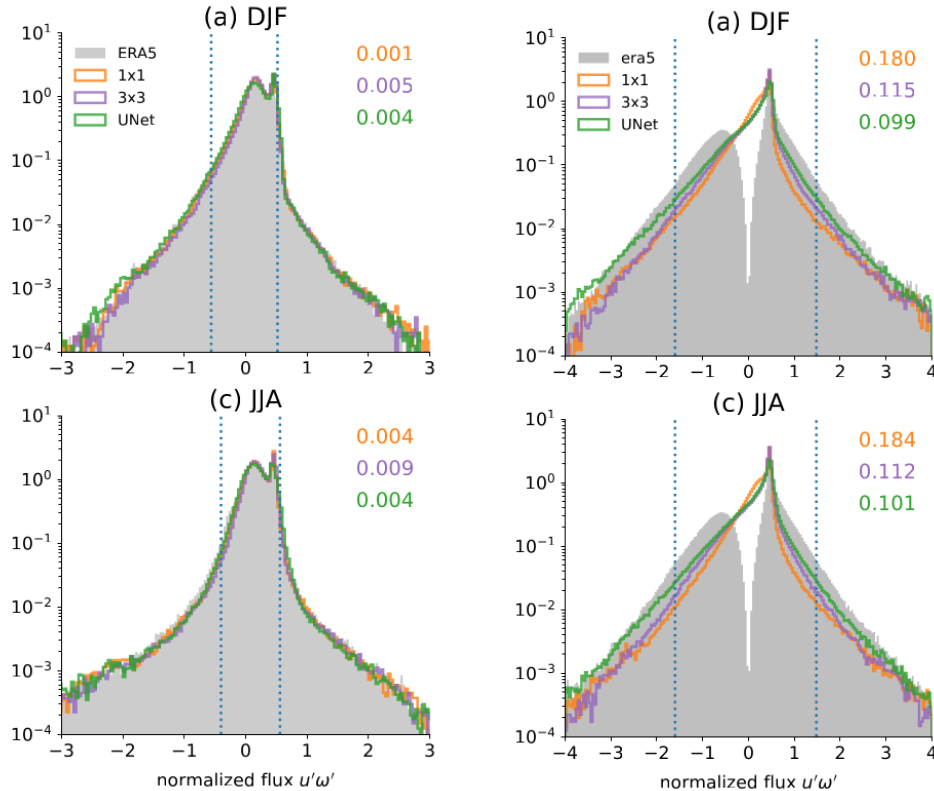


2. Seasonal Average

All of M1, M2, M3 generate reasonable predictions.

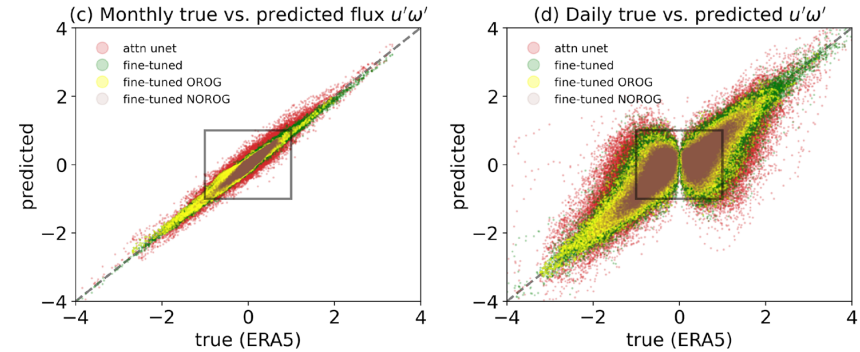
Attention UNets generate the most accurate predictions in the midlatitudes (where horizontal propagation is most prominent).

3. Global Flux Distribution



Seasonal
averages

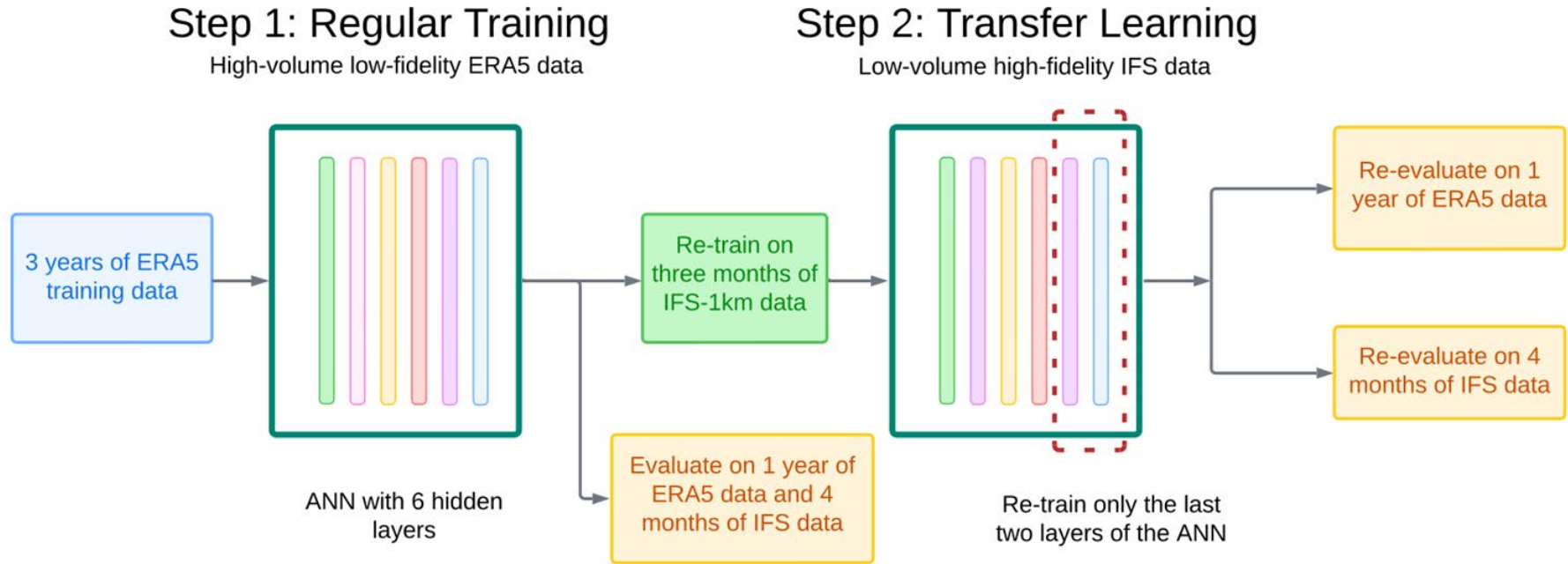
daily
averages



The seasonally averaged distributions are reproduced quite well.

