

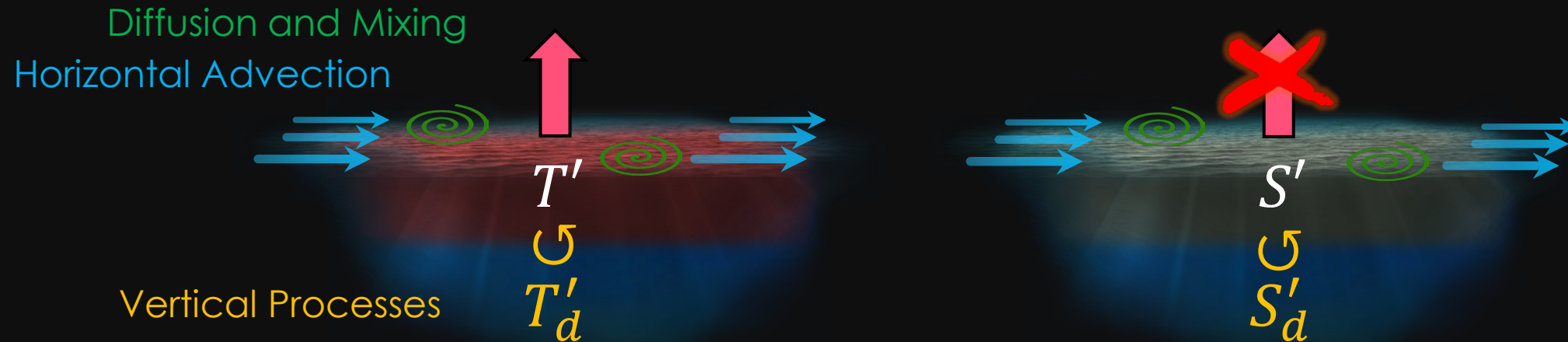
# Investigation of the drivers of sea surface salinity and North Atlantic climate variability using a stochastic model

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Climate Variability and Change Working Group

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# Salinity Variability and Ocean Dynamics



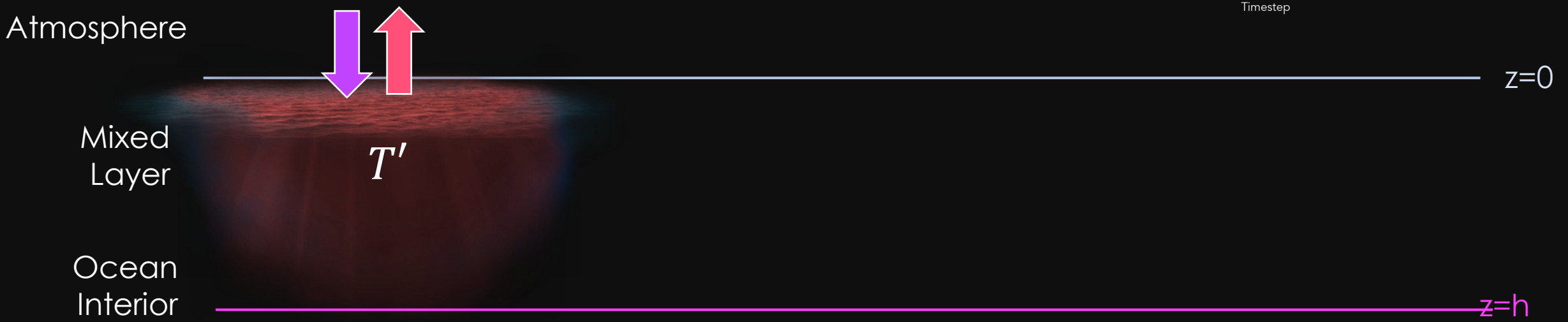
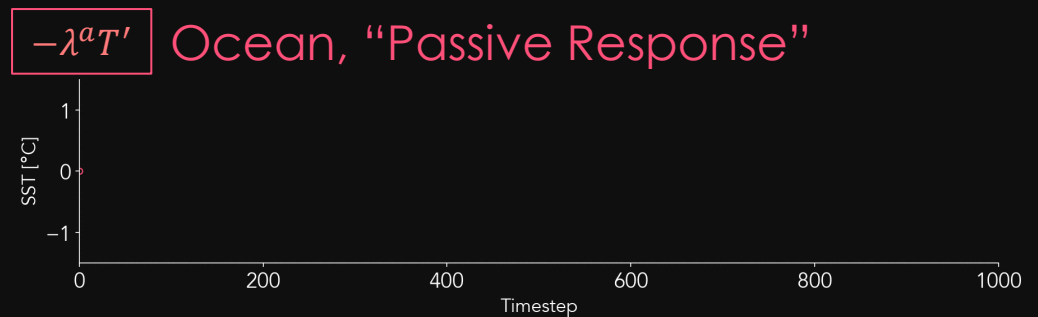
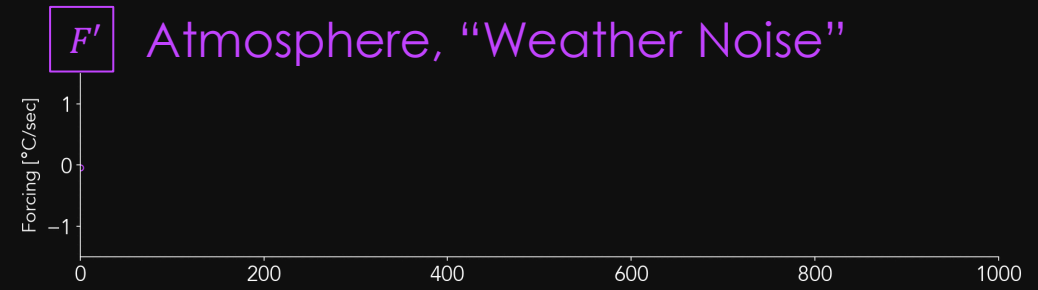
Q: *How do specific ocean processes impact salinity variability?*

*Can this tell us anything about North Atlantic Climate?*

# Stochastic Model Theory (Frankignoul and Hasselmann 1977)

$$\frac{\partial T'}{\partial t} = \frac{F'}{\rho C_p h} - \frac{\lambda^a}{\rho C_p h} T'$$

stochastic atmospheric forcing      heat flux damping



Winter (Year 1)

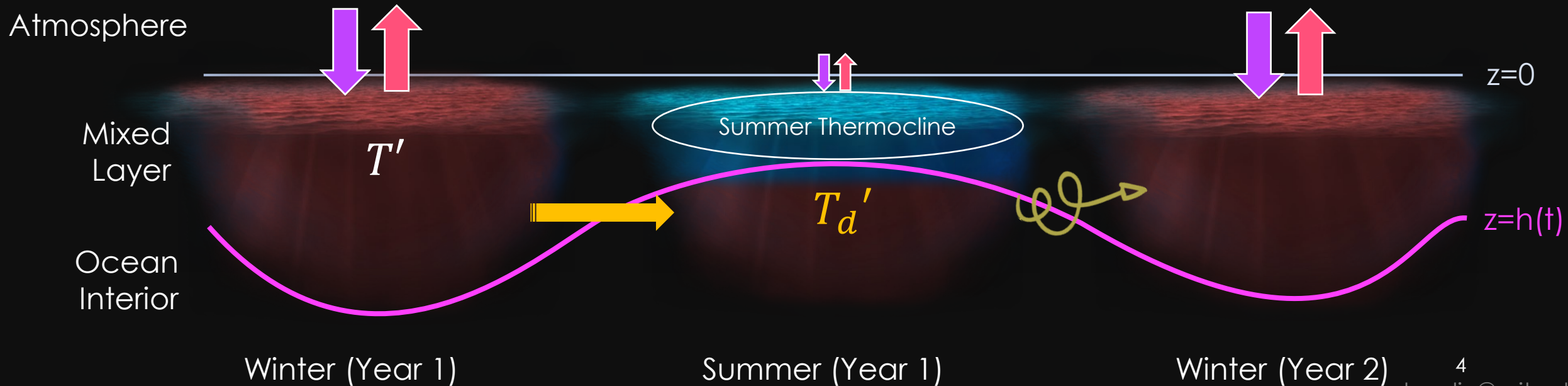
Summer (Year 1)

