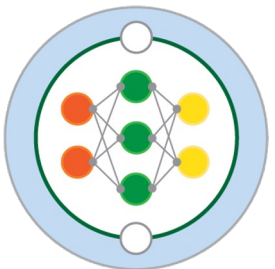
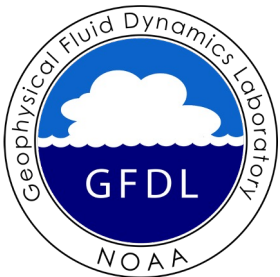


Learning Ocean Model Errors from Data Assimilation Increments

Tarun Verma, Feiyu Lu, Alistair Adcroft

02/09/2023

CESM Ocean Working Group Meeting



Bias: a persistent problem in climate modeling



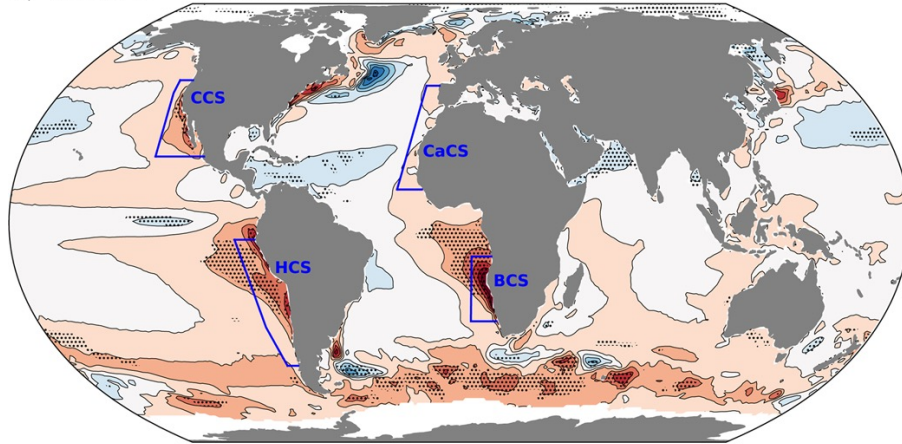
Multi-model Mean SST Bias (Farneti et al. 2022)

High-res MIP (1.78° C)

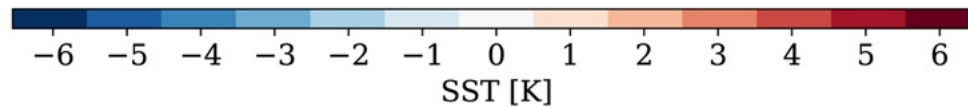
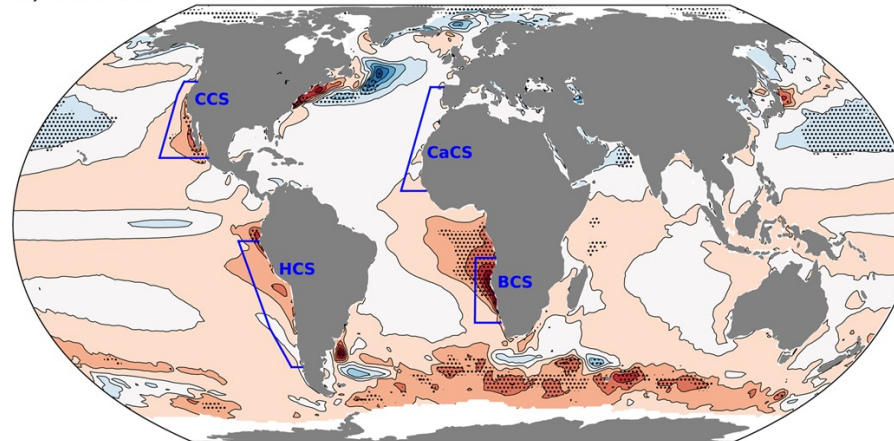
CMIP5 (3.25° C)

CMIP6 (2.78° C)

a) CMIP5 SETA SST bias mean = 3.24° C, max = 7.61° C



b) CMIP6 SETA SST bias mean = 2.78° C, max = 6.45° C



Ocean MIP2 (1.14° C)



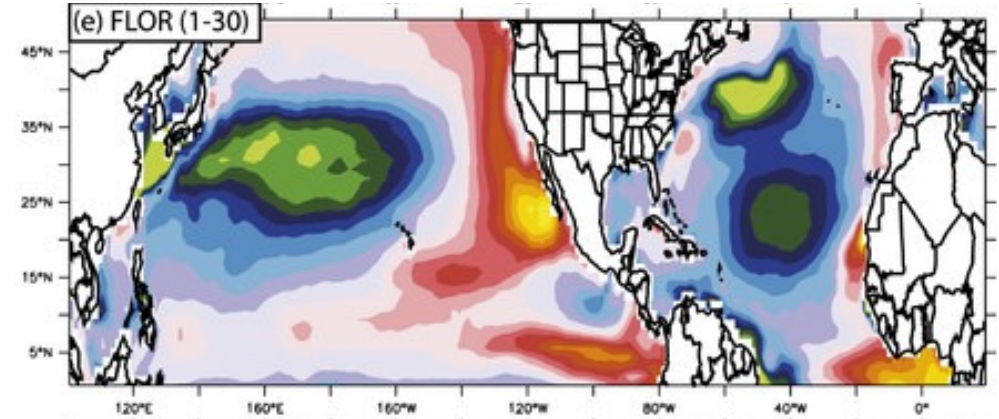
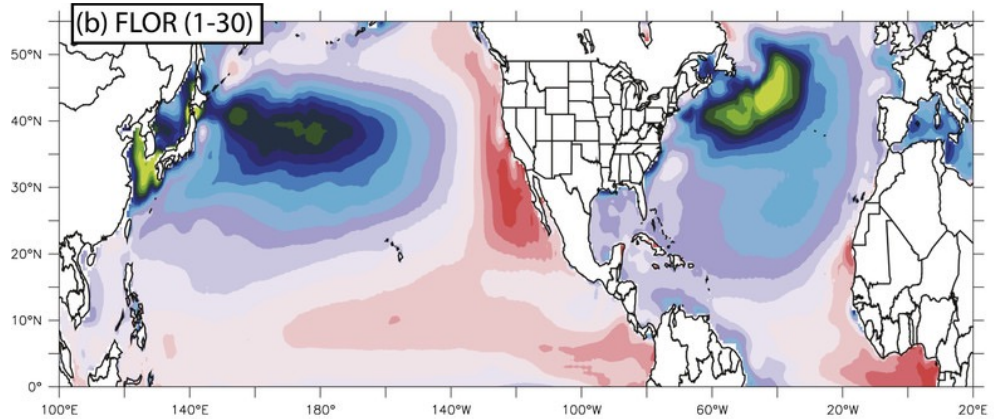
SST bias affects many other important phenomena, e.g., Tropical Cyclones (TC)