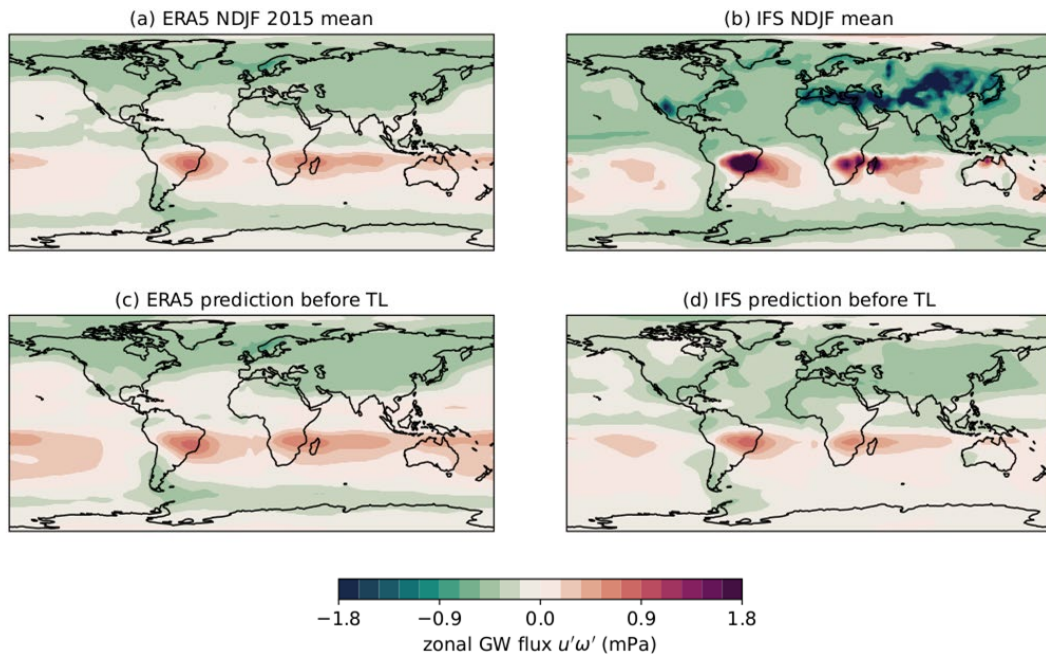
... but the neural nets struggle with small values – predict zeros instead.

Improving predictions using transfer learning



Next, the learning is augmented by using limited-but-high-resolution data which fully resolved GWs

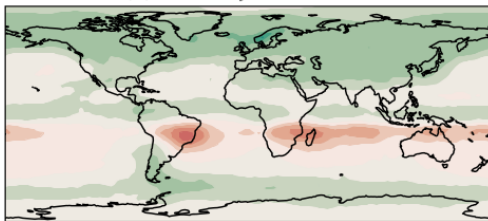
Transfer learning on Attention UNet | u, v, θ, ω | 10-30 hPa



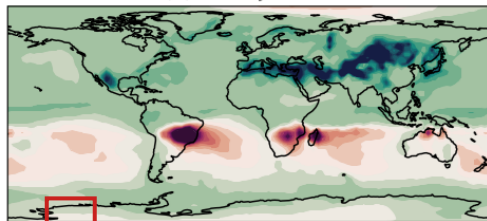
ML models trained only on ERA5 underestimate fluxes in 1km-IFS

Transfer learning on Attention UNet | u, v, θ, ω | 10-30 hPa

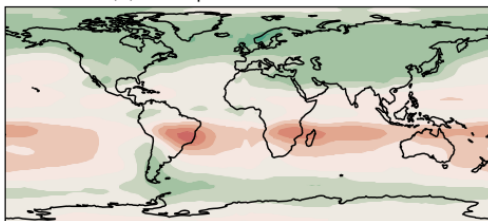
(a) ERA5 NDJF 2015 mean



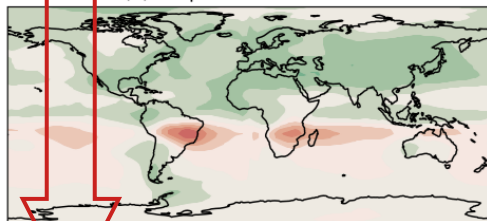
(b) IFS NDJF mean



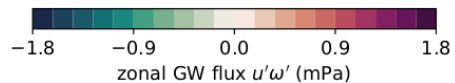
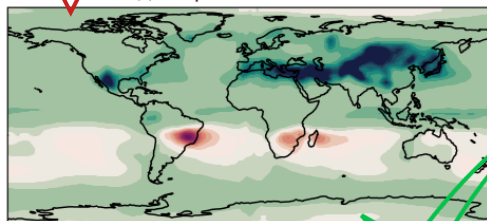
(c) ERA5 prediction before TL



(d) IFS prediction before TL

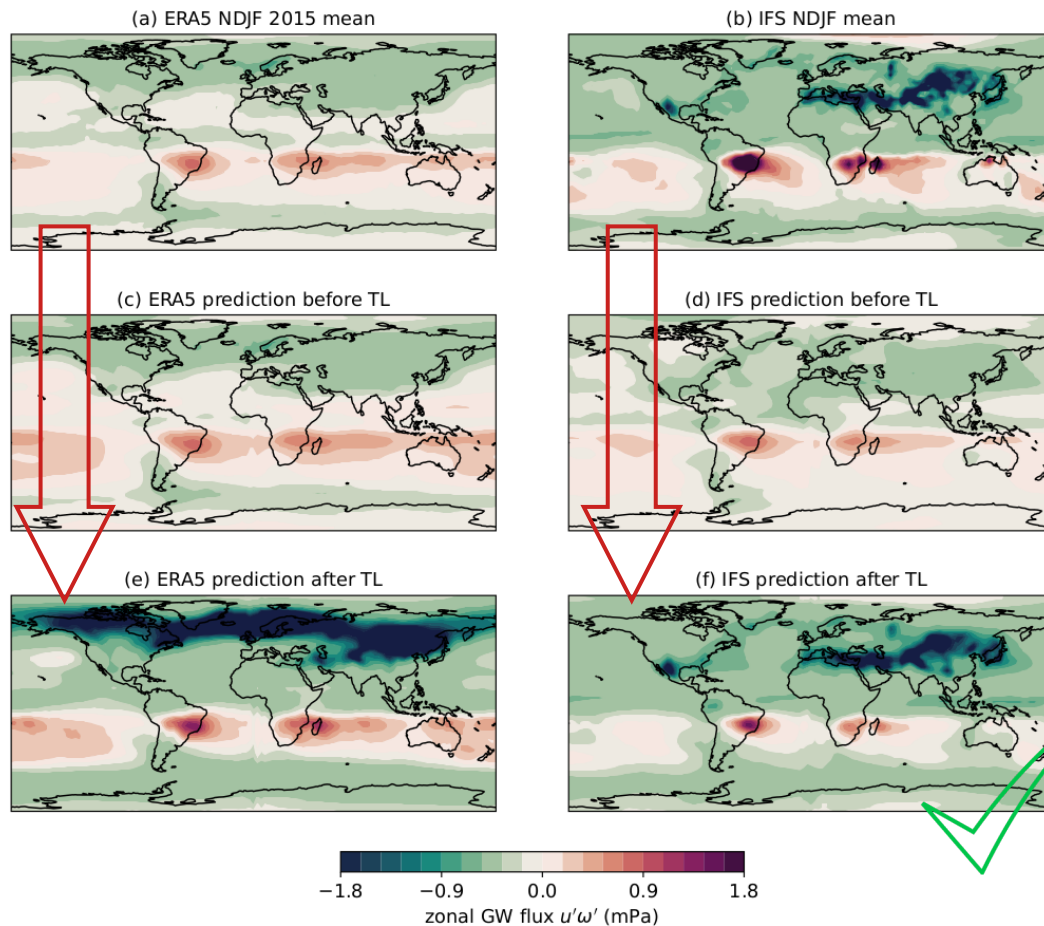


(f) IFS prediction after TL



Following Transfer Learning, models predict stronger fluxes in ERA5, while identifying the correct hotspots.

Transfer learning on Attention UNet | u, v, θ, ω | 10-30 hPa



Following Transfer Learning, models predict stronger fluxes in ERA5, while identifying the correct hotspots.

Thus, the models effectively blend learnings from both *low-fidelity high-volume* and *high-fidelity low-volume* datasets.

Potential to learn from multiple high-resolution climate datasets.