Winter (Year 2)

# Entrainment and Re-emergence

$$\frac{\partial T'}{\partial t} = \frac{F'}{\rho C_p h} - \frac{\lambda^a}{\rho C_p h} T' - \frac{1}{h} w_e (T' - T_d')$$

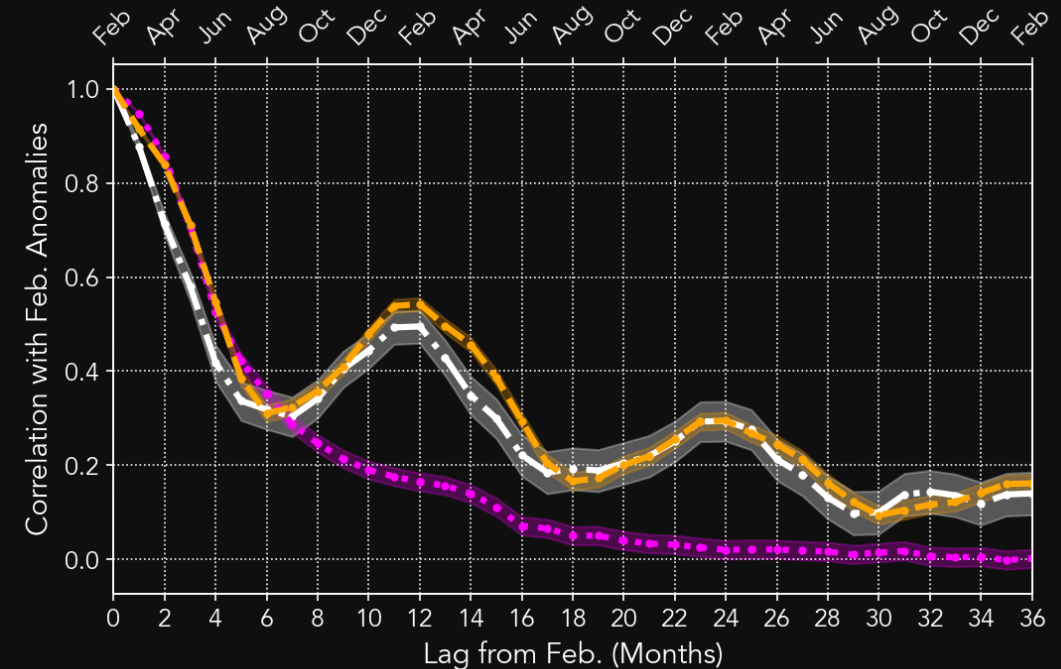
stochastic atmospheric forcing     heat flux damping     entrainment velocity     SST' below mixed layer



# Entrainment and Re-emergence

$$\frac{\partial T'}{\partial t} = \frac{\overset{\text{stochastic atmospheric forcing}}{F'}}{\rho C_p h} - \frac{\overset{\text{heat flux damping}}{\lambda^a}}{\rho C_p h} T' - \frac{\overset{\text{entrainment velocity}}{1}}{h} w_e (T' - \overset{\text{SST' below mixed layer}}{T_d'})$$

The **entraining stochastic model** successfully captured aspects of SST behavior at key locations in the **Community Earth System Model 1** (Liu et al. 2023)

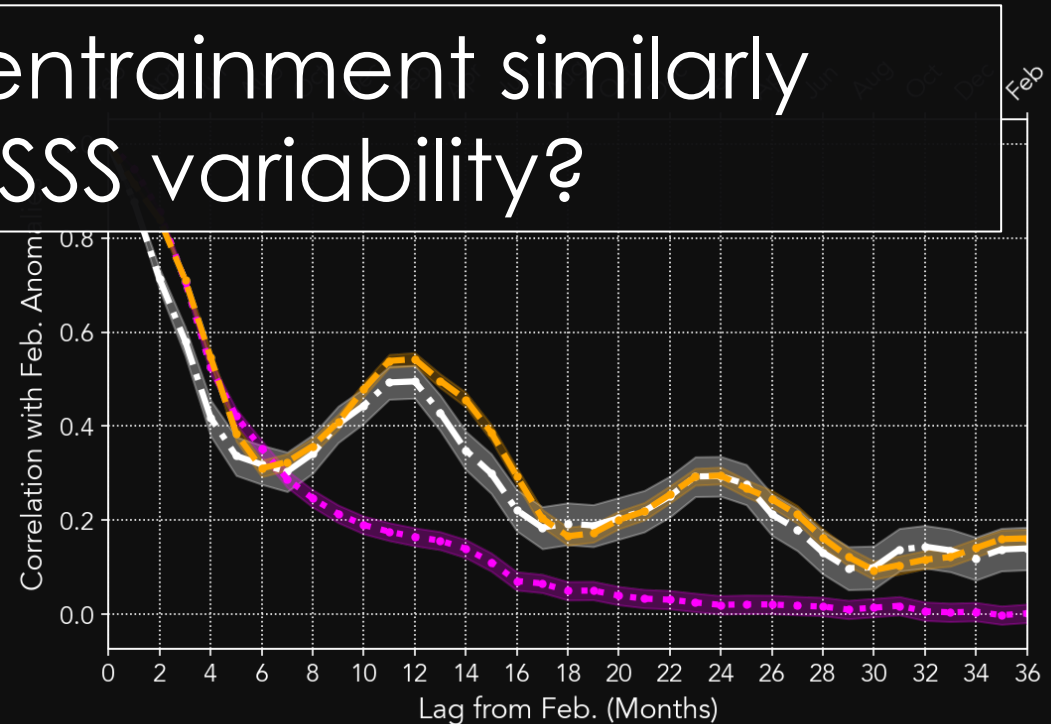


# Entrainment and Re-emergence

$$\frac{\partial T'}{\partial t} = \frac{\overset{\text{stochastic atmospheric forcing}}{F'}}{\rho C_p h} - \frac{\overset{\text{heat flux damping}}{\lambda^a}}{\rho C_p h} T' - \frac{\overset{\text{entrainment velocity}}{1}}{h} w_e (T' - \overset{\text{SST' below mixed layer}}{T_d'})$$

Q: Is local vertical entrainment similarly important for SSS variability?

