Ocean Modeling II

Parameterized Physics

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PARAMETERIZATIONS IN CESM2 POP2

• Vertical mixing (momentum and tracers)
  - surface boundary layer
  - interior
• Horizontal viscosity (momentum)
• Lateral mixing: mesoscale eddies (tracers)
• Overflows
• Submesoscale eddies (tracers)
• Estuary box model parameterization
• Solar absorption
Unresolved turbulent vertical mixing due to small-scale overturning motions parameterized as a vertical diffusion.

Guided by study and observations of atmospheric boundary layer

\[ \partial_t X = -\partial_z w'X' \quad \text{parameterize} \quad w'X' = -K_x \partial_z X \]

where \( K_x \) represents an “eddy diffusivity” or “eddy viscosity” and \( X = \{ \text{active/passive scalars or momentum} \} \).
VERTICAL MIXING SCHEME:
K-PROFILE PARAMETERIZATION (KPP)

• KPP is not just a vertical diffusion scheme because the scalars (Temp and Salinity) have non-local or “countergradient” terms $\gamma_x$

$$w'X' = -K_x(\partial_z X - \gamma_x)$$

• KPP involves three high-level steps:
  1. Determination of the boundary layer (BL) depth: $d$
  2. Calculation of interior diffusivities: $\nu_x$
  3. Evaluation of boundary layer (BL) diffusivities: $K_x$

• Diffusivity throughout the boundary layer depends on the surface forcing, the boundary layer depth, and the interior diffusivity.

• KPP produces quite large diffusivities below the boundary layer, which mixes temp and salinity quite deep in times of very strong surface wind stress, such as strong midlatitude atmosphere storms.
VERTICAL MIXING SCHEME: K-PROFILE PROFILE PARAMETERIZATION (KPP)

1. BL depth $d$ is minimum depth where the bulk Richardson # ($Ri_b$) referenced to the surface equals a critical Richardson # ($Ri_{cr}$=0.3).

$$Ri_b(d) = \frac{[B_r - B(d)]d}{|V_r - V(d)|^2 + V_t^2(d)}$$

$B_r$: near-surface reference buoyancy

$V_r$: near-surface reference horizontal velocity

$V_t(d)$: velocity scale of (unresolved) turbulent shear at depth $d$

$Ri$ measures the stability of stratified shear flow. "Boundary layer eddies with mean velocity $V_r$ and buoyancy $B_r$ should be able to penetrate to the boundary layer depth, $d$, where they first become stable relative to the local buoyancy and velocity."
VERTICAL MIXING SCHEME: K-PROFILE PARAMETERIZATION (KPP)

2. Calculation of interior diffusivities

\[ \nu_x(d) = \nu_x^s(d) + \nu_x^w(d) + \nu_x^d(d) + \nu_x^c(d) + \nu_x^t(d) \]

\( \nu_x \): interior diffusivity at depth \( d \) (below the boundary layer)

\( \nu_x^s \): (unresolved) shear instability

\( \nu_x^w \): internal wave breaking

\( \nu_x^d \): double diffusion

\( \nu_x^c \): local static instability (convection)

\( \nu_x^t \): tidal mixing

Superposition of processes sets interior vertical diffusivity, \( \nu_x \), below the surface boundary layer.
VERTEXAL MIXING SCHEME: K-PROFILE PARAMETERIZATION (KPP)

Verification example at Ocean Weather Station Papa (50°N, 145°W):

Large et al (1994)

Figure 9. Time-depth sections of 4-day averages of observed temperatures in degrees Celsius (a) from ocean weather station (OWS) Papa during the ocean year March 15, 1961, to March 15, 1962 and (b) from the standard KPP simulation of OWS Papa.
LAPLACIAN HORIZONTAL VISCOSITY

Isotropic, spatially varying coefficient in Cartesian coordinates

\[ D(U) = \left( A \ U_x \right)_x + \left( A \ U_y \right)_y \]

\[ D(V) = \left( A \ V_x \right)_x + \left( A \ V_y \right)_y \]
ANISOTROPIC HORIZONTAL VISCOSITY

\[ \partial_t u + \ldots = \partial_x (A \partial_x u) + \partial_y (B \partial_y u) \]
\[ \partial_t v + \ldots = \partial_x (B \partial_x v) + \partial_y (A \partial_y v) \]

Need the viscosity matrix to be symmetric in order to satisfy a number of constraints on the viscosity.

Small $B$ in $u$ equation does not diffuse strong, but thin, equatorial currents, such as the equatorial undercurrent.