A Nonlocal Deep Learning Parameterization for Climate Model Representation of Atmospheric Gravity Waves: Offline Performance

Aman Gupta¹, Aditi Sheshadri¹, Sujit Roy^{2,3}, Valentine Anantharaj⁴

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²Earth System Science Center, The University of Alabama in Huntsville, Huntsville, AL, USA

³NASA Marshall Space Flight Center, Huntsville, AL, USA

⁴Oak Ridge National Laboratory, Oak Ridge, Tennessee, USA

Submitted to JAMES (preprint:
[authorea.com//1263806](https://authorea.com/publication/1263806)

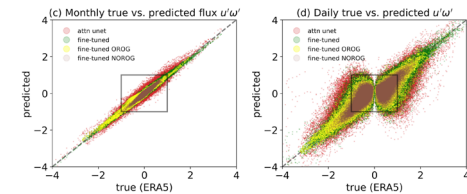
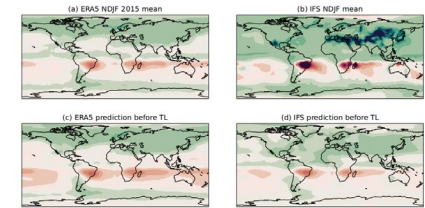
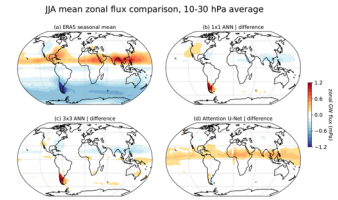
Code:

github.com/DataWaveProject/nonlocal_gwfluxes

HiRes IFS data: *<https://osf.io/gx32s/>*

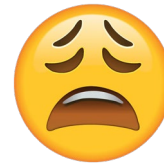
Key Conclusions

1. The three ML schemes learn nonlocal propagation, temporal coherence, and seasonal distributions of GW fluxes from high-resolution data.
2. The model with the highest embedded nonlocality generates the best predictions.
3. Transfer learning allows blending multiple datasets to improve performance
4. Limitation: the schemes proficiently predict large-amplitude GW packets, but predicting small values is still a challenge

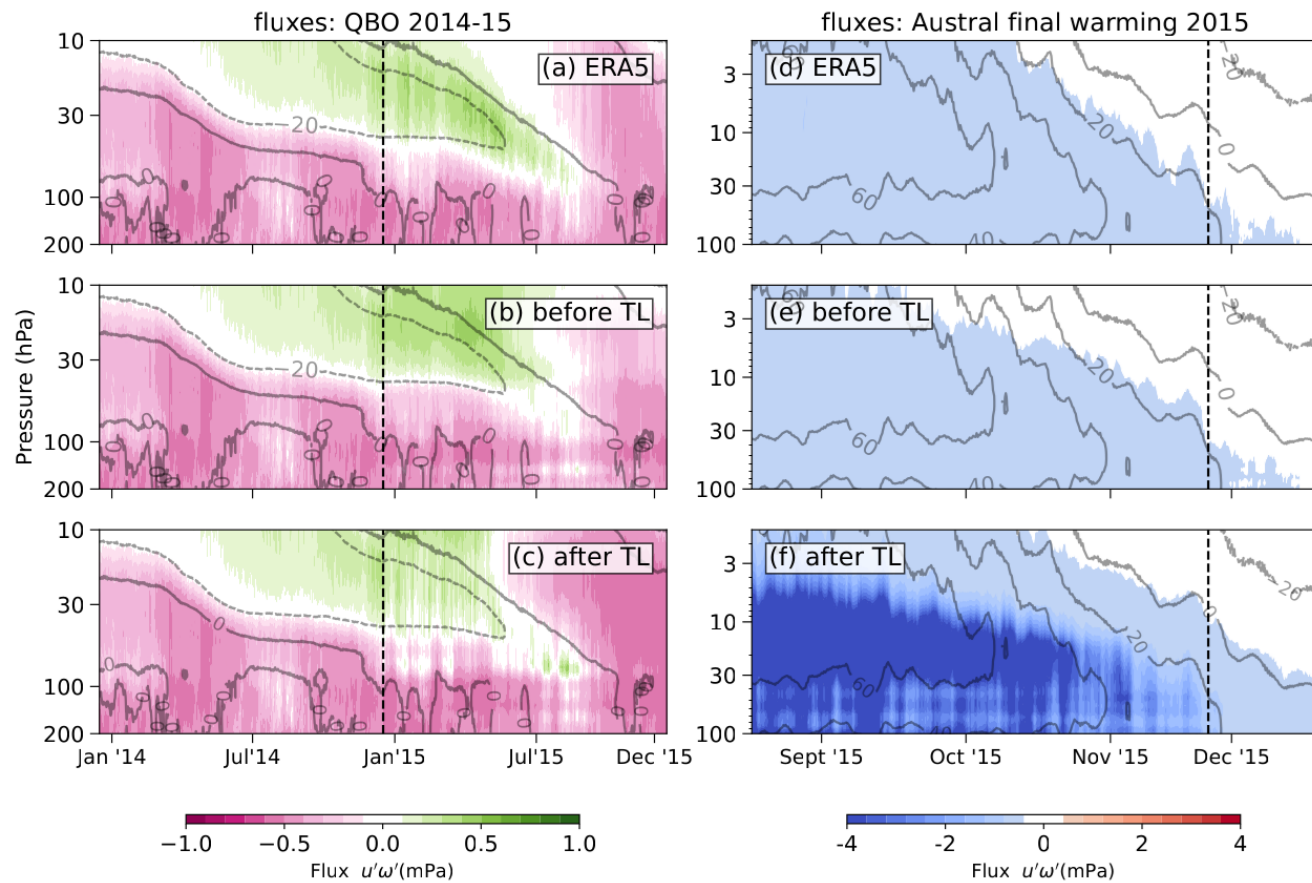


In Progress

1. Testing performance on dissimilar model outputs: high-resolution CAM and ICON runs.
2. Coupling to test online performance in CAM7: challenges



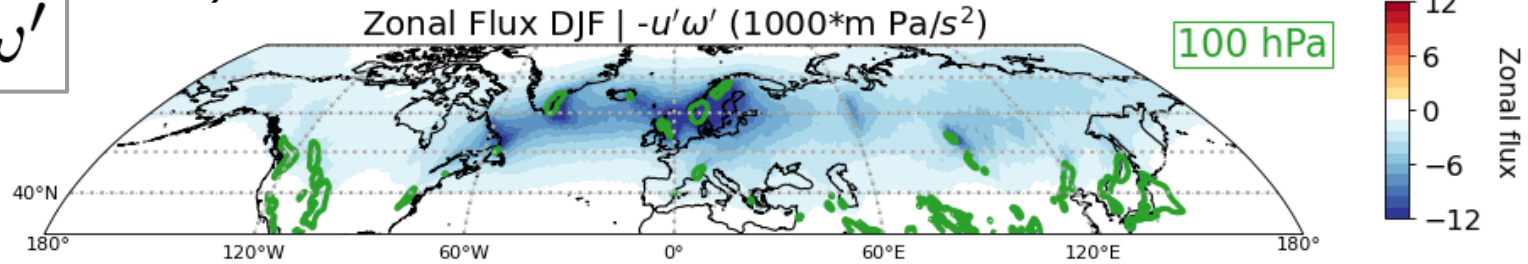
Supplemen t



GWs form a belt of wave activity in the middle atmosphere

Green: Flux envelope, Color: Flux at 2 hPa (~45 km)

