

Estimating trends in freshwater fluxes using linear response theory

Aurora Basinski and Laure Zanna

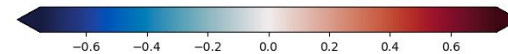
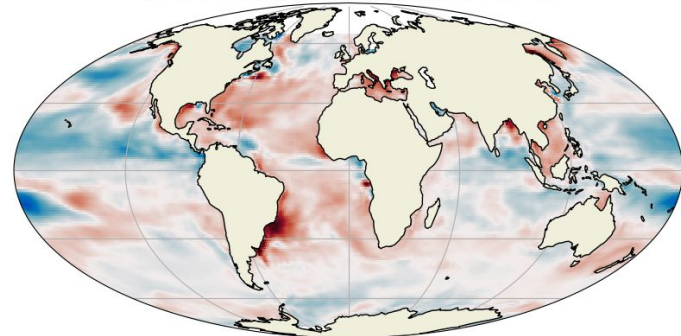
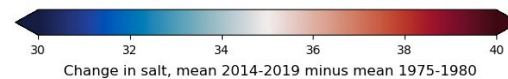
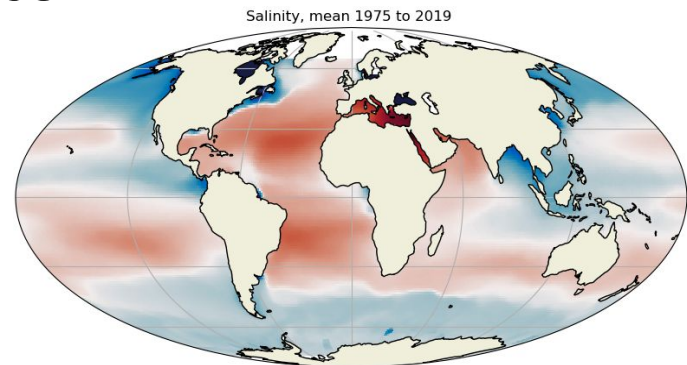
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Surface salinity patterns and freshwater fluxes

- Salinity pattern change is used to estimate amount of water cycle change as surface freshwater fluxes are difficult to directly measure
- Change in local surface salinity also affected by change in ocean transport:

$$\frac{\partial c}{\partial t} + \mathbf{u} \cdot \nabla c = \nabla \cdot (D \nabla c) + S$$