Reduction in SST bias improves TC activity
(Vecchi et al. 2014)

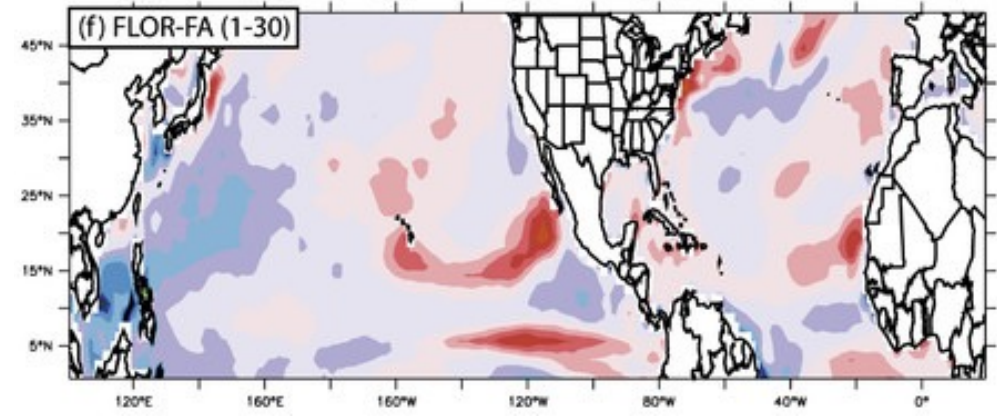
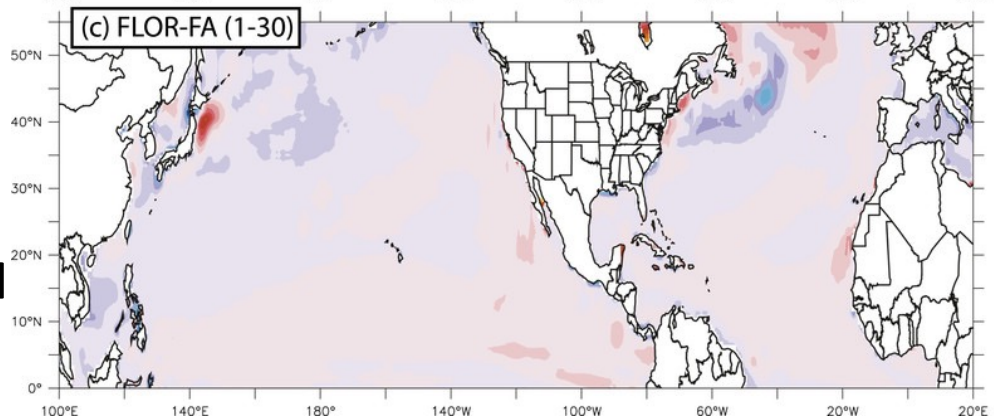
SST bias

TC Potential Intensity

Control



Flux-adjusted

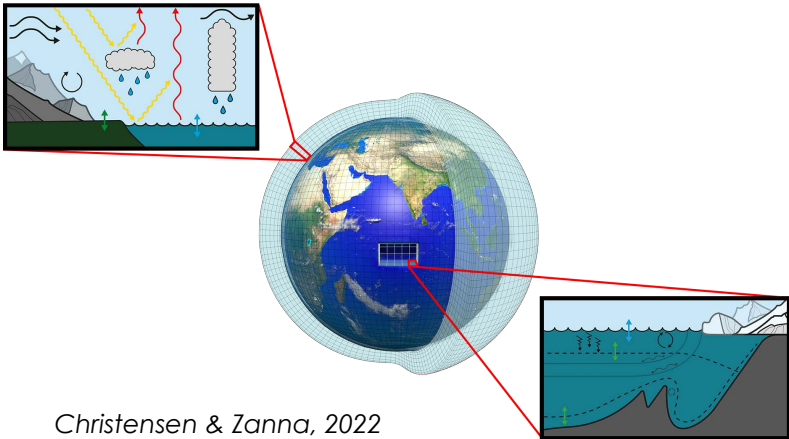




Part of the bias stems from fast physics errors

Model error

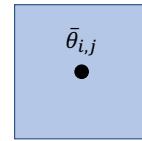
➔ Poor or lacking representation of key processes



Christensen & Zanna, 2022

➔ Numerics

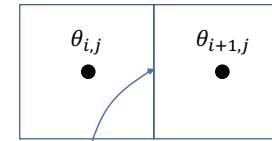
a) Finite volume



$$V_{i,j} \frac{\partial \bar{\theta}_{i,j}}{\partial t} = \oint \kappa \nabla \theta \cdot dA$$

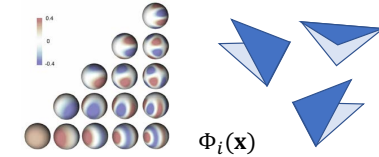
truncate the functional operators

b) Finite difference



$$\frac{\partial \theta}{\partial x} \approx \frac{\theta_{i+1,j} - \theta_{i,j}}{\Delta x}$$

c) Spectral or finite element



$$\theta(\mathbf{x}) = \sum_{i=1}^n A_i \Phi_i$$

$$\frac{\partial}{\partial t} \int W \theta dV = \int \kappa \nabla \theta \cdot \nabla W dV$$

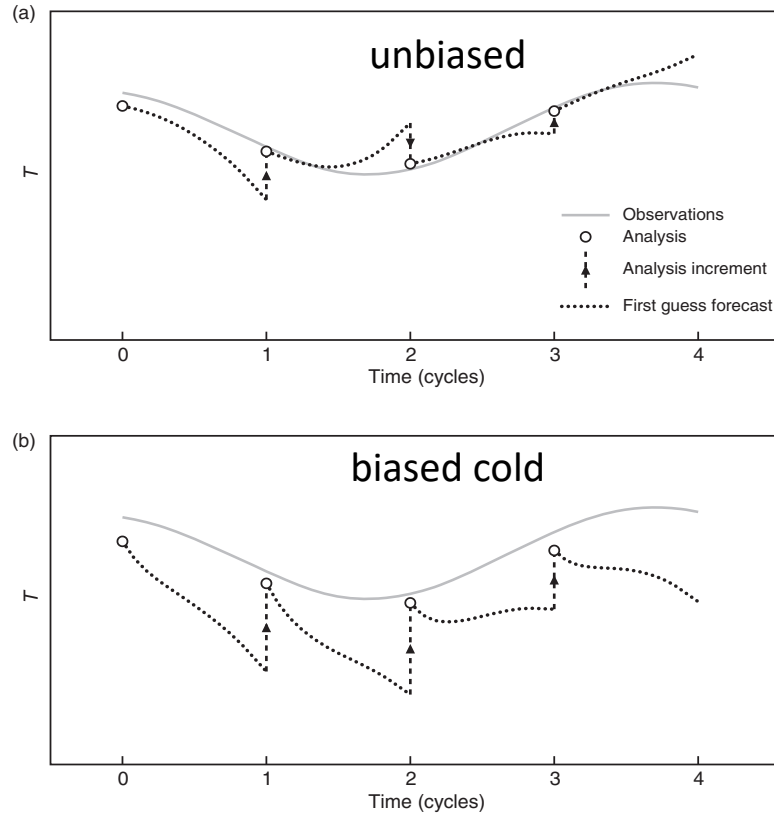
truncate the functional space

- Missing or inaccurate physics,
 - vertical mixing, sub-meso-mesoscale eddies etc.
- Numerics.