$$-u'\omega'$$

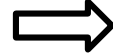


1979-2022
December
January
February
mean
From
reanalysis

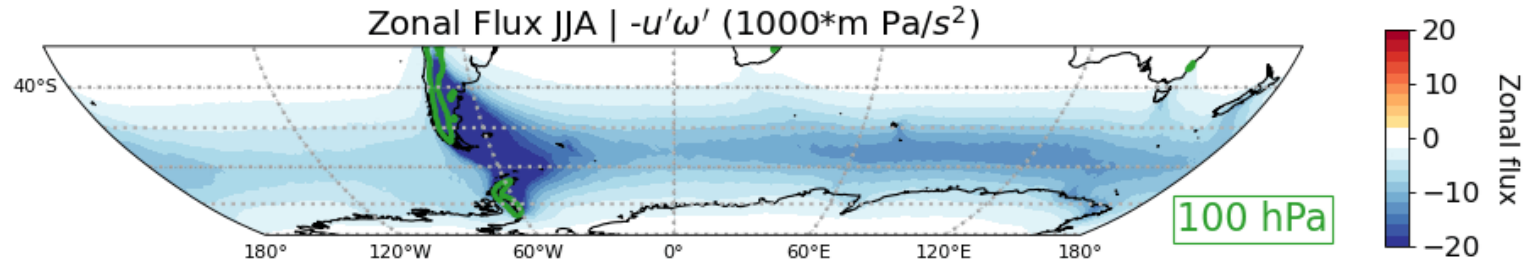
local GW
generatio



propagation through
strong shear



global
spreadin



1979-2022
June
July
August
mean from
reanalysis

Critical Impacts of Gravity Waves



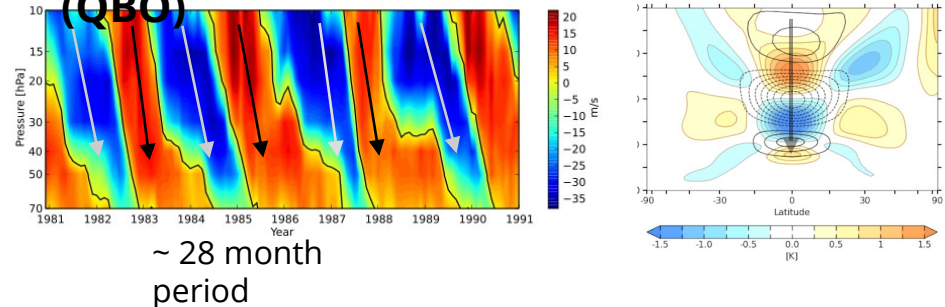
Atmospheric GWs induce clear air turbulence (CAT) and influence upper tropospheric predictability.

Severe Convectively Induced Turbulence Hitting a Passenger ...

by S Gisinger · 2024 · Cited by 2 — The Singapore Airlines flight SQ321 was on its way from London to Singapore when severe turbulence was encountered over Myanmar on 21 May 2024.

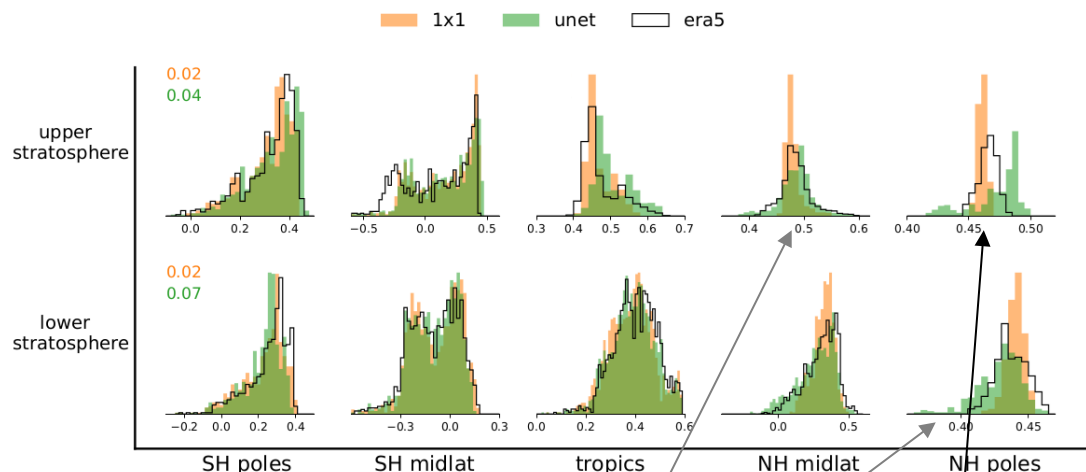
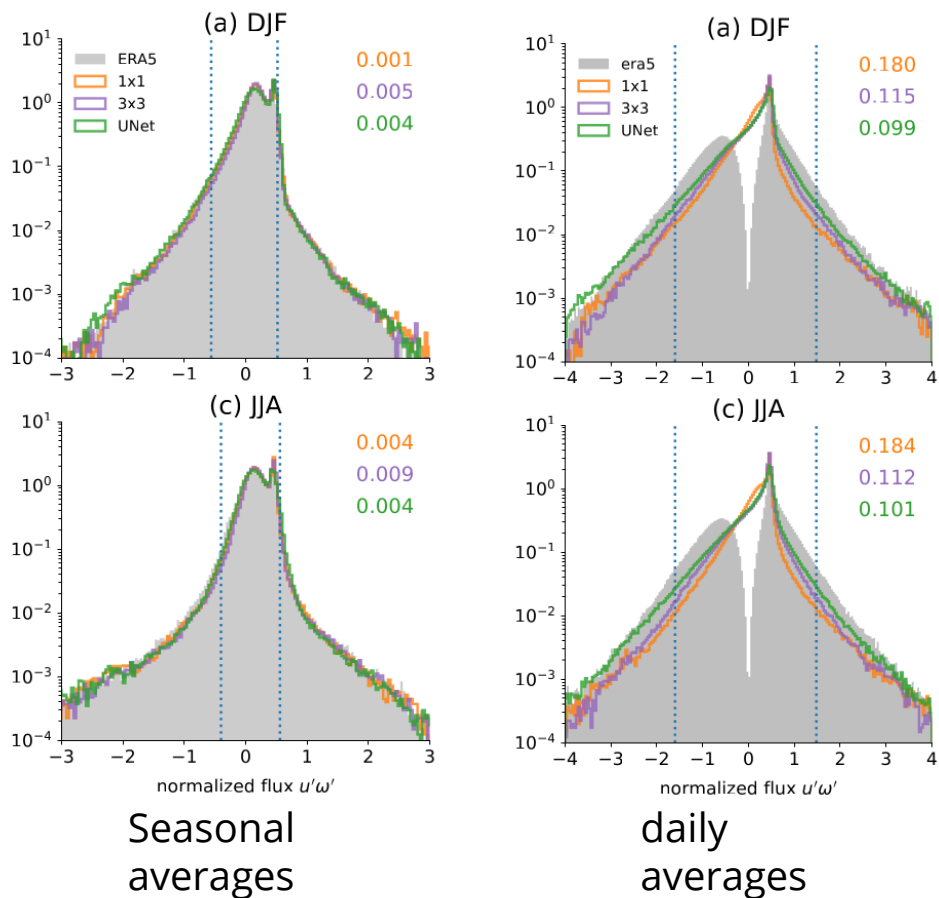
Key drivers of global circulation and periodic wind patterns, in the middle atmosphere. Indirectly influencing Antarctic summer heat extremes via polar vortex variability (Choi et al., 2024).