Material derivative of tracer Mixing of tracer sources -sinks

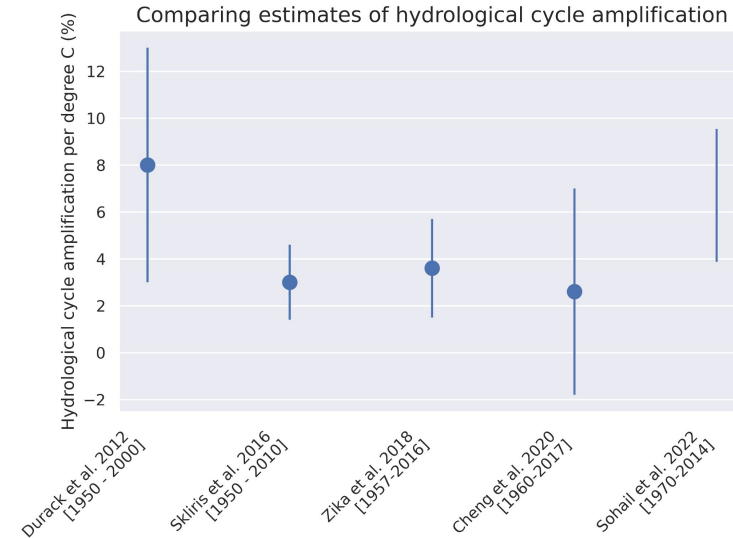


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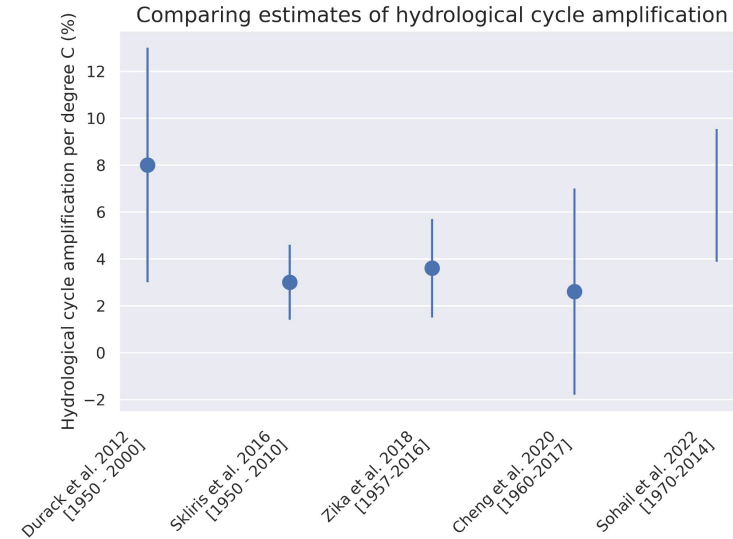
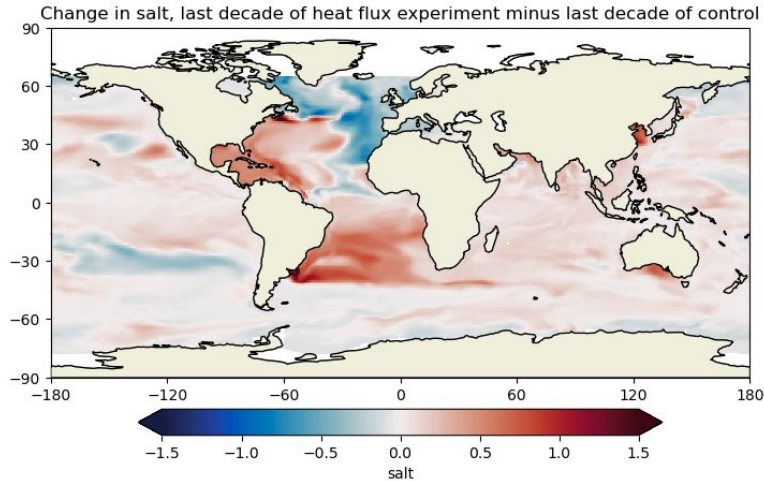
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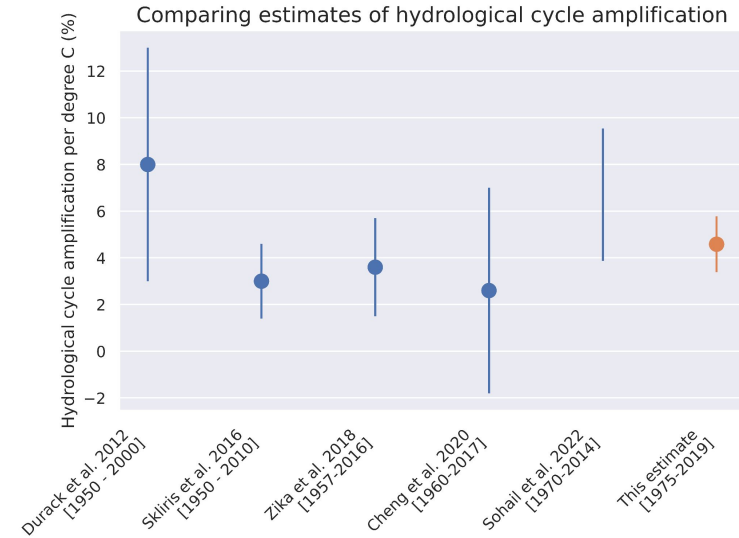
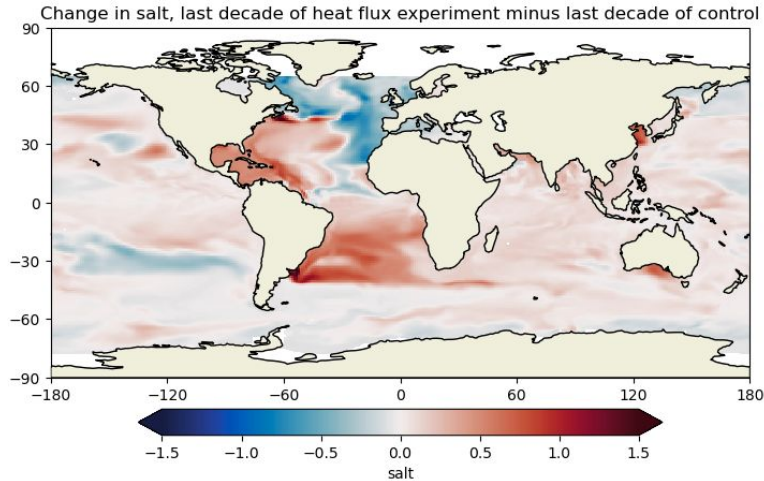
Goal of work