Here we propose to **(machine) learn ocean model corrections** at these fine-scales using **data assimilation increments**.

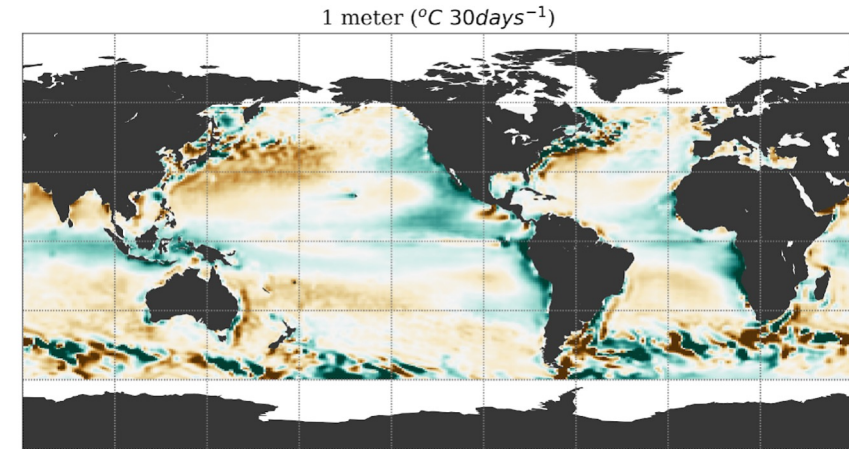


Palmer and Weisheimer 2011

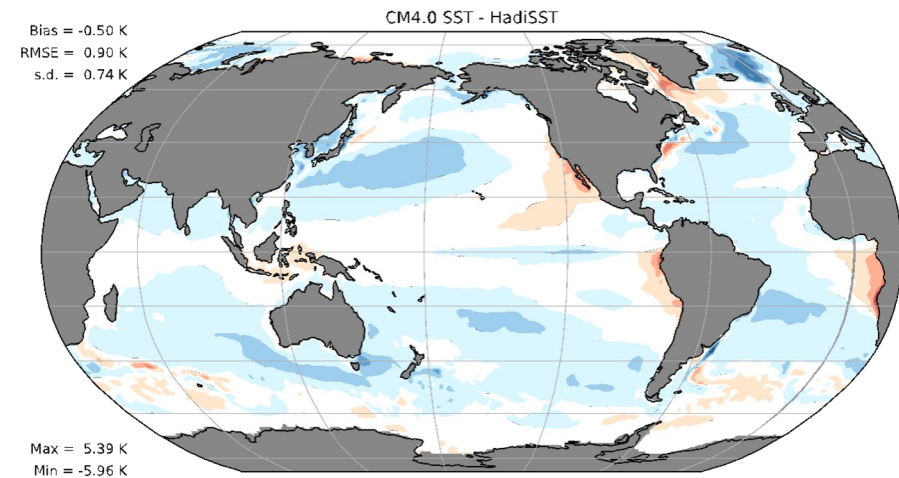


- a) DA corrects random errors.
 - b) DA corrects systematic errors.
- Learning corrections = Learning Increments

Mean Increments in GFDL SPEAR



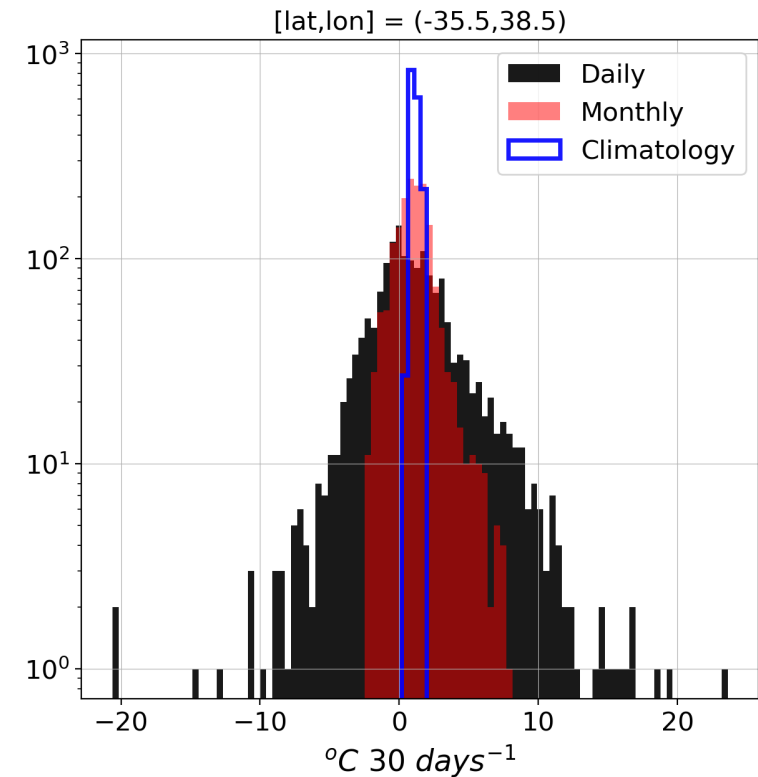
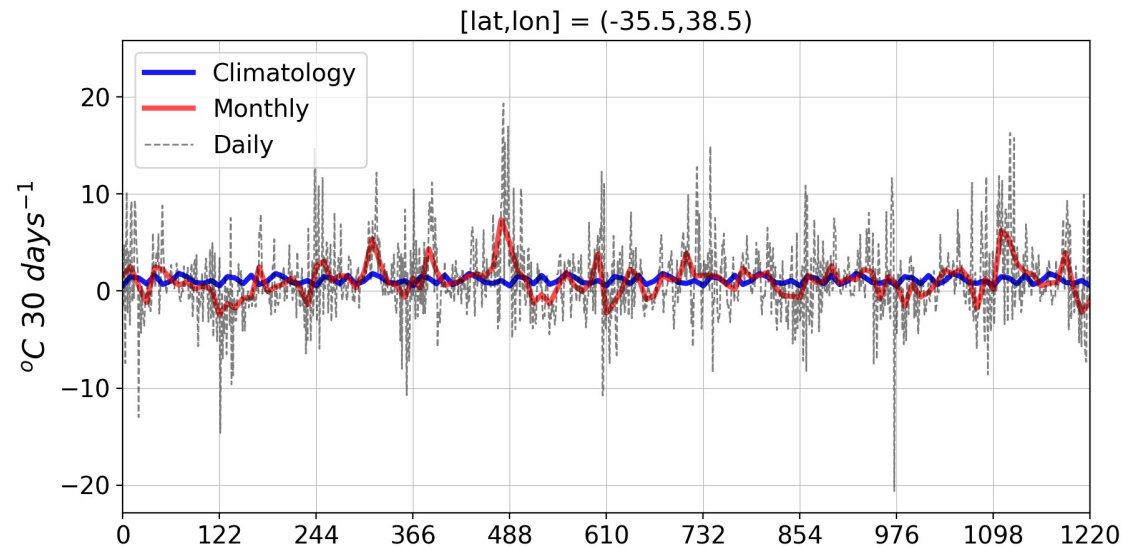
Mean SST Bias in CM4.0



Held et al. 2019



Learn high frequency or low frequency increments?