Tropical Quasi-Biennial Oscillation (QBO)



3. Global Flux Distribution

$$\mathcal{H}(p, q) = \frac{1}{2} \int_{x \in X} \left(\sqrt{p(x)} - \sqrt{q(x)} \right)^2 dx = 1 - \int_{x \in X} \sqrt{p(x)q(x)} dx.$$



The three models generate comparable distribution tails for all seasons

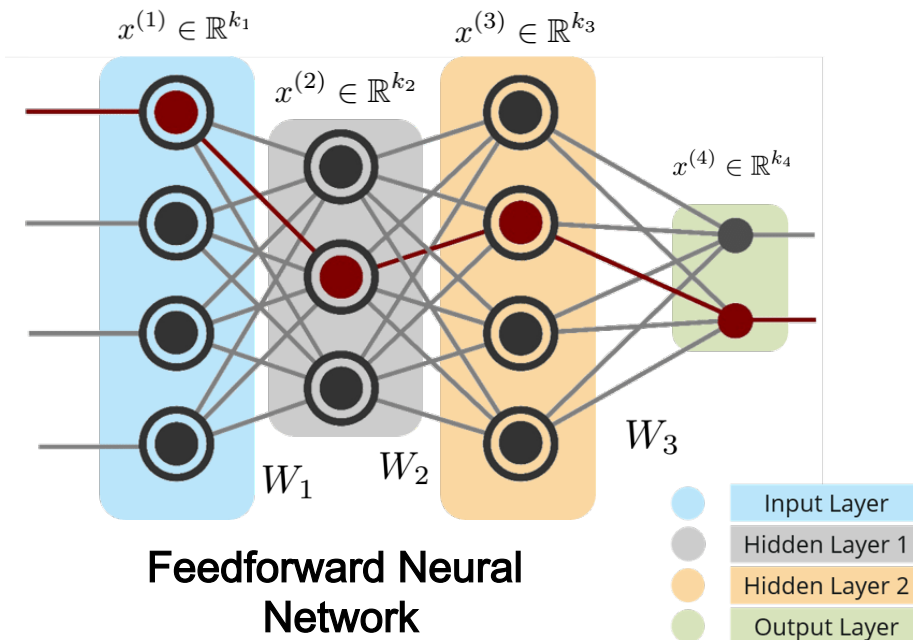
Prominent narrow bias in flux predictions by ANNs

Areas of weak GW activity (in summer stratosphere) most challenging to simulate.

Neural Network as a Collection of Perceptrons

Brain is a network of interconnected neurons. For any input/actions, only selected neurons fire at a given time. A **multi-layer perceptron (MLP)** is a collection of neurons with equisized, fully-connected hidden layers. Similarly, a size-varying MLP without loops is called a **feedforward neural network**.

Consider a feedforward neural network arranged as an input layer, 2 hidden layers, and an output layer:



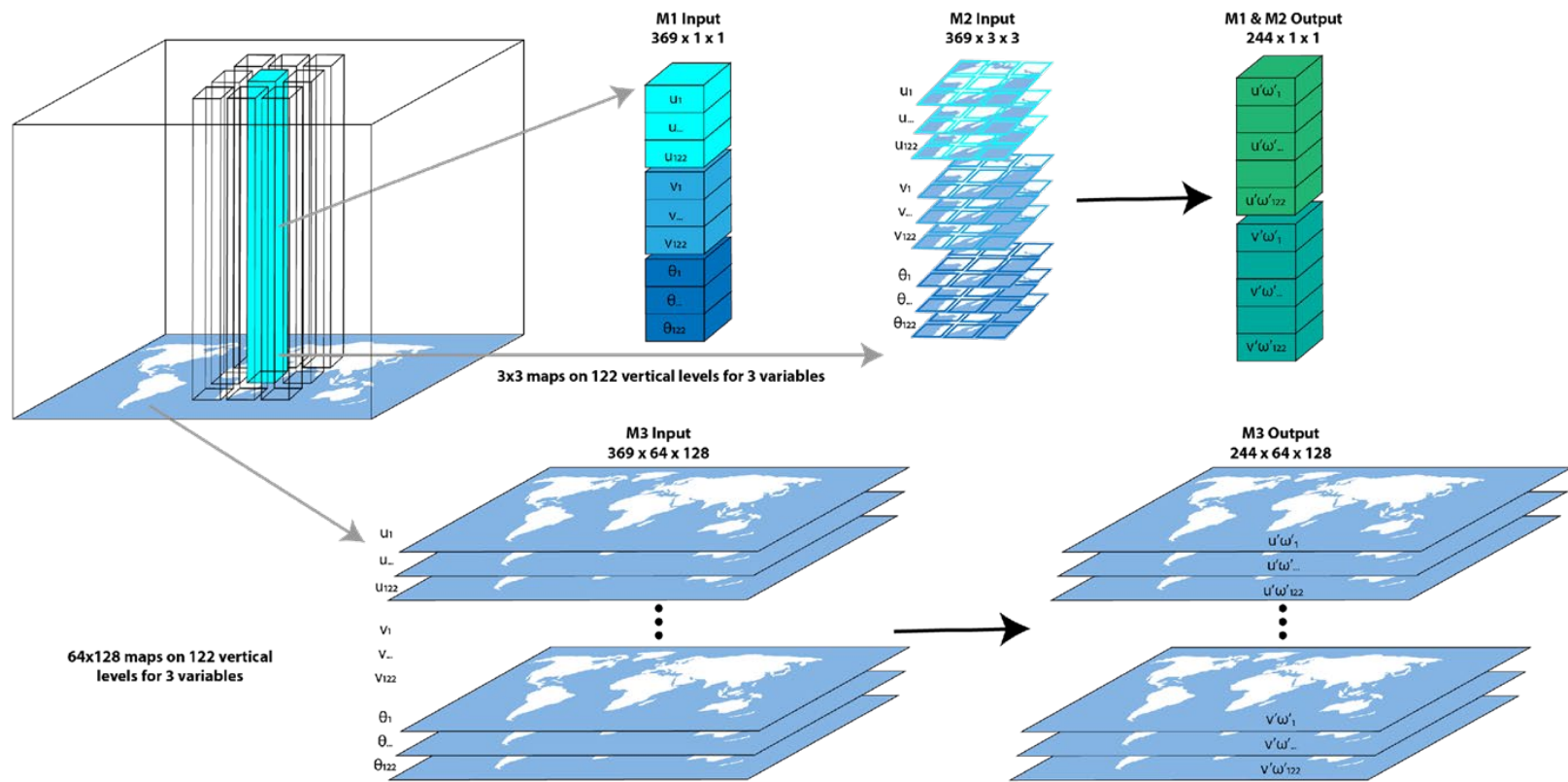
Forward Propagation

- (1) Each layer maps to the next using a set of weights
- (2) The linear transformation is followed by a non-linear activation $\sigma(\cdot)$