- **Additional physics to capture:** change in salinity from ocean circulation change is local/regional



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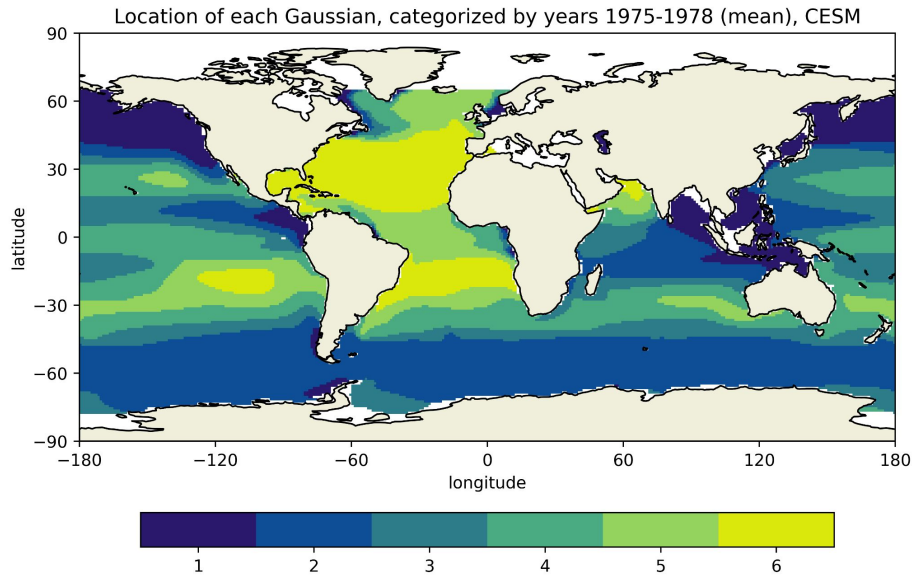
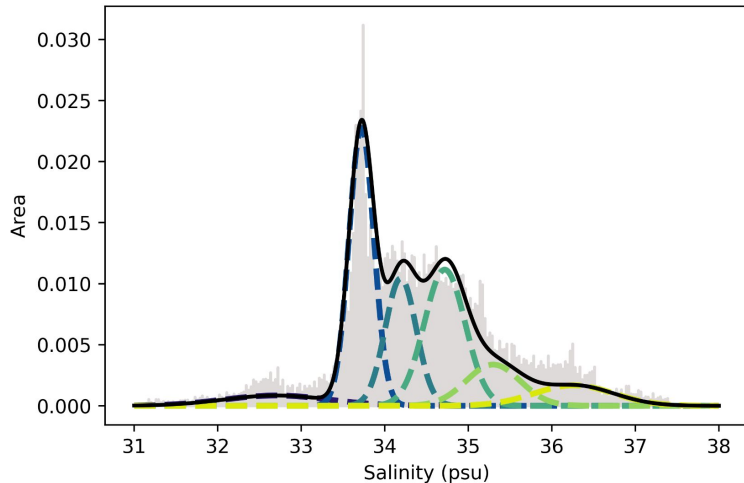
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Characterizing regions of the salinity pattern