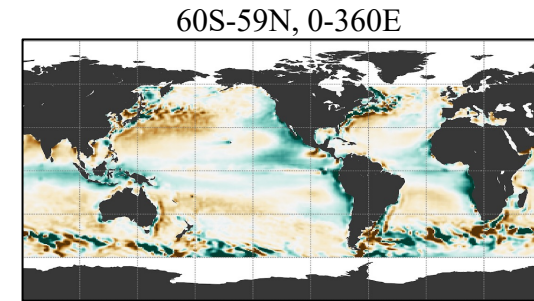
- $X_{t,s}$ is a daily DA increment with t and s indices representing time and space.
- $\langle X_{t,s} \rangle^{d,m,c}$ is a smoothing (or high frequency filtering) operation with daily, monthly or climatological timescales

- Loss function for the neural network can then be written as
$$\mathbf{E} \left[\left(\hat{X}_{t,s} - \langle X_{t,s} \rangle^{d,m,c} \right)^2 \right]$$

Use Neural Nets to learn nonlinear mapping from model state to DA increments

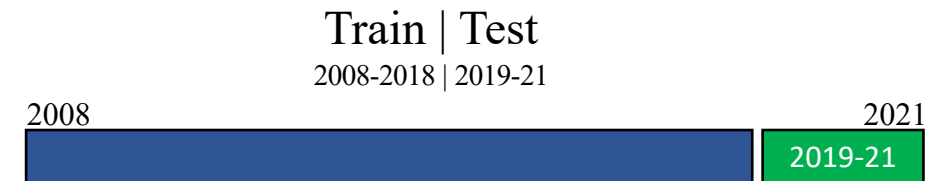


- ✓ **Goal:** local, state-dependent (\sim parameterization)
- ✓ **Inputs:** daily T , T_z , U_z , V_z , h_{fds} , τ_{aux} , τ_{y} etc.
- ✓ **Output:**
 - 1) daily climatology of temperature increments
 - 2) raw daily temperature increments
- ✓ **Architecture:** Fully connected neural network
(2h32 to 5h256)



- ✓ near-global domain
- ✓ sub-sampled to $\sim 2^\circ$ horizontally
- ✓ coarsened to 19 levels in vertical
- ✓ sub-sampled every 3rd day

- ✓ Using **GFDL SPEAR DA system** which assimilates SST, ARGO observations
- ✓ 2004-2021



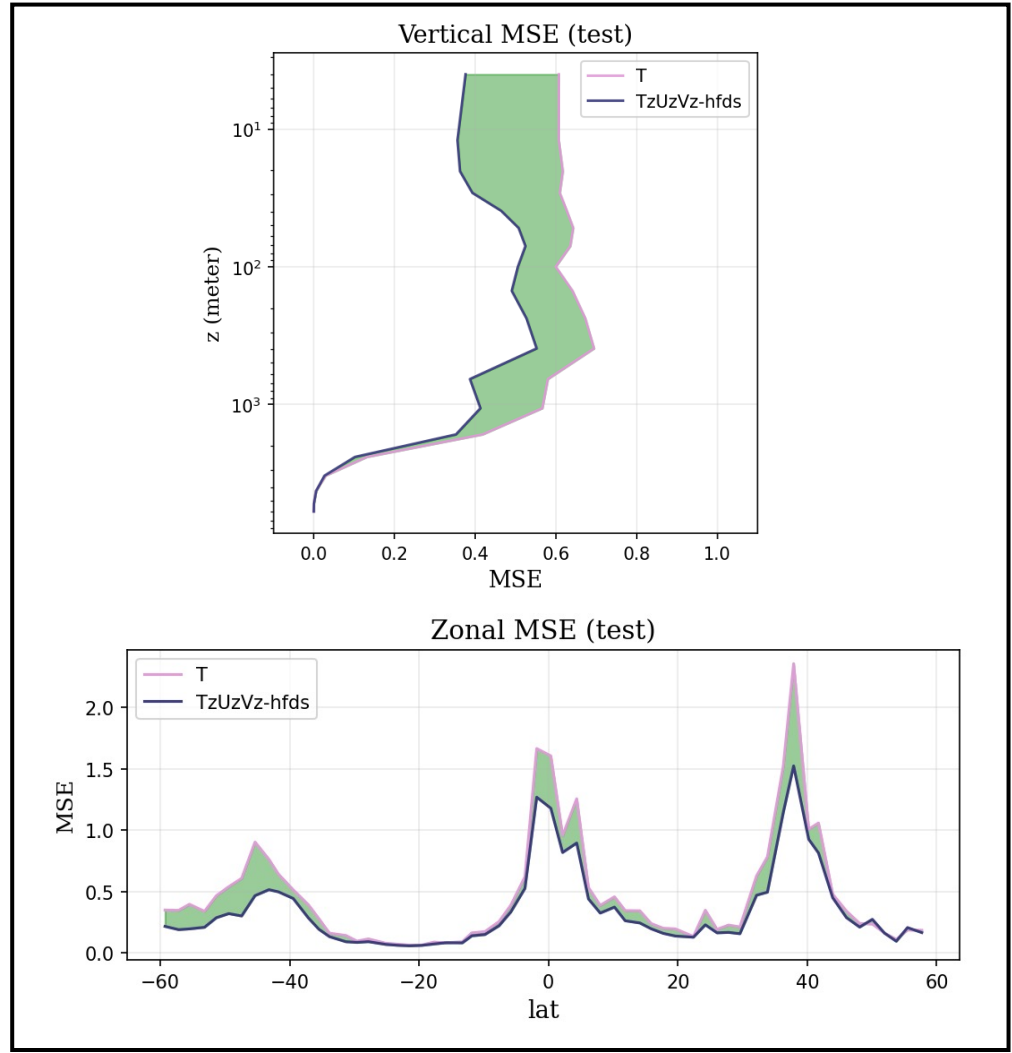
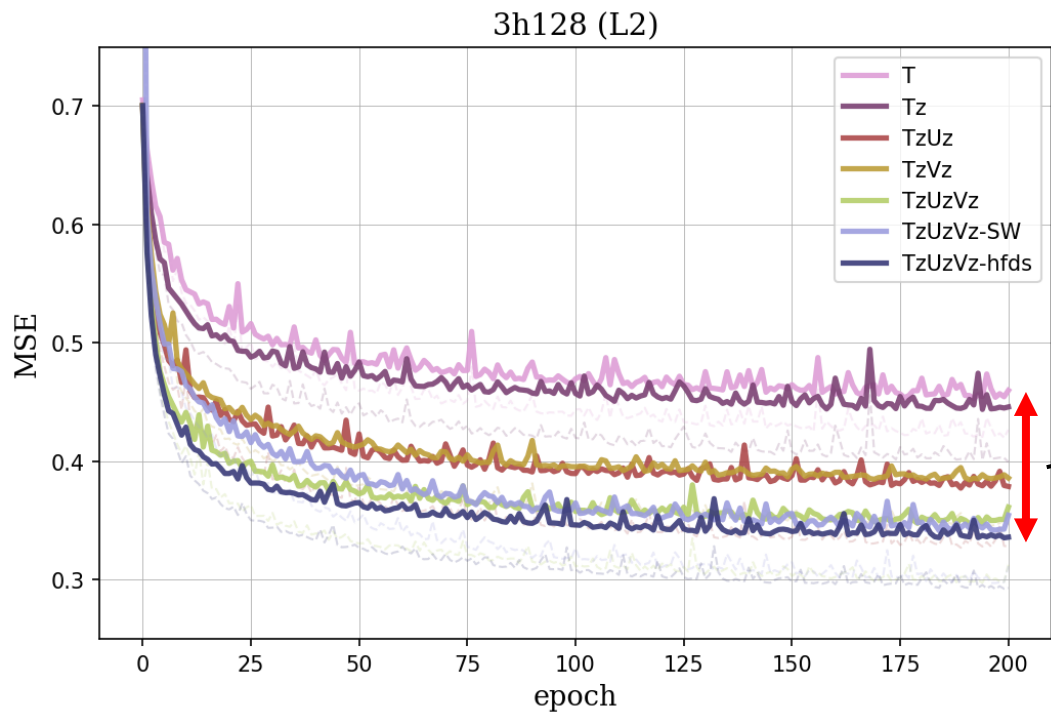