$$x^{(i+1)} = \sigma \left(W_i^T x^{(i)} \right)$$

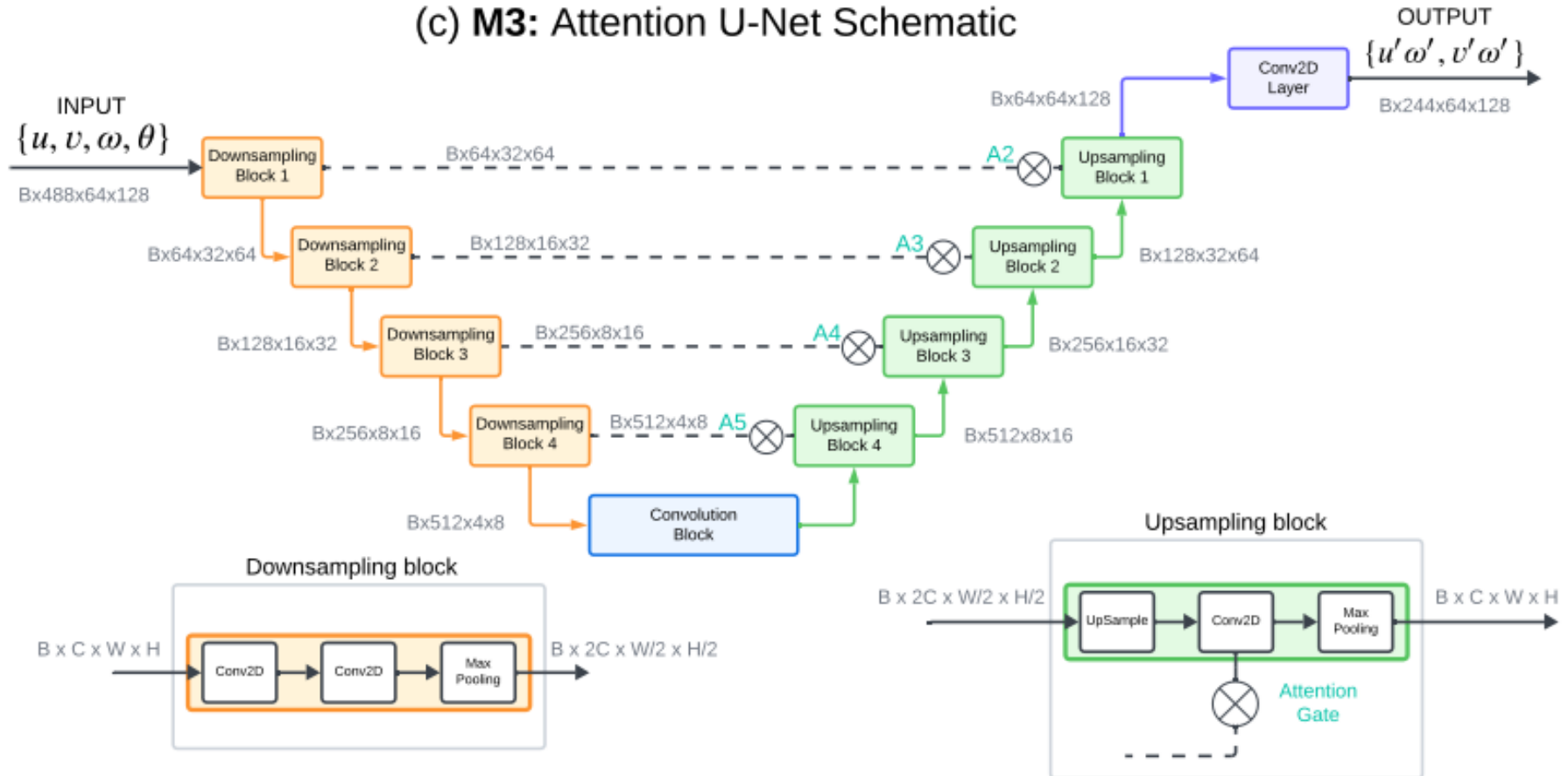
$$W_i \in \mathbb{R}^{k_i \times k_{i+1}}, \sigma_i : \mathbb{R}^{k_{i+1}} \rightarrow \mathbb{R}^{k_{i+1}}$$

Learning nonlocality through nonlocal architectures

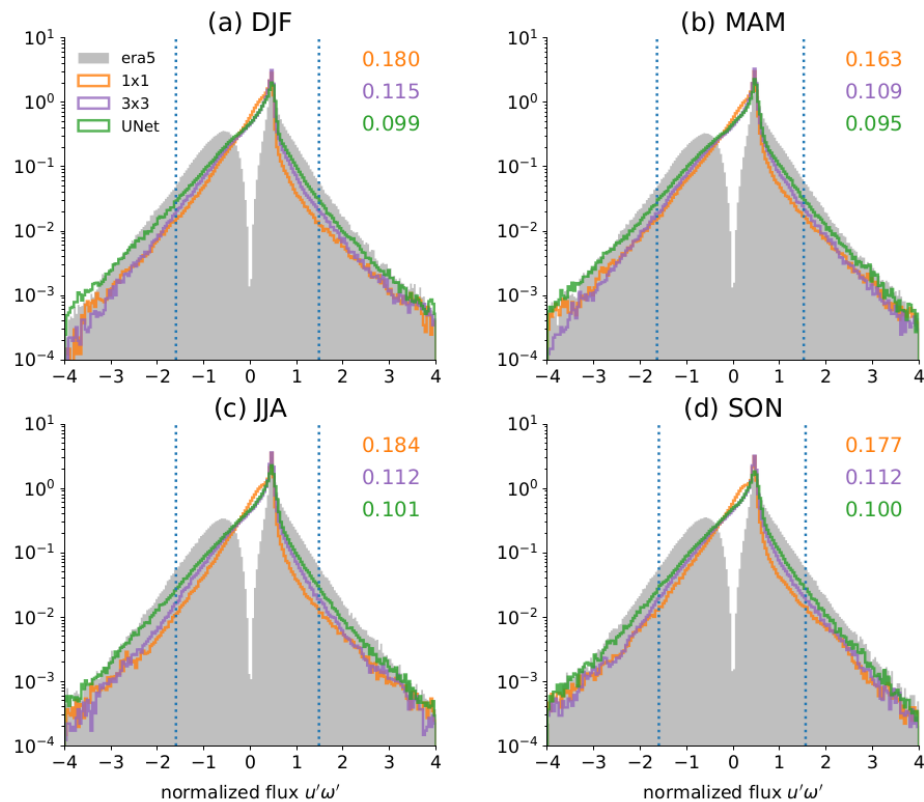


Attention UNet Schematic

(c) **M3**: Attention U-Net Schematic



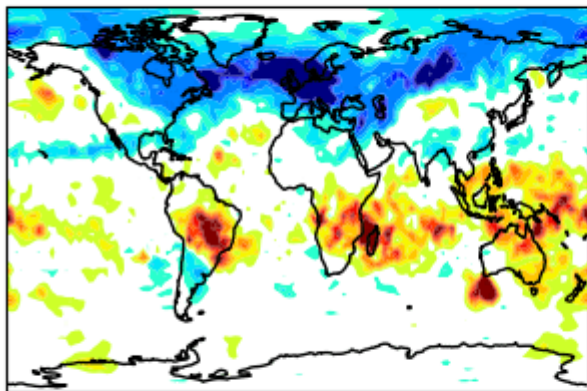
Daily Sampled Flux Distributions



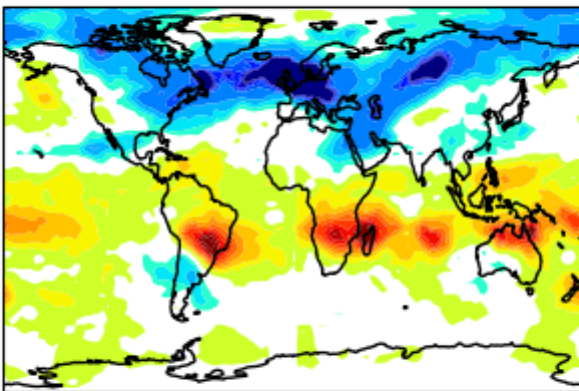
Transfer Learning on out-of-set months

Transfer Learning (TL) on 1-km IFS | 10-01-2015 01 UTC

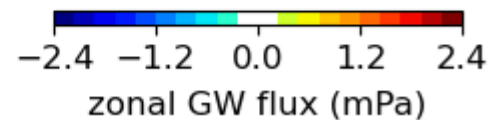
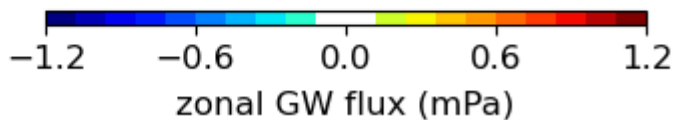
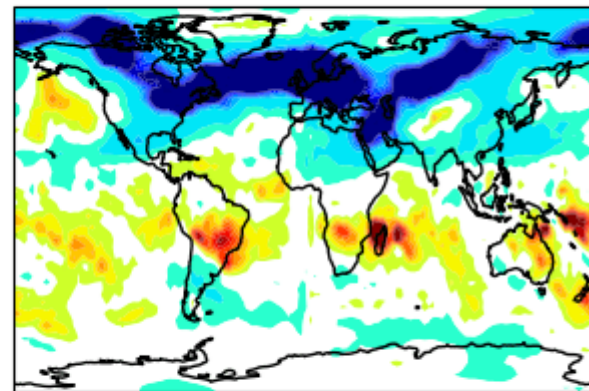
(a) ERA5 Flux