- Find regions making up salinity pattern by fitting surface salinity distribution with a Gaussian mixture model (GMM)

Gaussian Mixture Model with 6 components in CESM data, mean 1975 to 1978

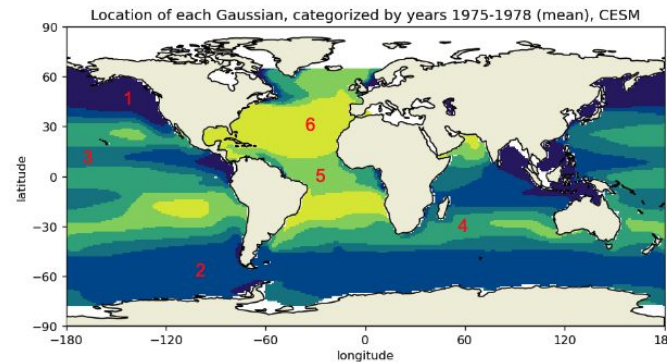


Linear response theory

- Response theory finds the change in statistical properties of a dynamical system due to a forcing

$$\boxed{\begin{array}{c} \text{Change in **ensemble** \\ \text{average of **salinity and** \\ \text{temperature in each} \\ \text{GMM region} \end{array}} = \boxed{\begin{array}{c} \text{Convolution of **response to step** \\ \text{function with time derivative of **forcing** \\ \text{time-series} \end{array}}$$

- Using normalized surface salinity/temperature in each region identified by the GMM



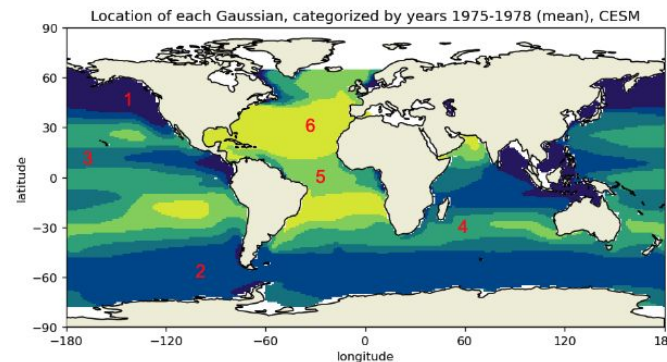
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Change in **ensemble average of salinity and temperature** in each GMM region = Convolution of **response to step function** with time derivative of **forcing time-series**

$$\langle \Delta \mathbf{Y}(t) \rangle = \int_0^t \mathbf{R}(t-t') \frac{dF}{dt'}(t') dt' + O(f^2)$$