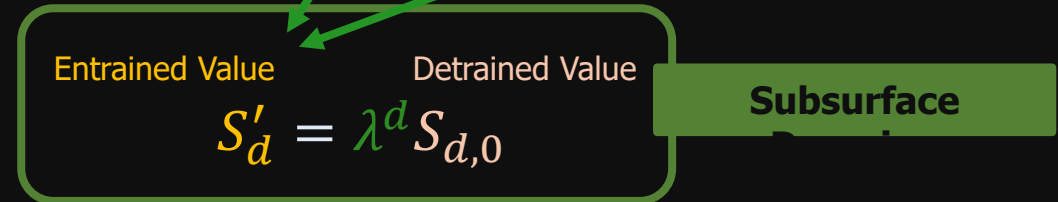
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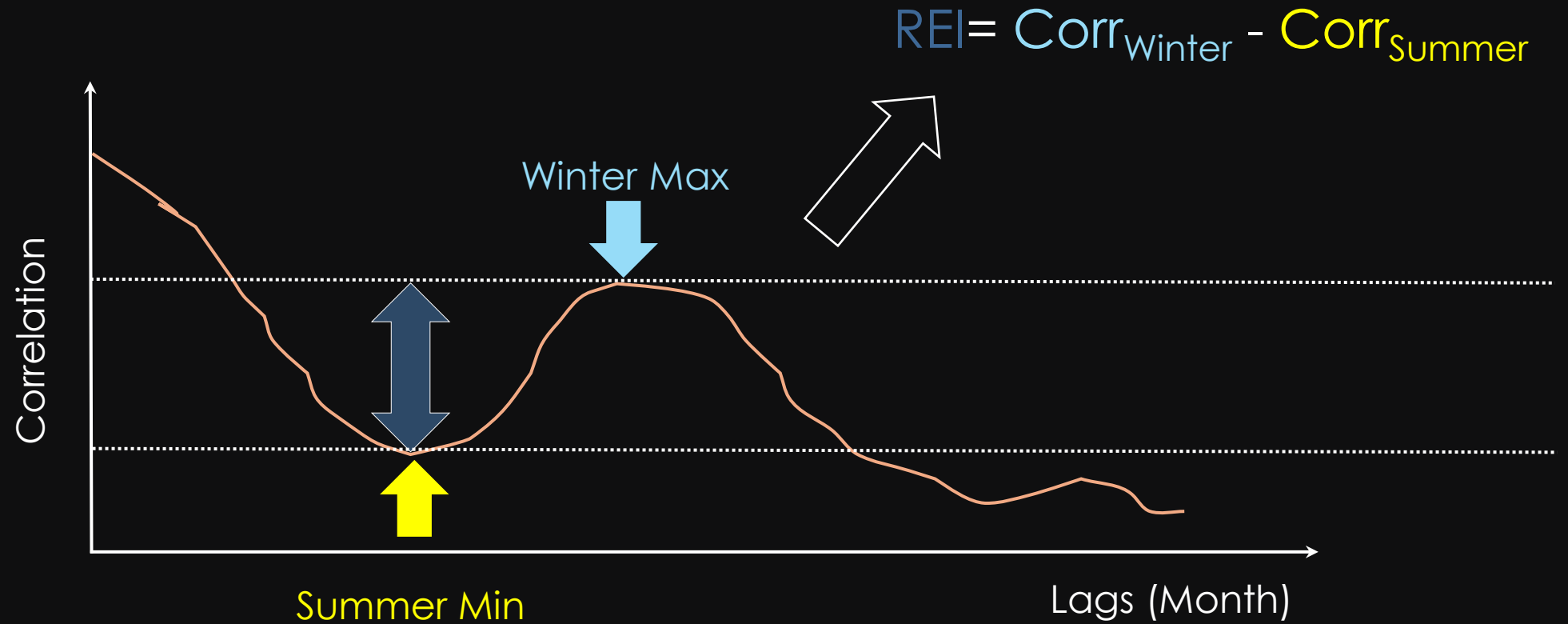
$$\frac{\partial T'}{\partial t} = \frac{\overset{\text{stochastic atmospheric forcing}}{F'}}{\rho C_p h} - \frac{\overset{\text{heat flux damping}}{\lambda^a}}{\rho C_p h} T' - \frac{1}{h} w_e (T' - \overset{\text{SST' below mixed layer}}{T_d'})$$

$$\frac{\partial S'}{\partial t} = \frac{\overset{\text{Stochastic evaporation and precipitation}}{\bar{S}(E' - P')}}{\rho h} - \frac{1}{h} w_e (S' - S_d')$$



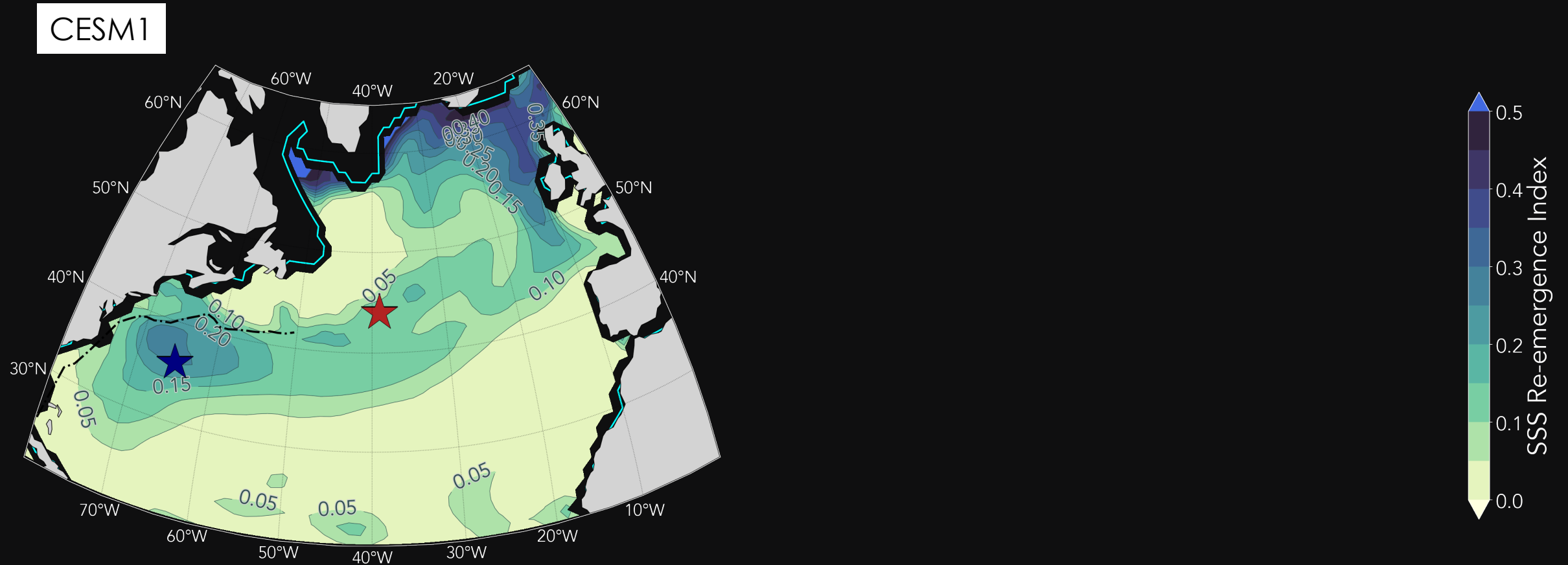
Estimate parameters and compare with the 42-member CESM1 Large Ensemble, 1920-2005