(b) Pred. flux before TL

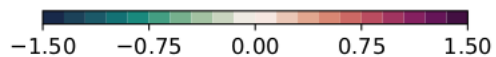
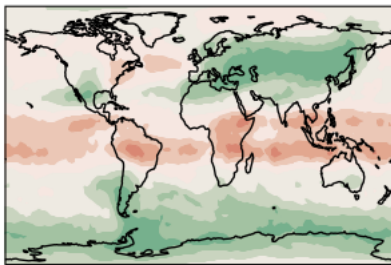


(c) Pred. flux after TL

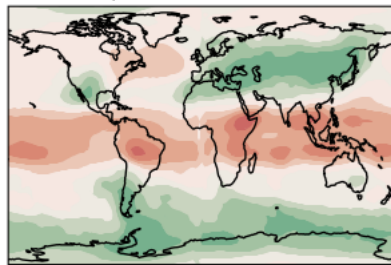


Apr
2015

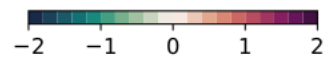
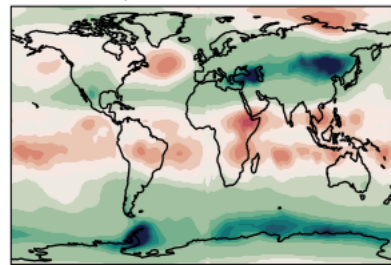
(a) resolved ERA5



(b) prediction before TL

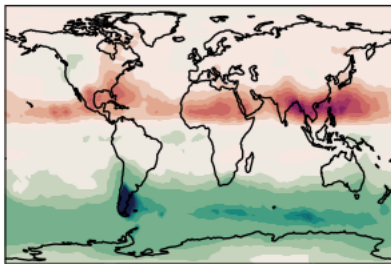


(c) prediction after TL

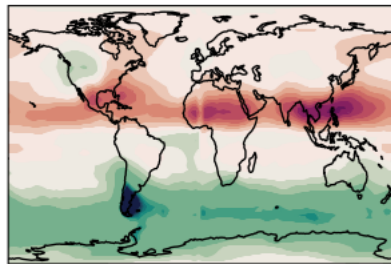


July
2015

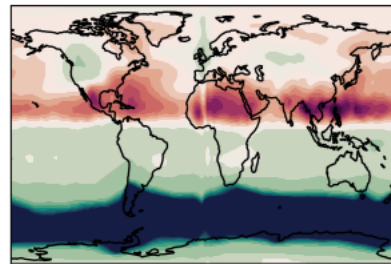
(d) resolved ERA5



(e) prediction before TL

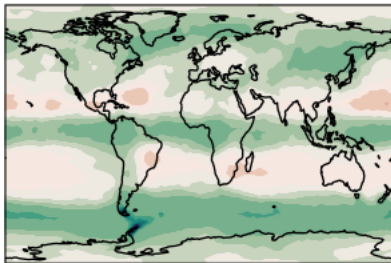


(f) prediction after TL

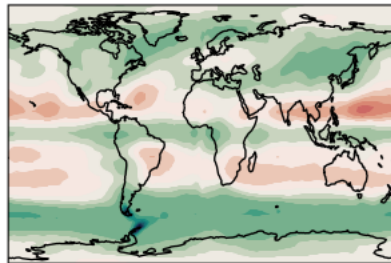


Oct
2015

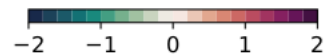
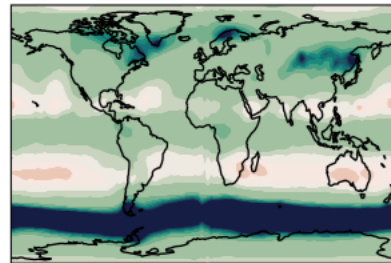
(g) resolved ERA5



(h) prediction before TL



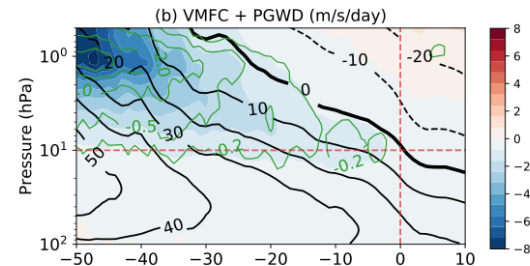
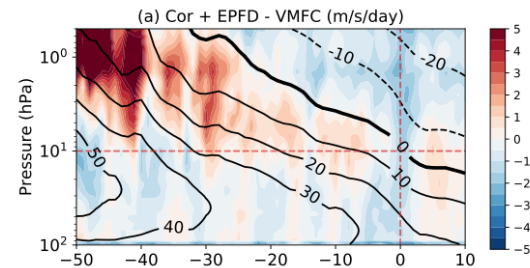
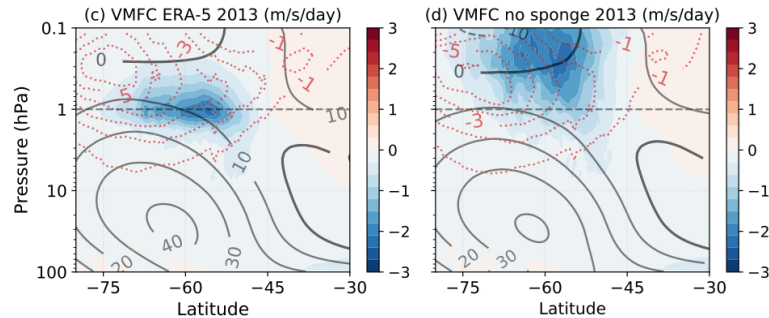
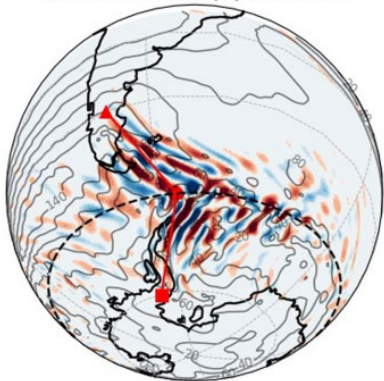
(i) prediction after TL



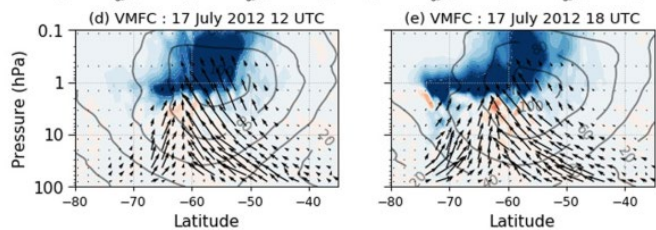
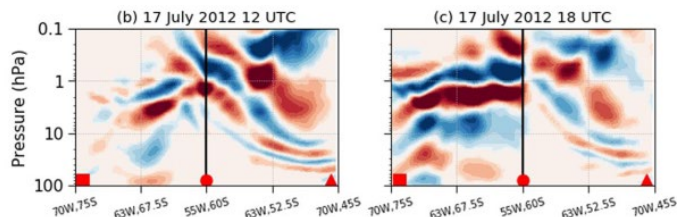
zonal GW flux $u'w'$ (mPa)

zonal GW flux $u'w'$ (mPa)