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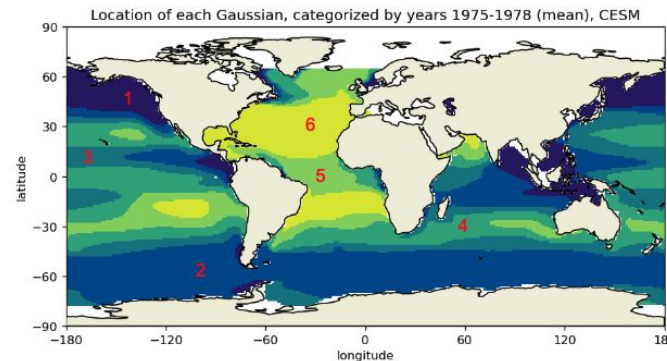
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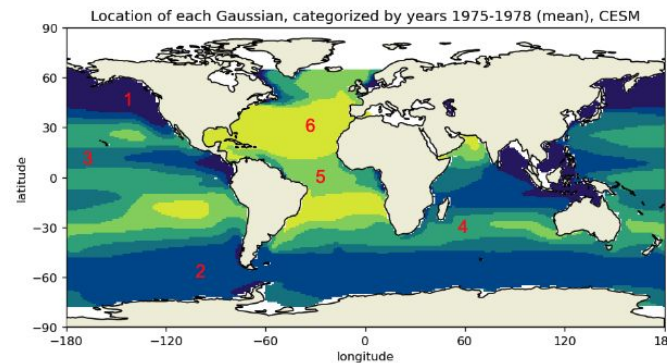
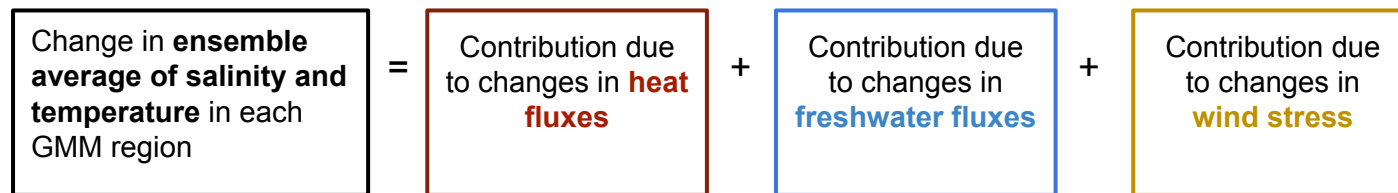
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- Using normalized surface salinity/temperature in each region identified by the GMM
- Response to step functions taken from ocean only FAFMIP → ocean models forced separately with flux perturbations (freshwater, heat, wind stress) associated with CO2 doubling



Set-up of problem

- Assume total response of regional salinity and temperature is a **linear combination** of the response to a heat flux perturbation, freshwater flux perturbation, and wind stress change