## Re-emergence and Persistence



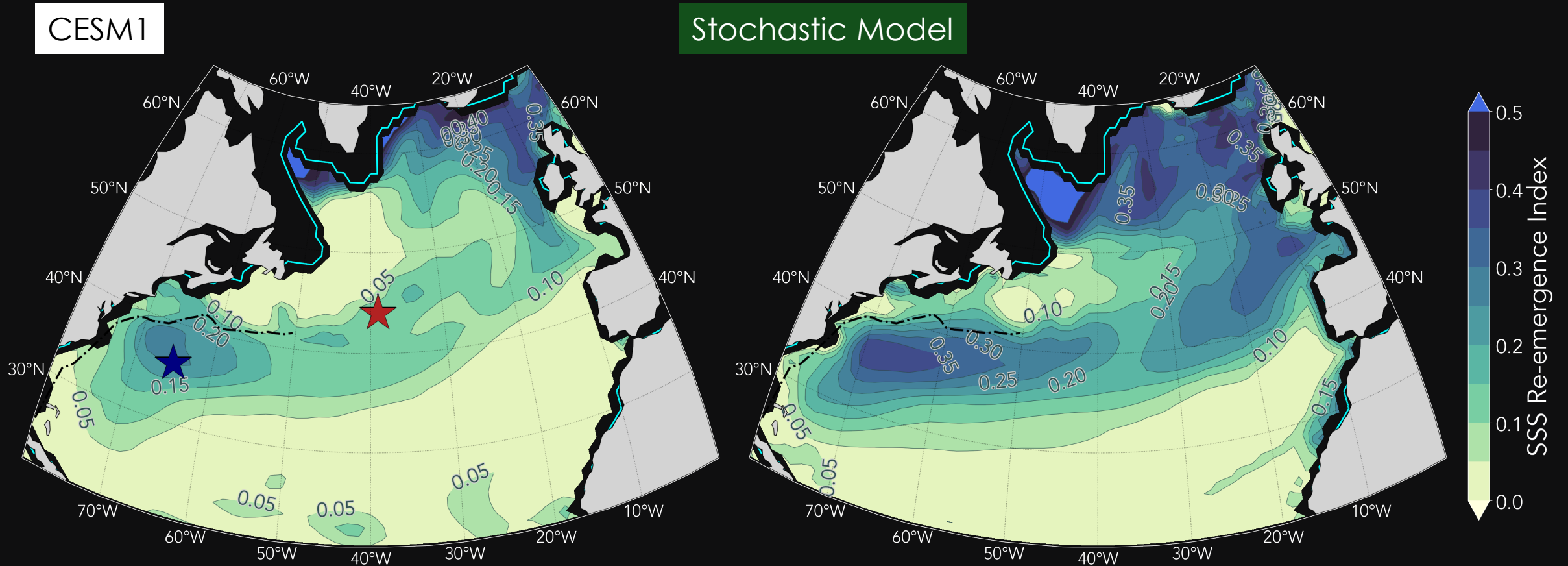


# SSS Re-emergence patterns in CESM1



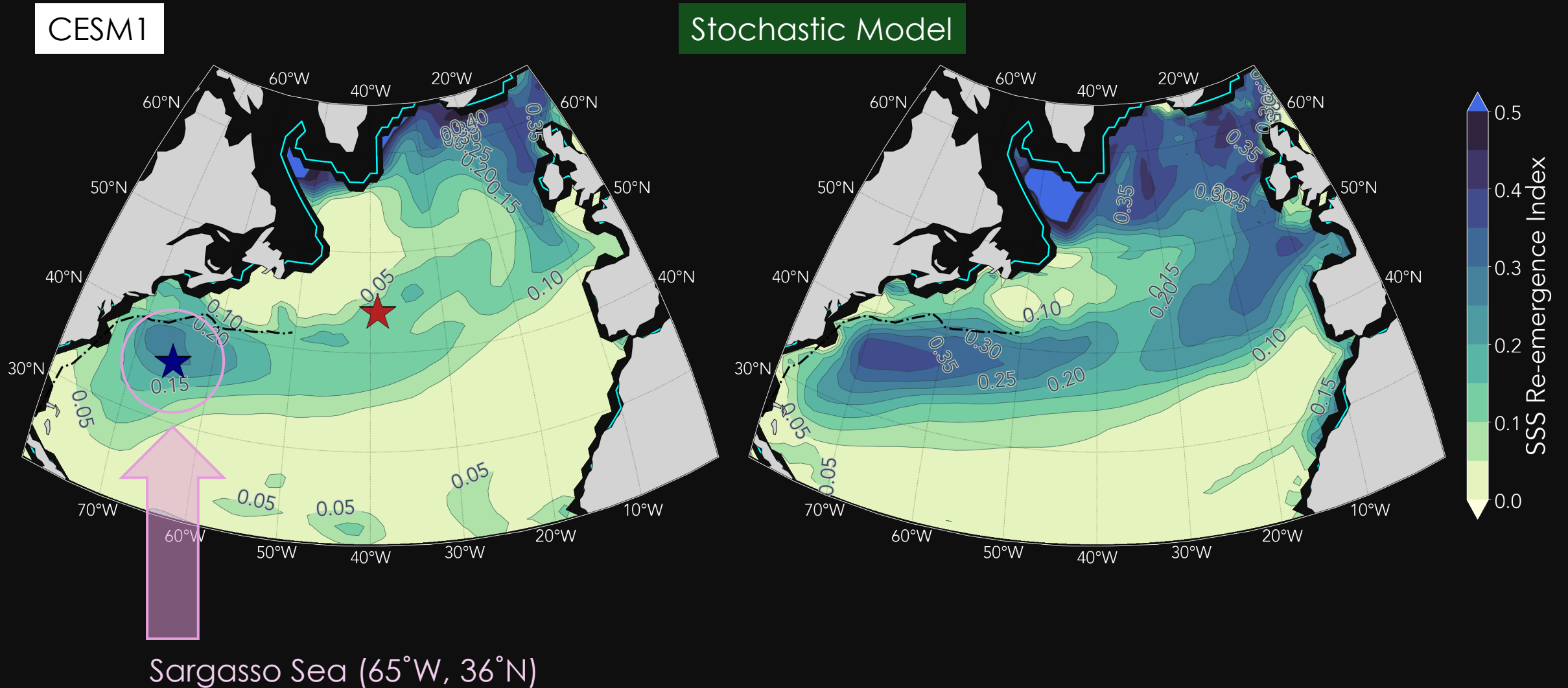
We then integrate the stochastic model for 10,000 years at each point in the North Atlantic...

# SSS Re-emergence patterns in CESM1

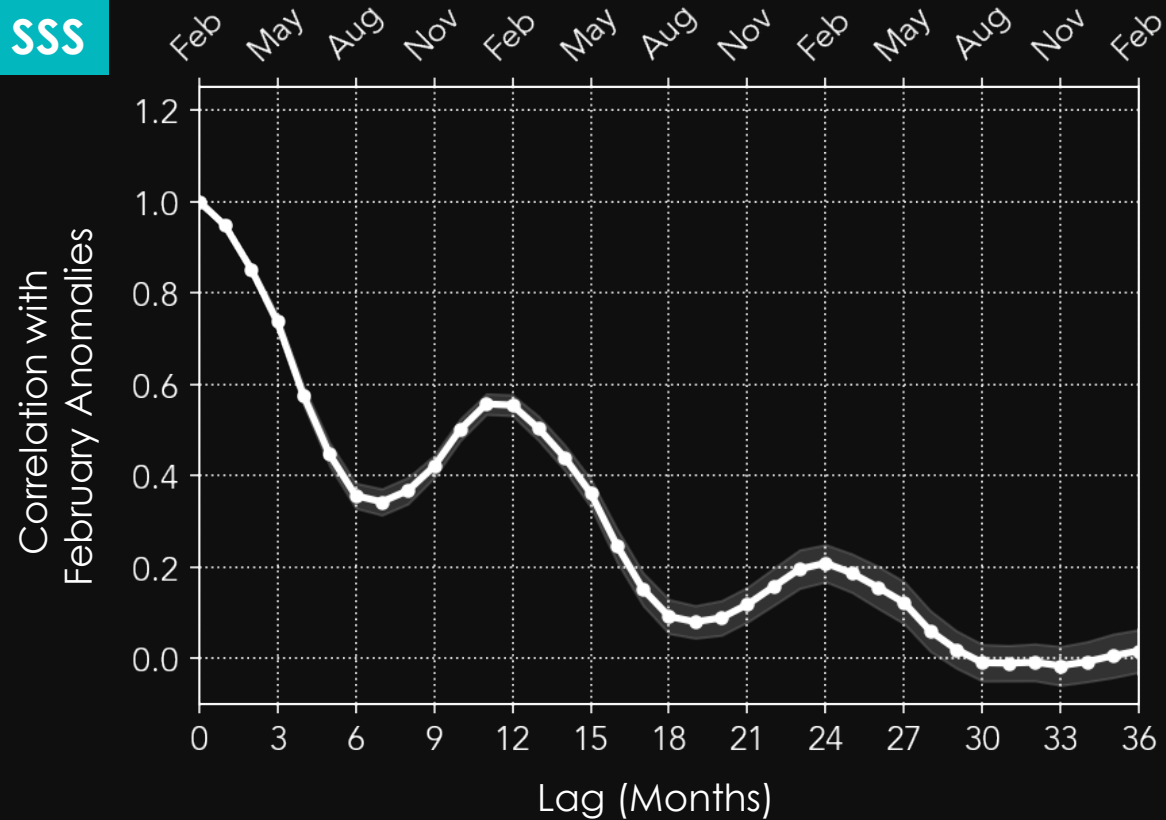


Even without horizontal dynamics, the stochastic model captures the **amplitude and pattern** of wintertime SSS re-emergence