Small $B$ in $v$ equation does not diffuse strong, but thin, western boundary currents, such as the Gulf Stream.
Mesoscale eddy mixing of tracers: Gent-McWilliams (GM) parameterization

Isopycnal Mixing in Ocean Circulation Models†

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20 March 1989 and 14 August 1989

ABSTRACT

A subgrid-scale form for mesoscale eddy mixing on isopycnal surfaces is proposed for use in non-eddy-resolving ocean circulation models. The mixing is applied in isopycnal coordinates to isopycnal layer thickness, or inverse density gradient, as well as to passive scalars, temperature and salinity. The transformation of these mixing forms to physical coordinates is also presented.

The Gent–McWilliams parameterization: 20/20 hindsight

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GFDL climate model with ocean resolution of 0.1°
Why is GM needed?

Agulhas Retroflection

$O(1^\circ)$ models do not resolve the 1$^{\text{st}}$ baroclinic deformation radius away from the equatorial regions, and hence lack the mesoscale turbulence which mixes temperature, salinity and passive tracers in the real ocean.
Ocean Observations suggest mixing along isopycnals is ~10^7 times larger than across isopycnals.

- Early ocean models parameterized the stirring effects of (unresolved) mesoscale eddies by Laplacian horizontal diffusion with $K_H = O(10^3 \text{ m}^2/\text{s})$, whereas the vertical mixing coefficient $K_v = O(10^{-4} \text{ m}^2/\text{s})$.

- Horizontal mixing results in excessive diapycnal mixing, which degrades the ocean solution: e.g. Veronis (1975) showed that it produces spurious upwelling in western boundary current regions which “short circuits” the N. Atlantic MOC.

- Thus, was a recognized need to orient tracer diffusion in z-coordinate models along isopycnal surfaces, to be consistent with observed ocean mixing rates.

Why is GM needed?

Isopycnal slopes are small $O(10^{-3})$ at most
The GM Parameterization

\[
\frac{\partial T}{\partial t} + (u + \underline{\underline{u^*}}) \cdot \nabla T = \kappa \nabla_\rho^2 T
\]

\[
w^* = -\nabla.(\kappa \nabla \rho / \rho_z), \nabla \underline{\underline{u^*}} = 0.
\]

GM (1990) proposed an eddy-induced velocity \( u^* \) in addition to diffusion along isopycnal surfaces.
GM impacts

Gent et al. (JPO, 1995): Eddy-induced velocity ($v^*, w^*$) acts to flatten isopycnals and minimize potential energy.

![Diagram of temperature and salinity distributions](image)

**Fig. 3.** Initial states of (a) temperature and (b) salt (contour interval one-quarter that of (a)). Both panels also show the streamfunction $k_p f p_0$ for the parameterized eddy-induced transport velocity.

![Diagram of temperature and salinity distributions](image)

**Fig. 4.** Distributions of (a) temperature and (b) salt after an integration time of $20\Delta t/k$. Both panels also show the streamfunction $k_p f p_0$ for the parameterized eddy-induced transport velocity. Contour intervals are the same as in Fig. 3.

![Diagram of density distribution](image)

**Fig. 5.** Density distribution at various times of the integration. (a) Initial, (b) $20\Delta t/k$, and (c) $1000\Delta t/k$. 
Baroclinic instability produces ACC eddies that try to flatten the isopycnals and produce a MOC that opposes the mean flow MOC.
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Impacts of GM

(a) Horizontal Diffusion, MOC ($u$)

(b) GM, MOC ($u$)

(c) GM, MOC ($u + u^*$)

4° x 3° x 20L ocean model

Danabasoglu et al. (1994, Science)
Impacts of GM

Deep Water Formation

(a) Horizontal Diffusion

(b) GM

In (b), deep water is formed only in the Greenland/Iceland/Norwegian Sea, the Labrador Sea, the Weddell Sea and the Ross Sea.

4° x 3° x 20L ocean model

Danabasoglu et al. (1994, Science)
**GM summary**

Mimics effects of unresolved mesoscale eddies as the sum of
- diffusive mixing of tracers along isopycnals (Redi 1982),
- an additional advection of tracers by the eddy-induced velocity $u^*$

Scheme is adiabatic and therefore valid for the ocean interior.

Acts to flatten isopycnals, thereby reducing potential energy.

Eliminates any need for horizontal diffusion in z-coordinate OGCMs
   $\Rightarrow$ eliminates Veronis effect.

Implementation of GM in ocean component was a major factor enabling stable coupled climate model simulations without “flux adjustments”.
There once was an ocean model called POP,
Which occasionally used to flop,
But eddy advection, and much less convection,
Turned it into the cream of the crop.