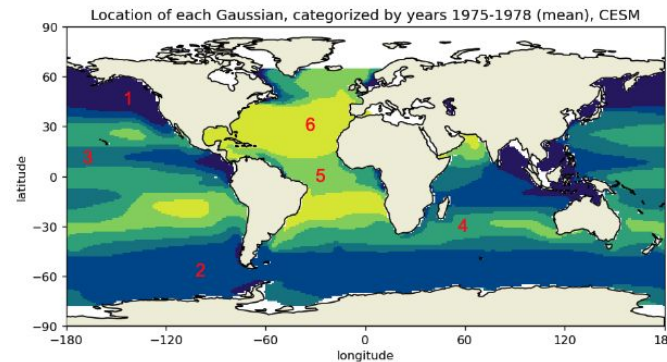


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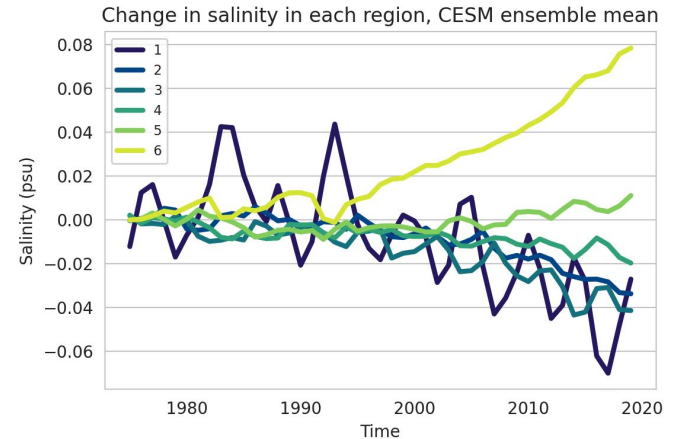
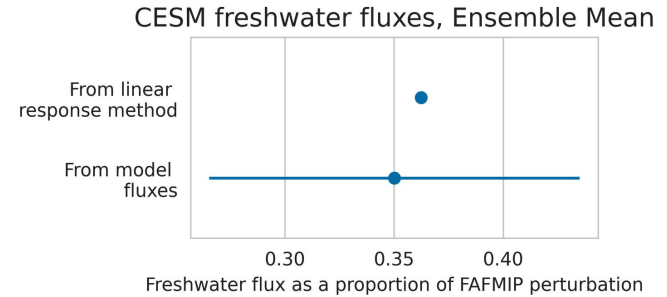
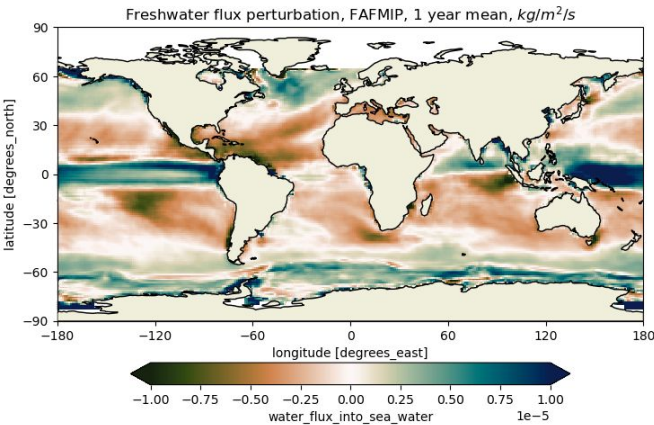
$$\begin{aligned} & \boxed{\begin{array}{l} \text{Change in ensemble} \\ \text{average of salinity and} \\ \text{temperature in each} \\ \text{GMM region} \end{array}} = \boxed{\begin{array}{l} \text{Contribution due} \\ \text{to changes in heat} \\ \text{fluxes} \end{array}} + \boxed{\begin{array}{l} \text{Contribution due} \\ \text{to changes in} \\ \text{freshwater fluxes} \end{array}} + \boxed{\begin{array}{l} \text{Contribution due} \\ \text{to changes in} \\ \text{wind stress} \end{array}} \\ & \langle \Delta \mathbf{Y}(t) \rangle = \int_0^t \mathbf{R}^h(t-t') \frac{dF^h}{dt'} dt' + \int_0^t \mathbf{R}^w(t-t') \frac{dF^w}{dt'} dt' + \int_0^t \mathbf{R}^s(t-t') \frac{dF^s}{dt'} dt' \end{aligned}$$

- Discretize and solve for time series of **heat flux**, **freshwater flux**, and **wind stress** forcing



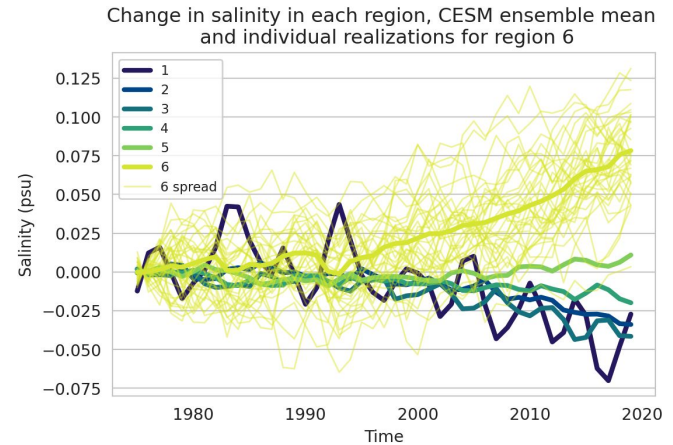
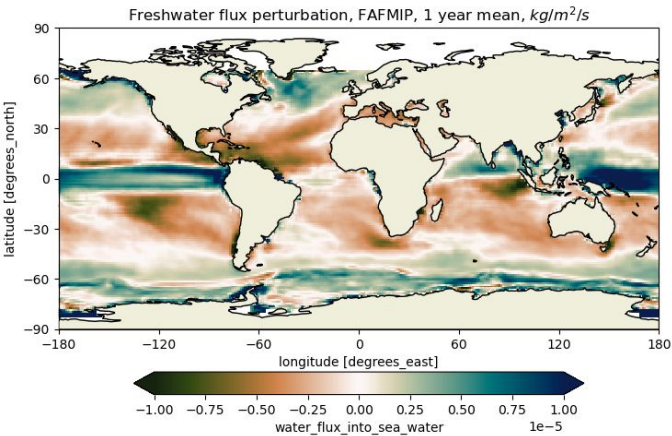
Validation of method – CESM data