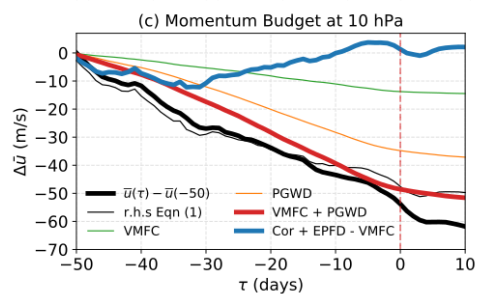
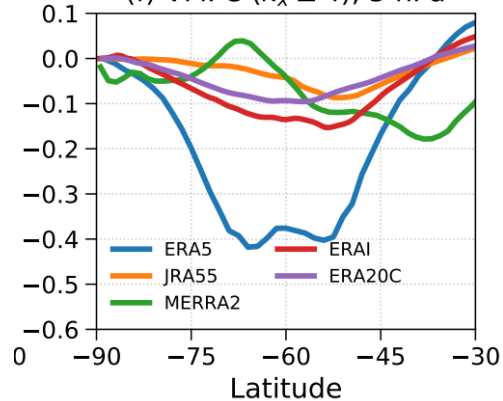
(a) T' at 1.5 hPa on 17 July 12 UTC



$$\bar{u}_t = \underbrace{\left(f - \frac{1}{R \cos \phi} (\bar{u} \cos \phi)_\phi \right)}_{\text{Cor}} \bar{v}^* - \underbrace{\bar{u}_p \bar{\omega}^*}_{\text{vAdv}} + \underbrace{\frac{1}{R \cos \phi} \vec{\nabla} \cdot \vec{F}}_{\text{EPFD}} + \underbrace{\bar{X}}_{\text{PGWD}}$$

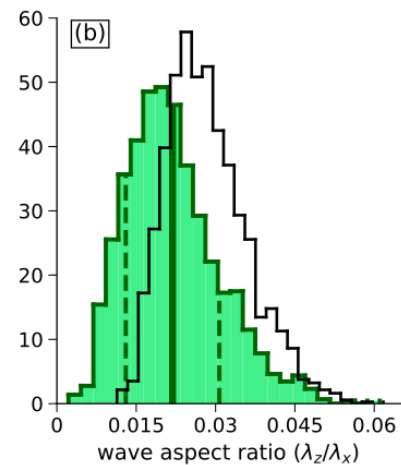
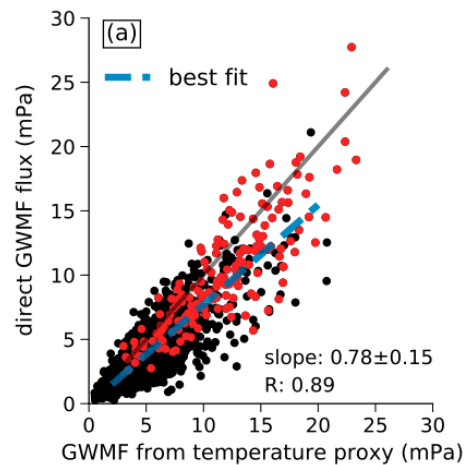
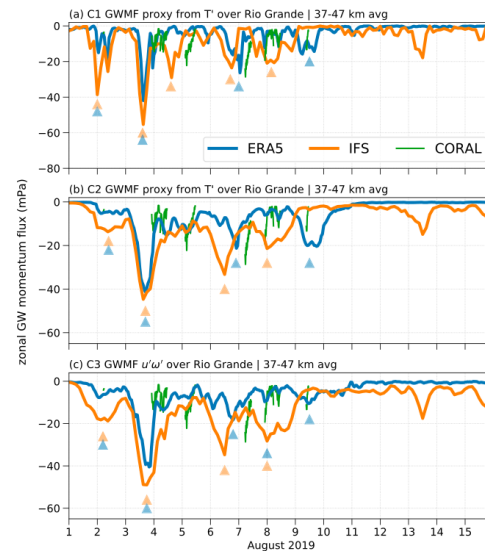
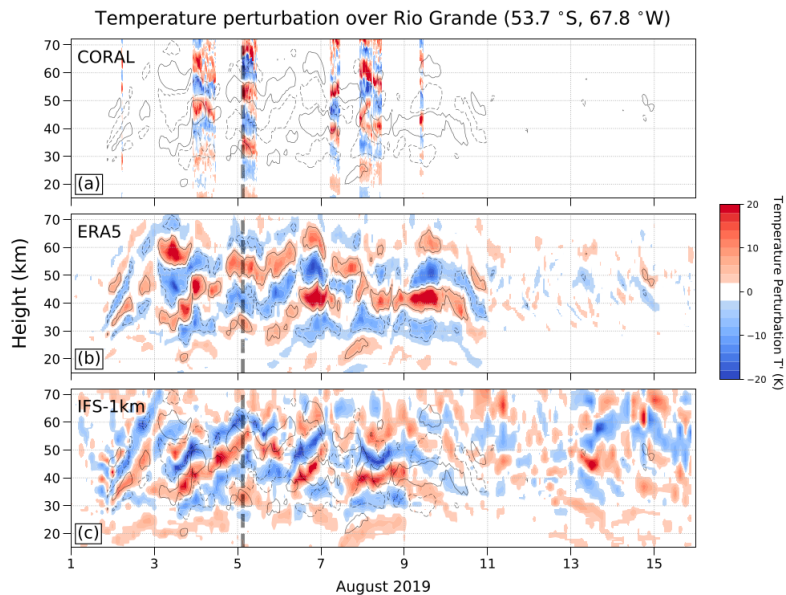


(f) VMFC ($k_x \geq 4$), 5 hPa

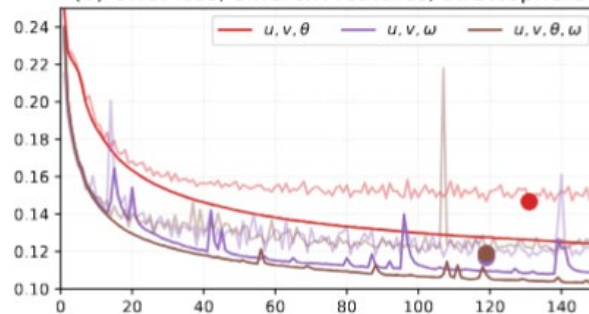


$$E_p = \frac{1}{2} \frac{g^2}{N^2} \overline{\left(\frac{T'}{T_0}\right)^2},$$

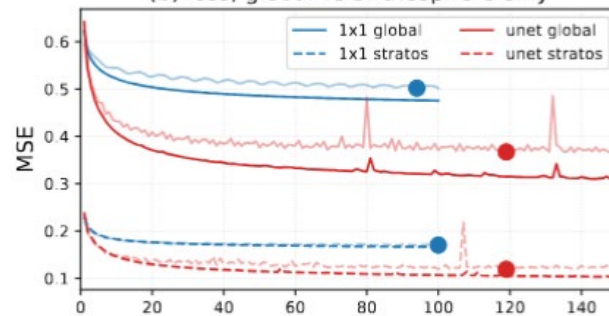
$$\mathbf{F} = g^{-1}(\overline{u' \omega'}, \overline{v' \omega'}).$$



(b) UNet loss, different features, stratosphere



(b) loss, global vs stratosphere only



(c) loss, diff. models, stratosphere, u, v, θ, ω