# SSS Re-emergence patterns in CESM1

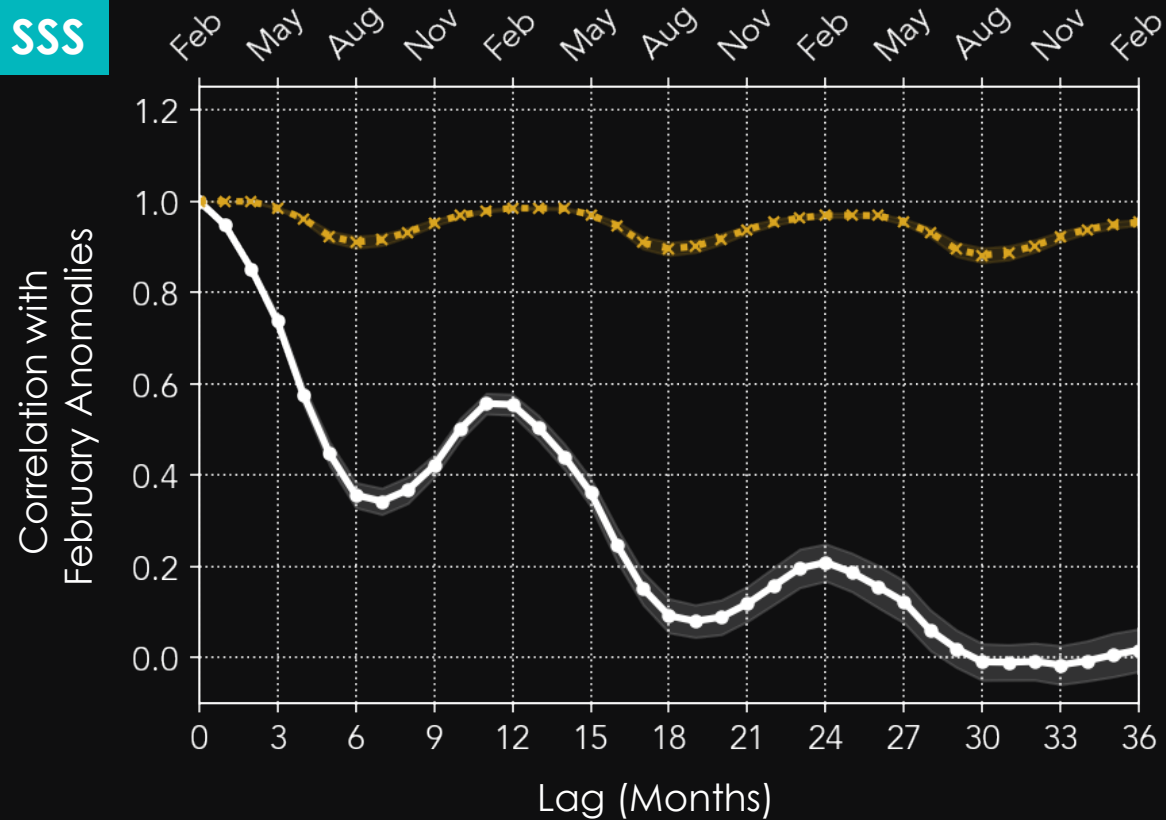


# Wintertime SSS Persistence

**SSS**

—●— CSM1

# Wintertime SSS Persistence

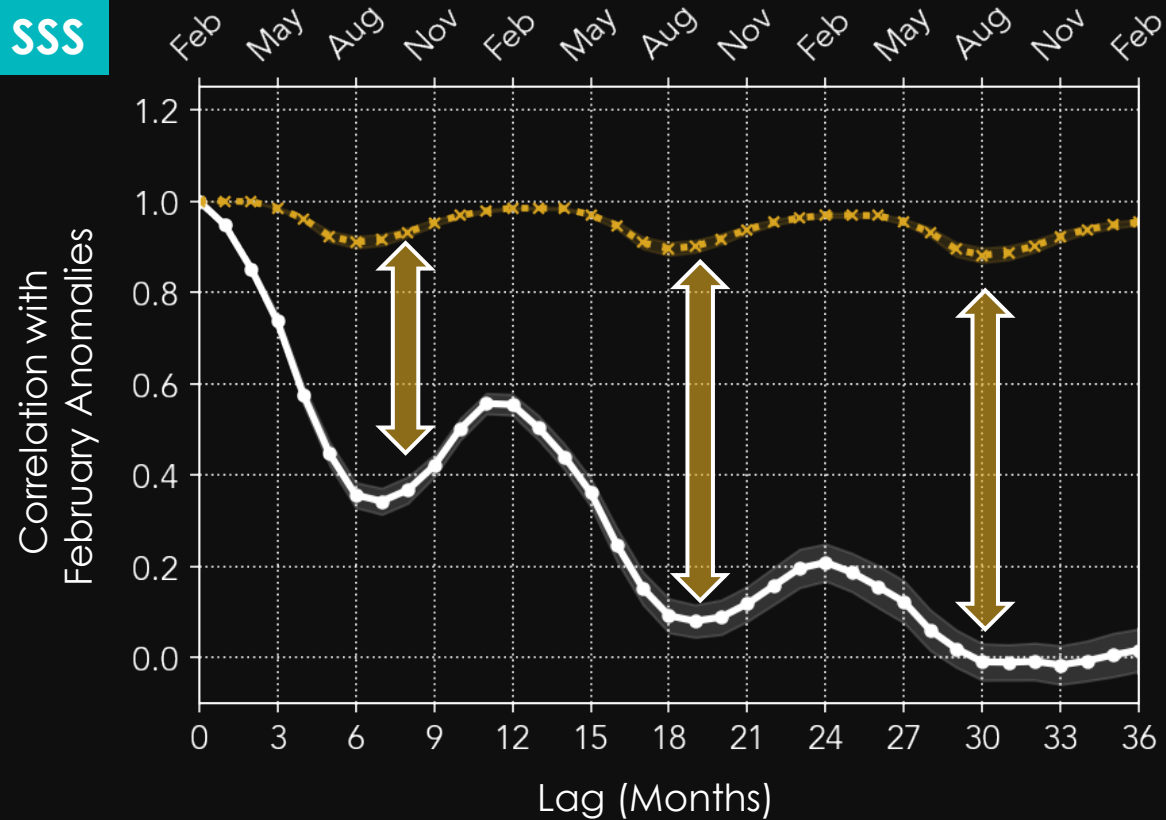
**SSS**

—●— CESM1  
—×— Stochastic Model

# Wintertime SSS Persistence

—●— CSM1  
—×— Stochastic Model

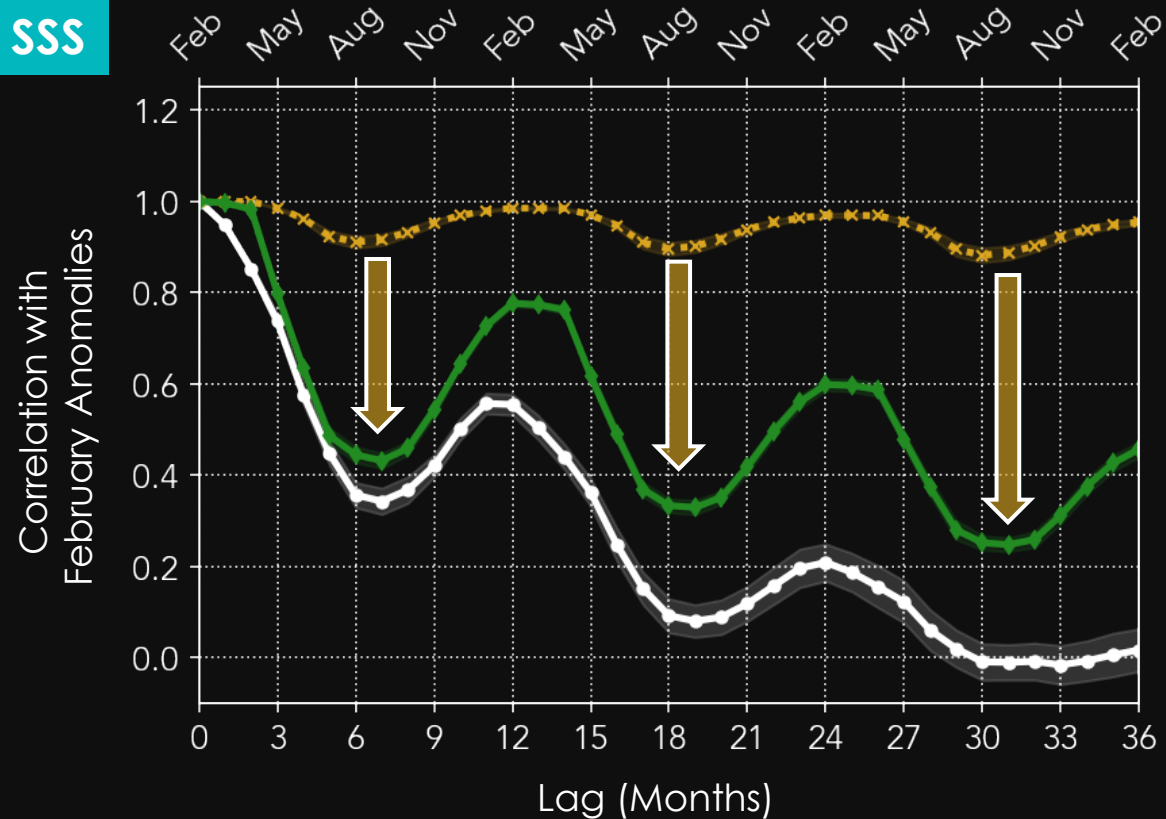
SSS