- **Tested method** on salinity and temperature from Community Earth System Model (CESM) large ensemble data over the period 1975 to 2019
 - Ensemble mean: **Find true response** from model fluxes



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 - Ensemble mean: **Find true response** from model fluxes
 - Individual members: **Find true response** provided significance criteria on salinity trends

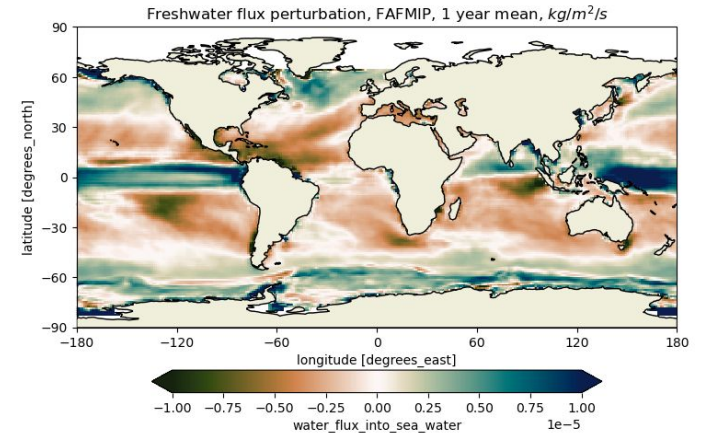


Application to observations

- Apply method to temperature and salinity surface data from Cheng et al. 2020, find: 0.303 ± 0.079 times FAFMIP perturbation

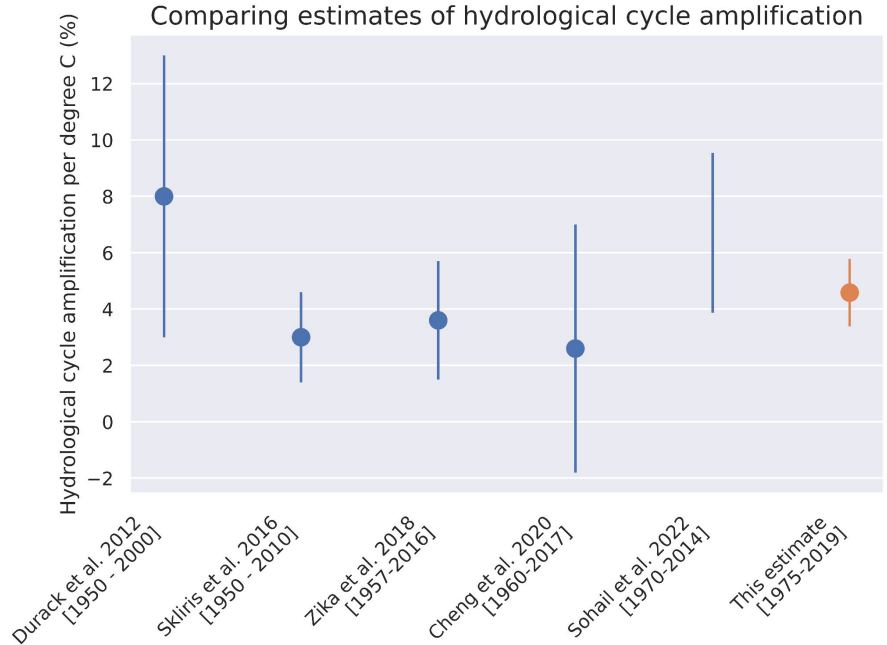


4.58 ± 1.19 % per °C



Conclusions

- Ocean transport change primarily affects surface salinity regionally
- Our method, taking this effect into account, finds the true CESM flux amplification
- Applied to observations, **agrees with previous estimates** of hydrological cycle amplification and adds confidence that the **rate has been less than Clausius-Clapeyron**



- Caveat: error bars not capturing all uncertainty