1) Learning daily climatology of temperature increments



Sensitivity to different input predictors

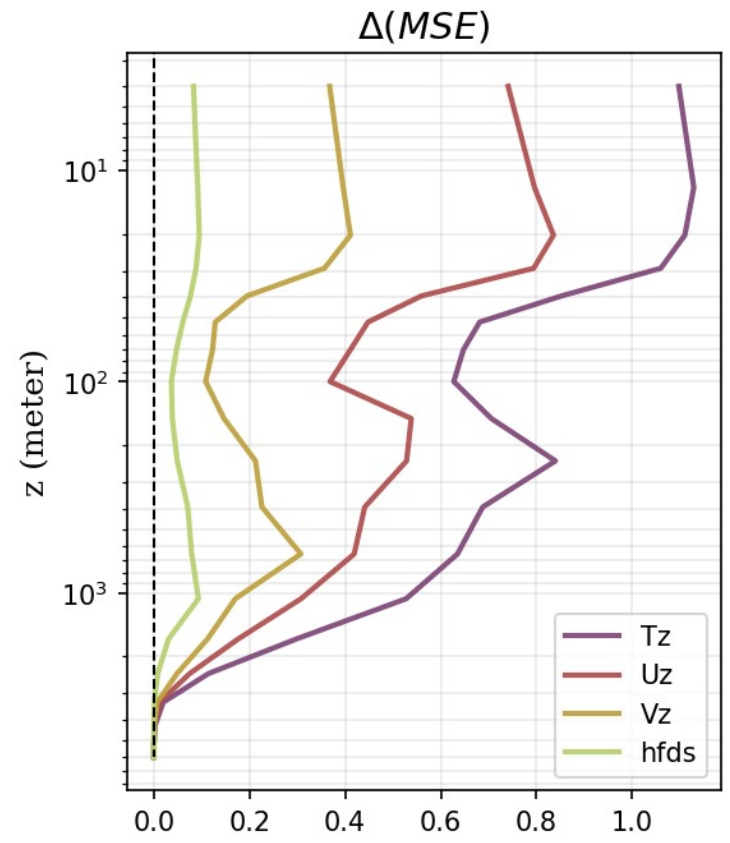
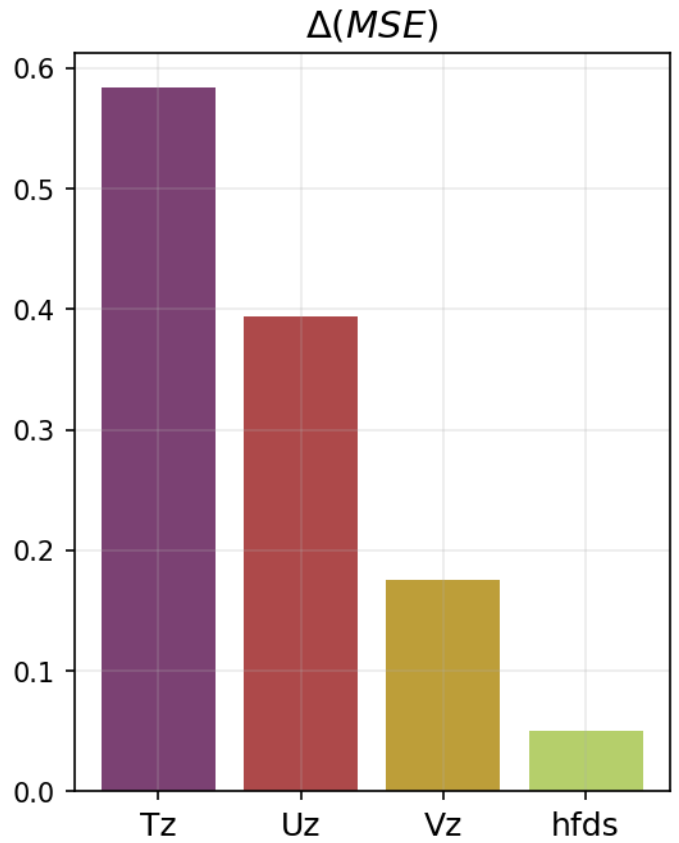
$[T]$, $[T_z]$, $[T_z U_z]$, $[T_z V_z]$, $[T_z U_z V_z]$, $[T_z U_z V_z sw]$, $[T_z U_z V_z hfds]$