With **entrainment damping** alone, SSS is too persistent

# Wintertime SSS Persistence

SSS

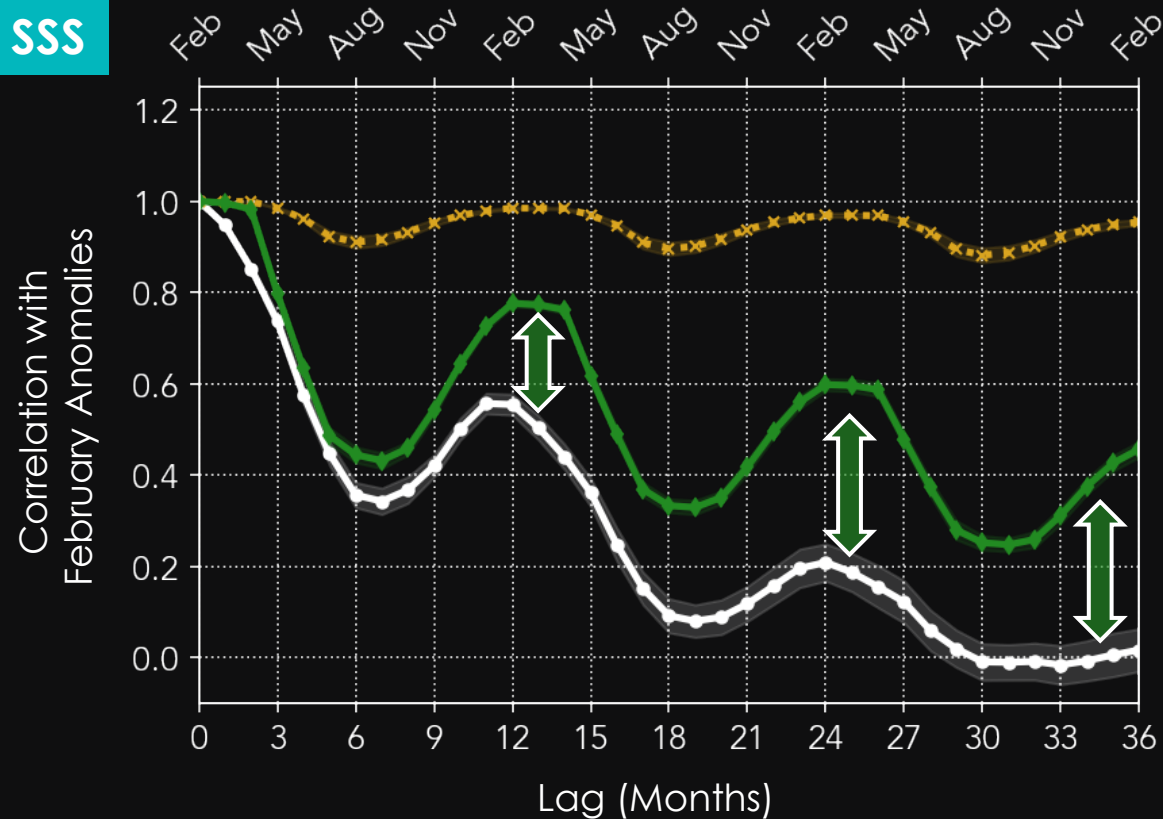


Addition of **subsurface damping** substantially improves representation of SSS persistence



# Wintertime SSS Persistence

SSS

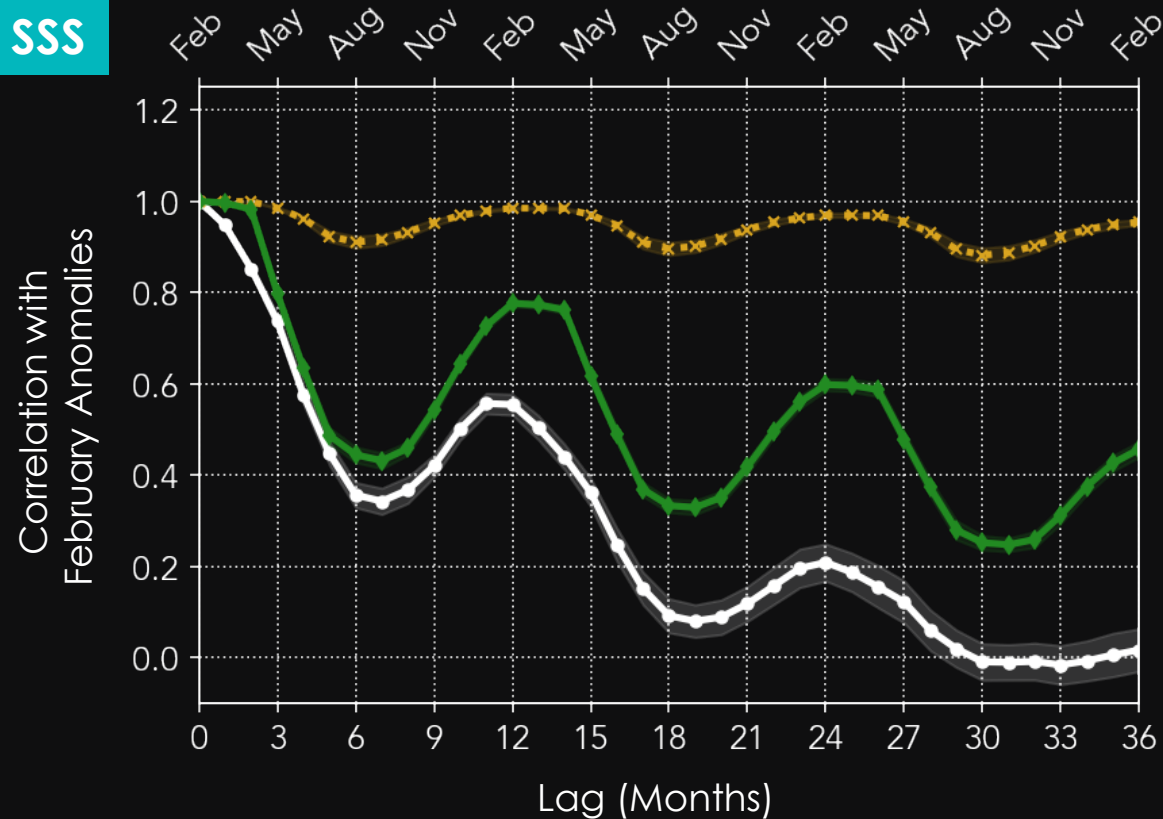


- CESM1
- x— Stochastic Model
- ◆— Stochastic Model (Subsurface Damping)

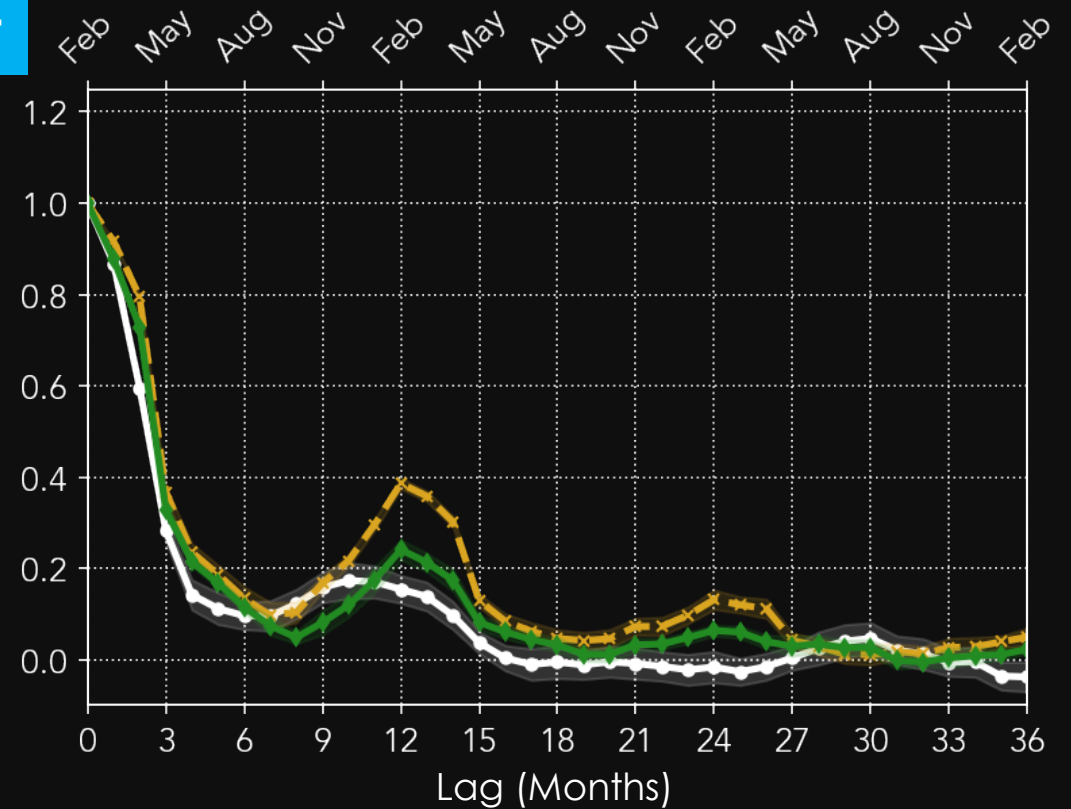
However, missing horizontal/vertical ocean dynamics are needed to correctly capture SSS persistence on longer timescales

## SSS versus SST Persistence

SSS



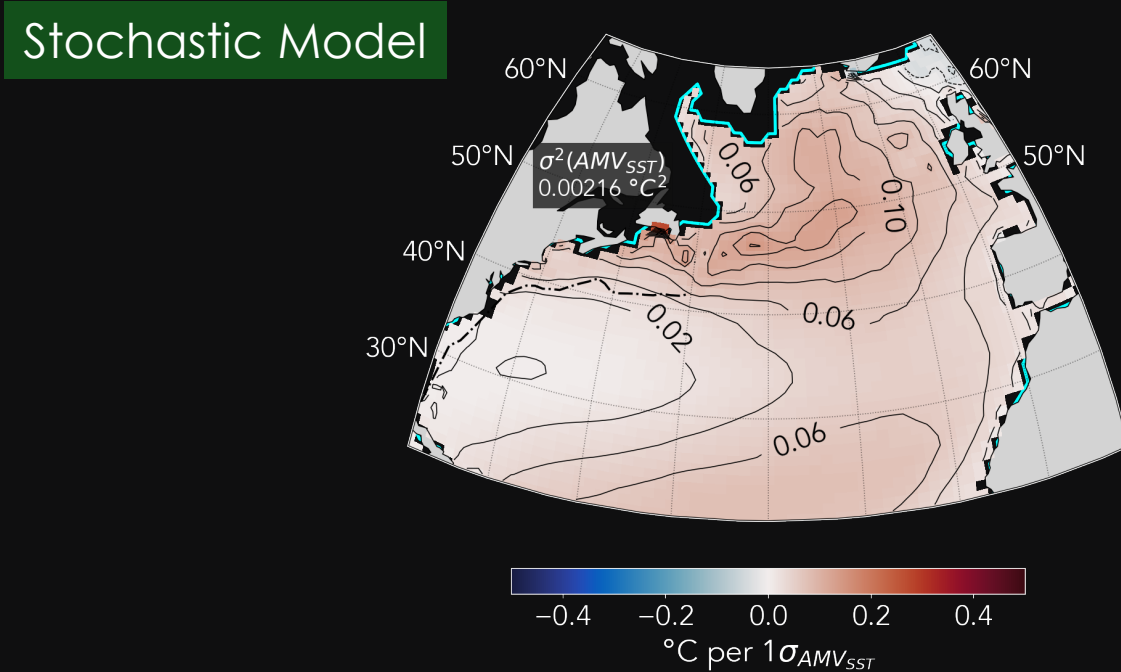
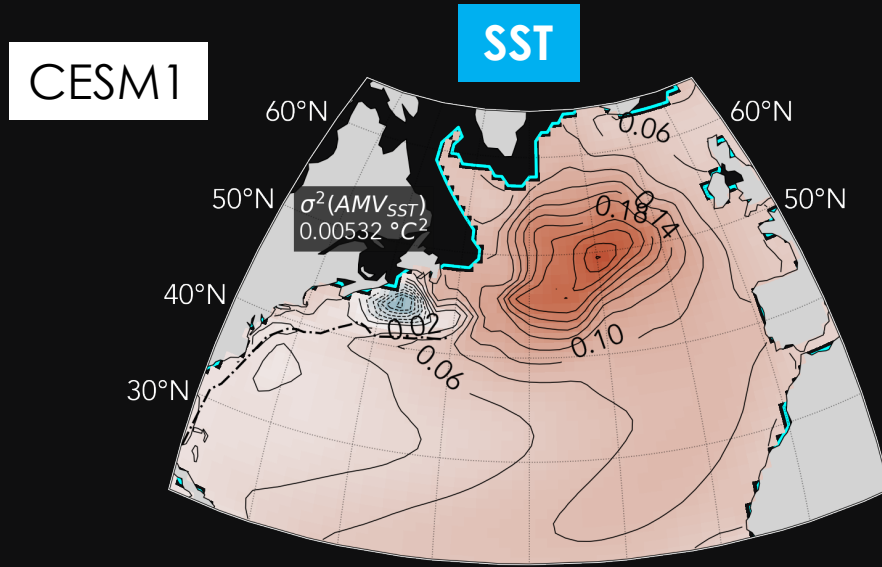
SST



Unlike SSS, **SST persistence is well captured** by the stochastic model *without* additional horizontal or vertical ocean dynamics beyond entrainment