Change in MSE due to randomizing input predictors

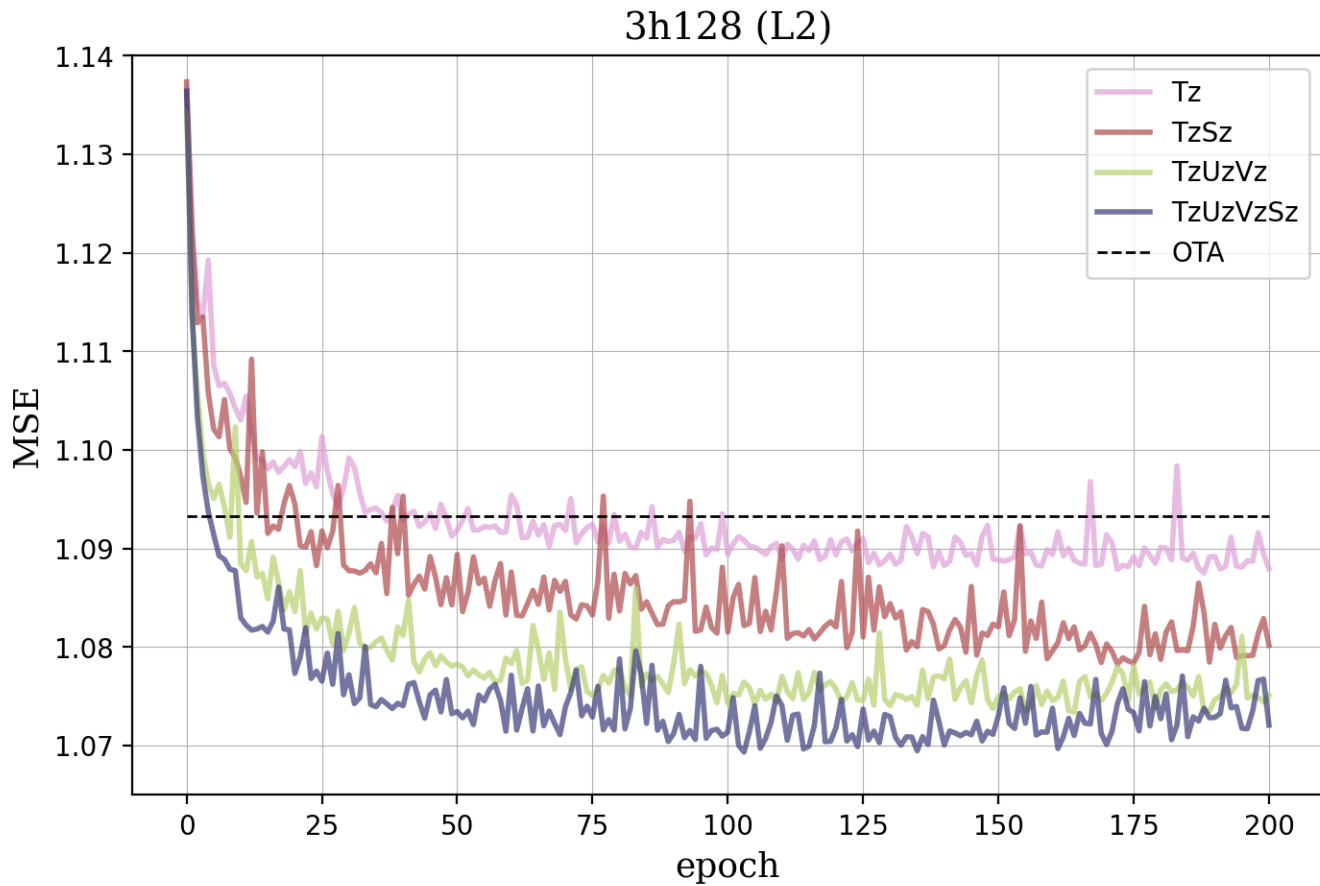
$$\overline{\delta T} = \hat{\mathcal{F}}[T_z, Uz, Vz, hfds; \theta] ; \text{NN} = 3\text{h}128$$





2) Learning raw daily temperature increments

Sensitivity to different input predictors

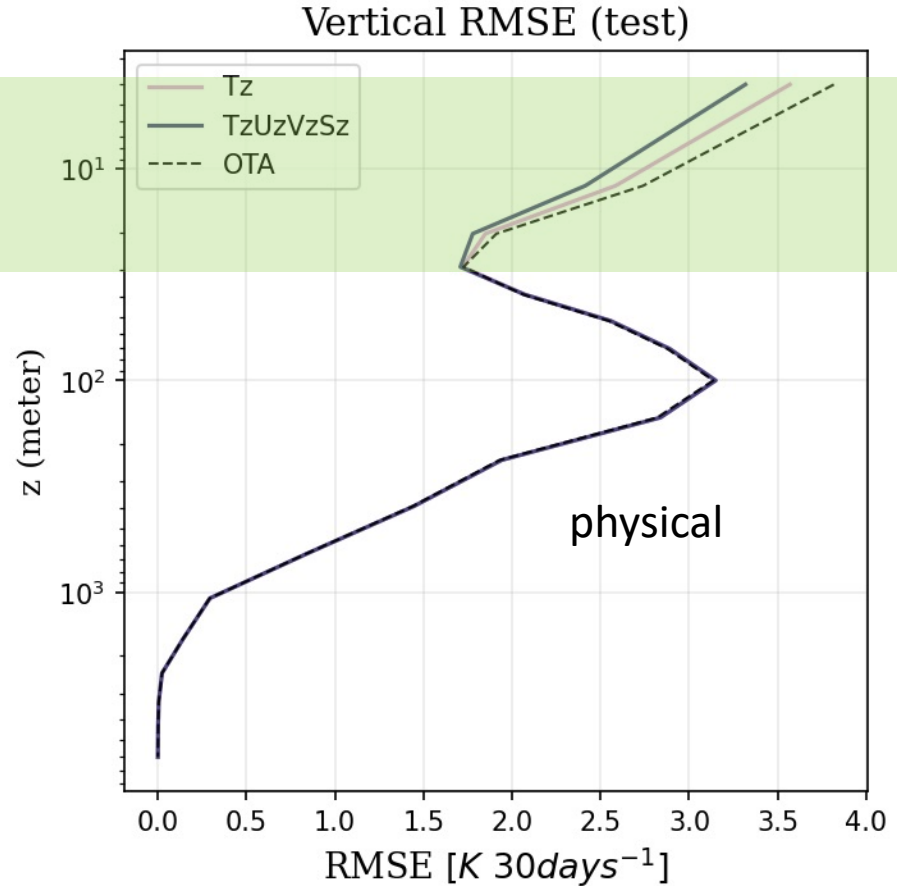
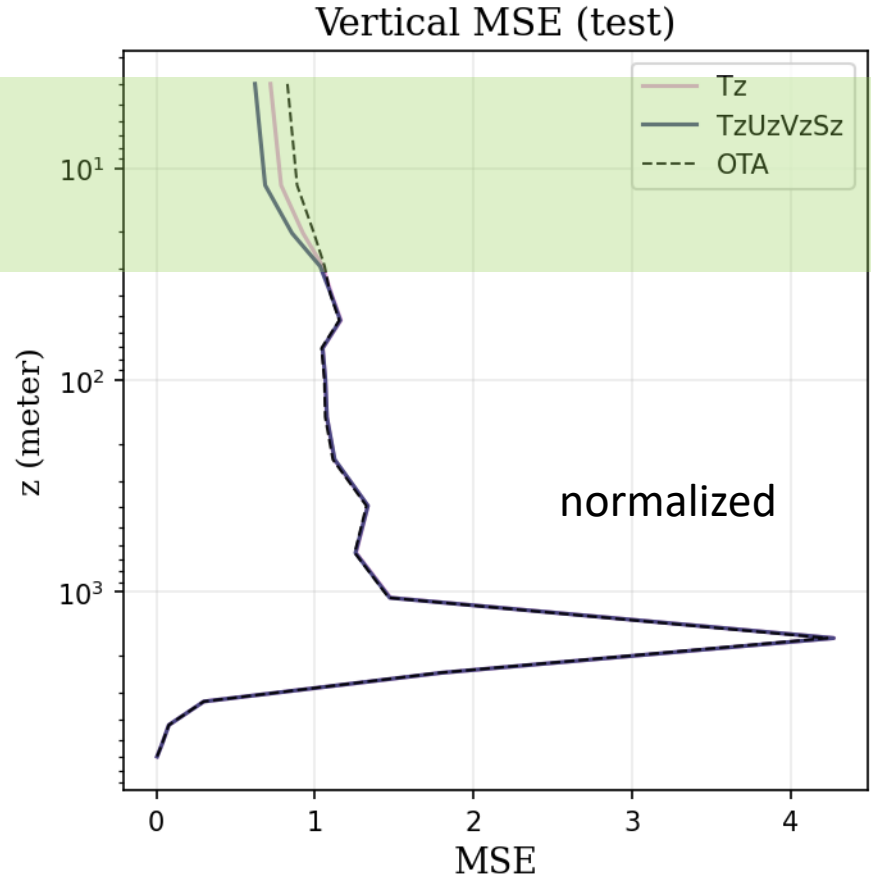