# Patterns of Multidecadal Variability

The stochastic model SST has only **~40%** of the variance of CESM1

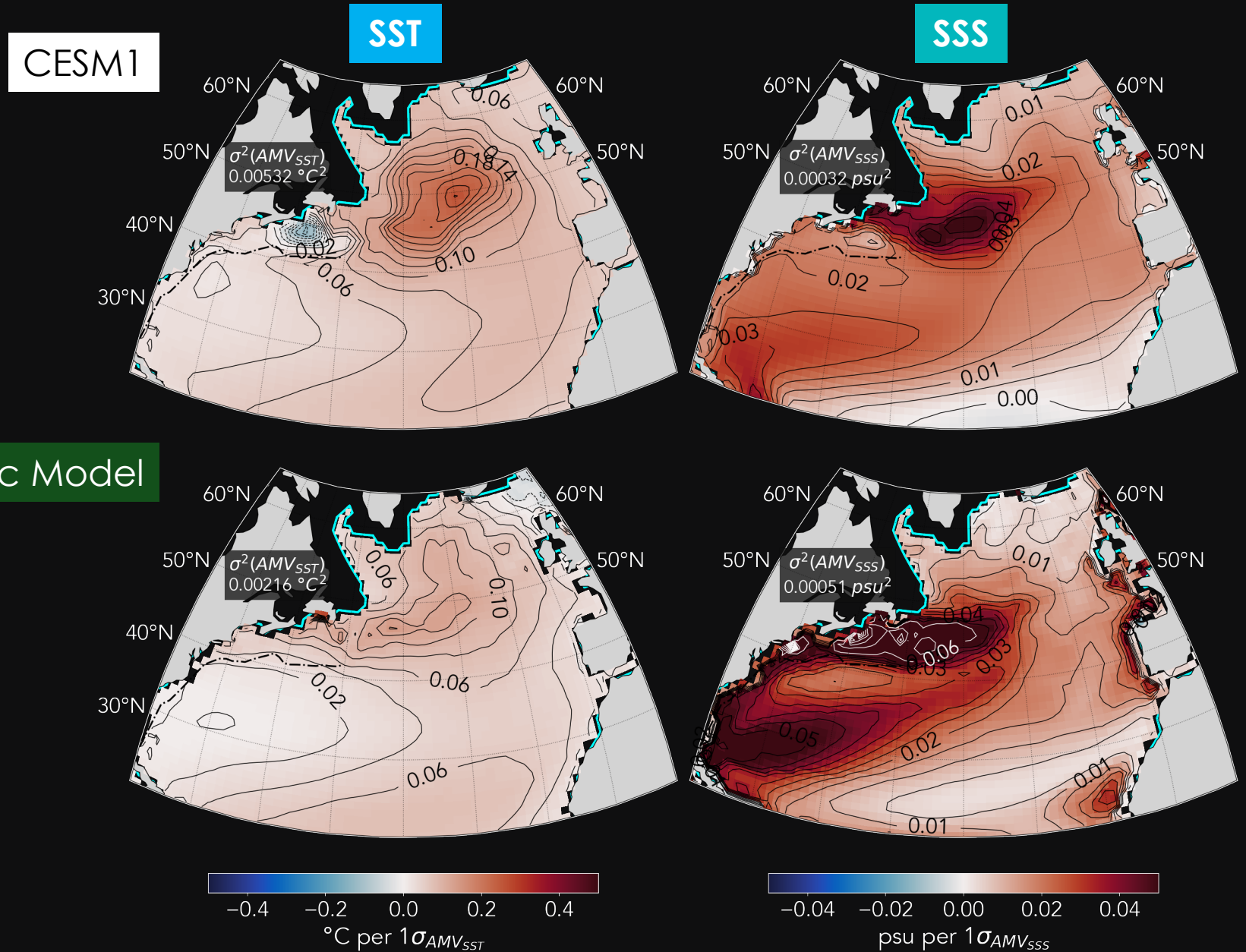


# Patterns of Multidecadal Variability

The stochastic model SST has only **~40%** of the variance of CESM1

## Stochastic Model

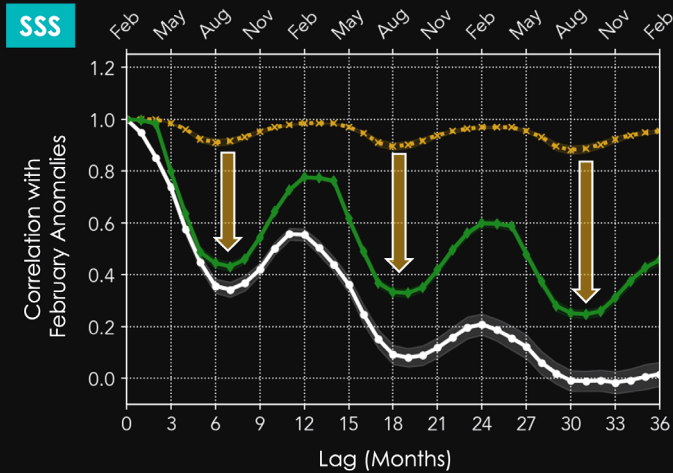
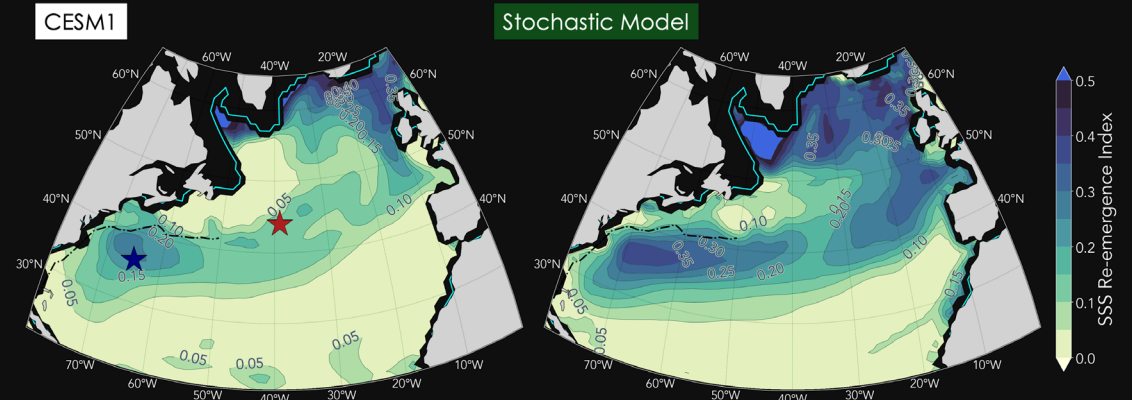
SSS in the stochastic model has **~1.6x** the variance of CESM1





# Main Takeaways

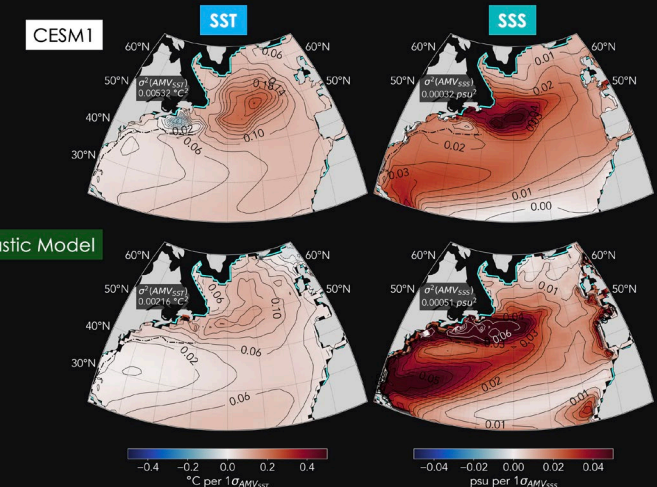
A stochastic model with vertical entrainment captures SSS persistence and its seasonal progression



Subsurface damping improves representation of SST/SSS behavior especially for SSS persistence

Ocean processes impact SST and SSS differently

- Damping SSS persistence and low-frequency variance
- Enhancing low-frequency SST



Thanks for Listening! Questions? ([glennliu@mit.edu](mailto:glennliu@mit.edu))