OTA = benchmark based on daily climatology of temperature increments



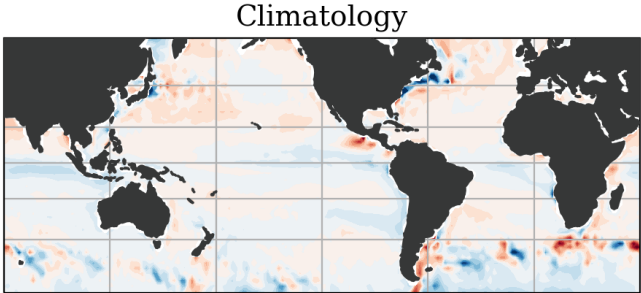
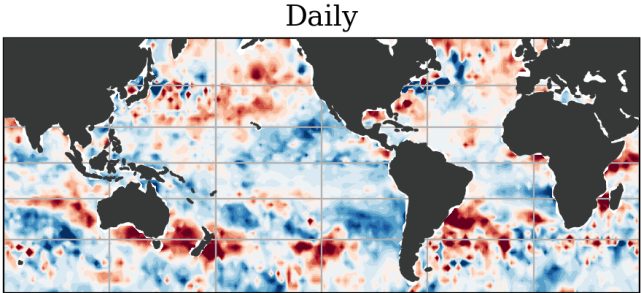
Vertical Structure of MSE/RMSE

OTA = benchmark based on daily climatology of temperature increments



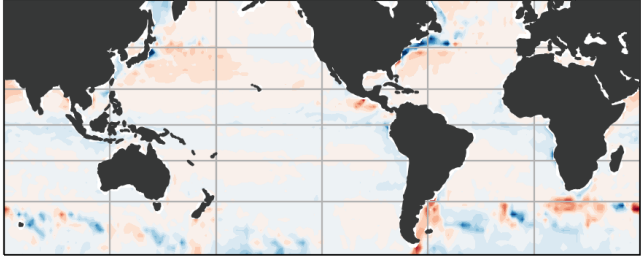
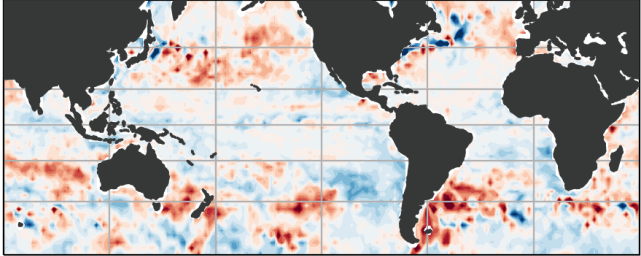
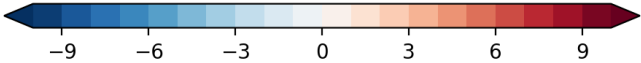
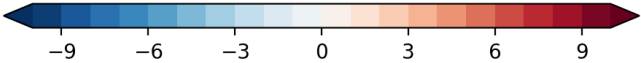
	OTA	Tz	TzUzVzSz
R ² (0-30m) (%)	12.1	18.4	25.0

2019-01-01 Truth and Predictions (learning daily vs climatology)



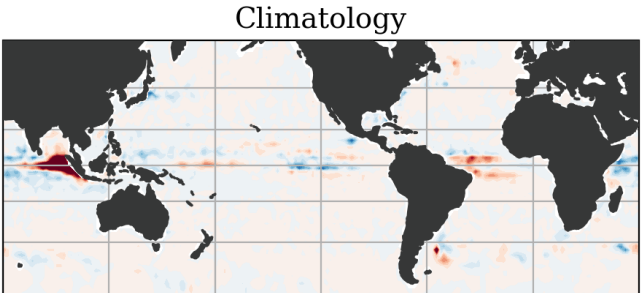
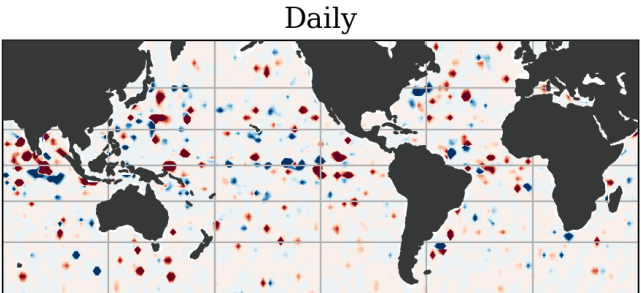
Truth

4 meter (K 30-days⁻¹)

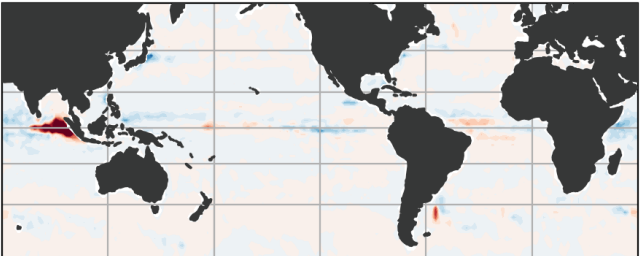
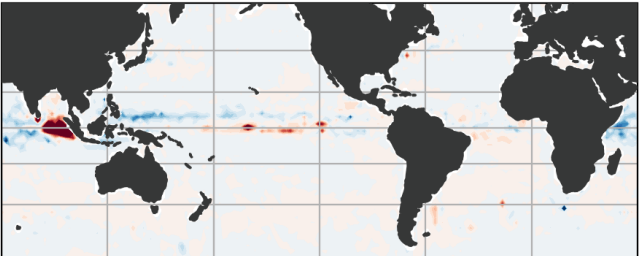


NN

100 meter (K 90-days⁻¹)

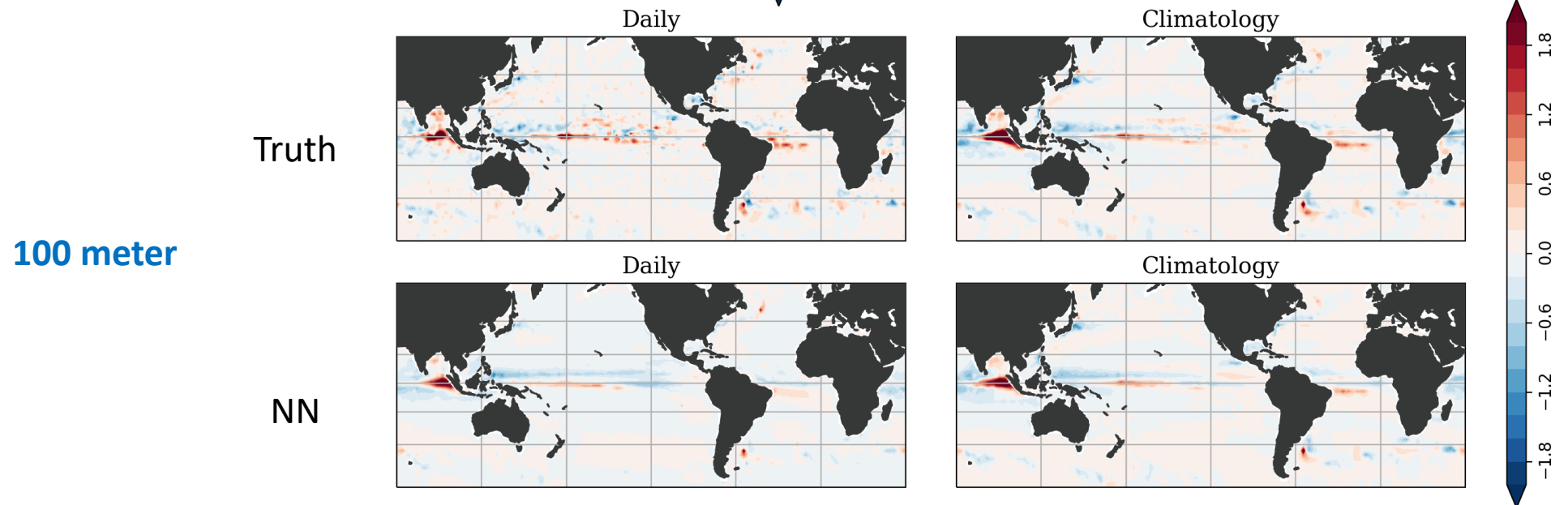
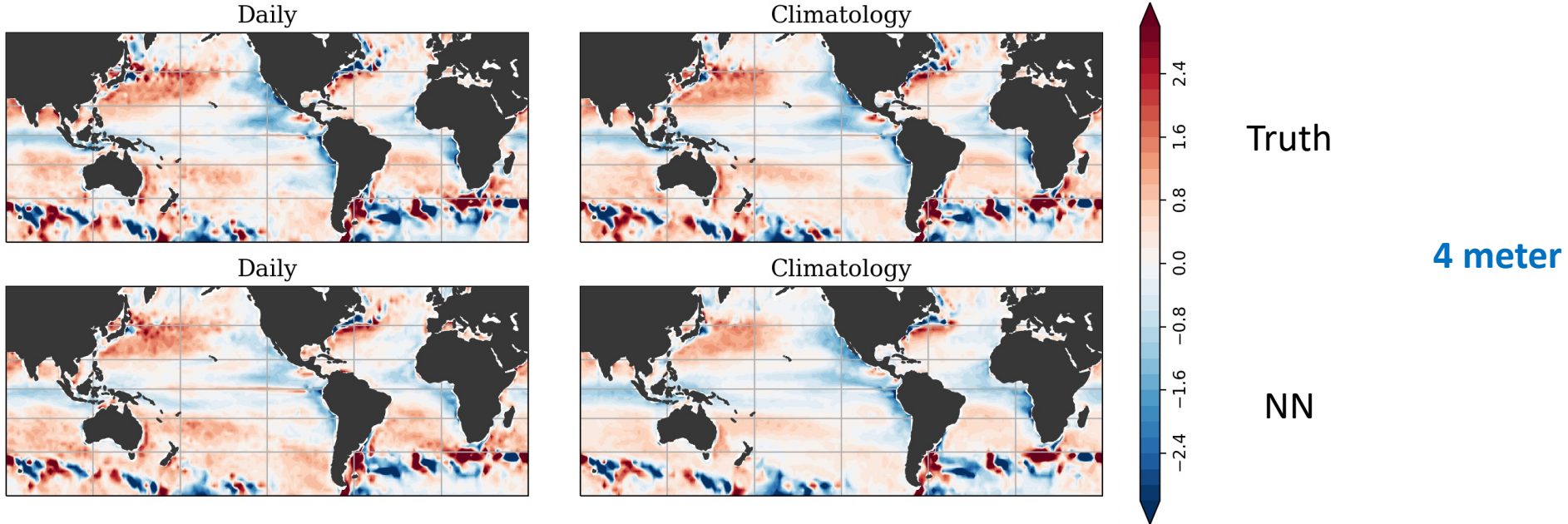


Truth



NN

2019-2021 mean Truth and Predictions (learning daily vs climatology; K 30-days⁻¹)





Conclusions

- ✓ DA increments can be used to learn systematic fast ocean model errors.
- ✓ Neural network shows significant offline skill in learning nonlinear relationships between model state and DA increments.
- ✓ The offline skill improves with the addition of dynamically relevant quantities.
- ✓ A network trained on raw daily temperature increments has better skill in the upper 30 meters which relaxes to the one trained on daily climatology of temperature increments below that.

Next...

- ✓ Expand to global domain, remove subsampling, coarsening
- ✓ Joint prediction of temperature and salinity increments.
- ✓ Interpretation and learn missing/inaccurate physics
- ✓ Online inference and evaluation